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A COMPUTER PROGRAM FOR
MÖSSBAUER DATA PROCESSING

by Lona M. Howser, Jag J. Singh,
and Robert E. Smith, Jr.

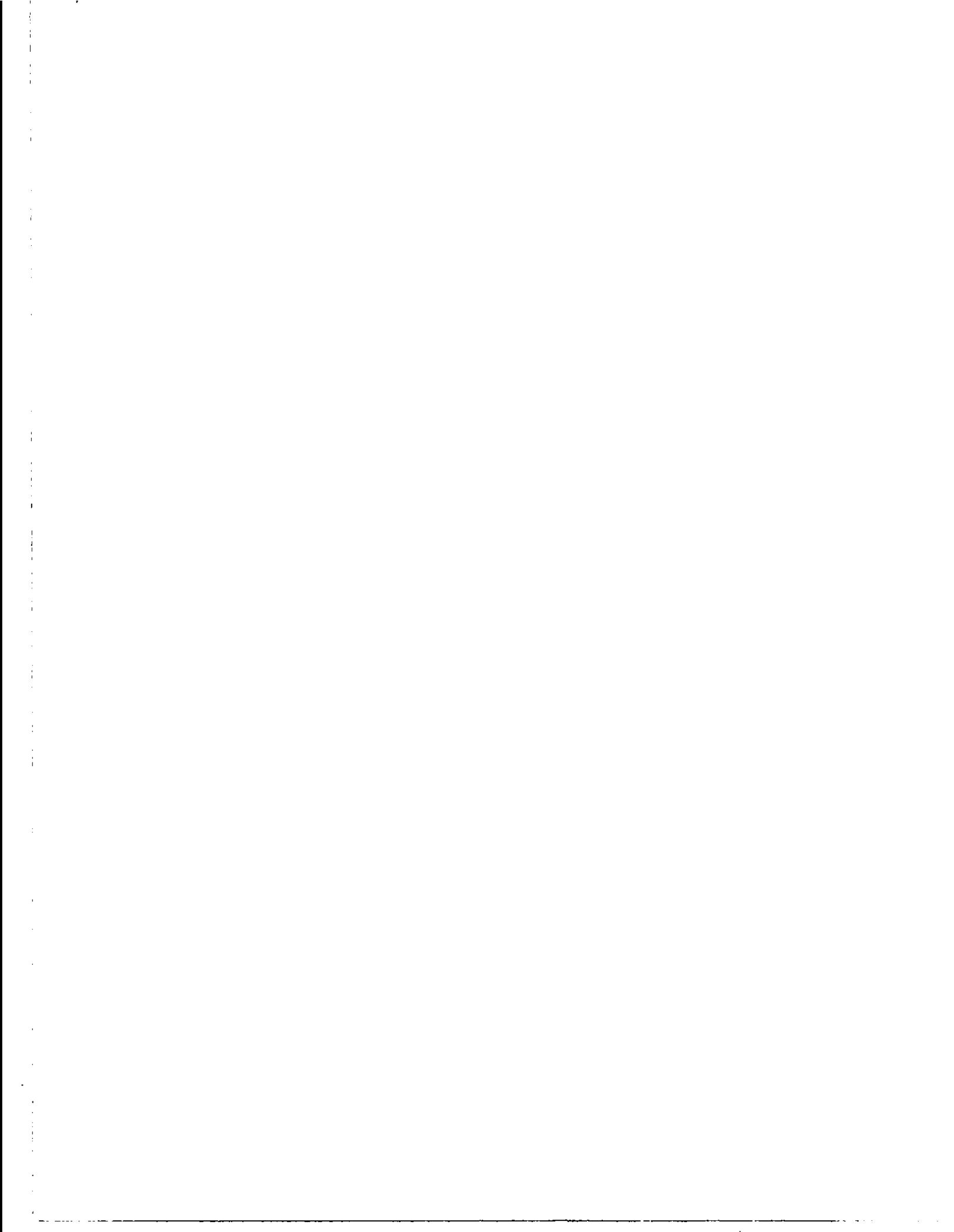
Langley Research Center
Hampton, Va. 23365

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The program is written in FORTRAN IV language for the Control Data 6000 series digital computer with the SCOPE 3.0 operating system and requires approximately 115 000 octal locations of core storage. A typical case with one absorption peak runs in 20 seconds, and a typical problem with six absorption peaks requires 50 seconds.			
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SUMMARY

A computer program to analyze Mössbauer data is presented in detail. The least-squares curve-fitting techniques described in this report apply to single-line spectra, single hyperfine spectra, or when the constituent spectra are separated well enough to let the individual absorption peaks stand alone. The present program has not been adapted for complex spectra resulting from the existence of several local environments in the absorber iron alloy. Sample problems are presented to aid the user in setting up and running the program.

The program is written in FORTRAN IV language for the Control Data 6000 series digital computer with the SCOPE 3.0 operating system and requires approximately 115 000 octal locations of core storage. A typical case with one absorption peak runs in 20 seconds, and a typical problem with six absorption peaks requires 50 seconds.

INTRODUCTION

The Mössbauer effect is one of the recent fundamental scientific discoveries that have found widespread applications in various branches of science. The theory of this phenomenon has been treated quite adequately in a number of recent publications (refs. 1 to 3) and will not be repeated herein. A brief discussion is, however, given in order to point out the basic factors that determine the wide applications of this phenomenon. This discussion will also serve to indicate the desirability — and indeed the necessity — of computer analysis of the Mössbauer spectra.

This report describes a computer program (D3290) developed at the Langley Research Center and provides the user with information necessary to use the program. Curve fitting of the Mössbauer data by using the least-squares analysis with no constraints on the amplitudes, half-widths, and positions of the absorption peaks was the technique used.

The program is written in FORTRAN IV language for the Control Data 6000 series digital computer with the SCOPE 3.0 operating system.

SYMBOLS

A	amplitude of absorption peak
a	coefficient of second-order term in equation of parabola
b	coefficient of first-order term in equation of parabola
c	constant term in equation of parabola
E	energy of incident photon
E_0	resonance energy, that is, energy equal to excitation energy of Mössbauer state above stable (ground) state
ΔE	energy uncertainty
g	gyroscopic factor
H	magnetic field at absorber nucleus
h	Planck's constant of action
$\hbar = \frac{h}{2\pi}$	
I	observed intensity
k	number of parameters
L	Lorentzian profile
M	mass of recoiling system
N	number of absorption peaks
n	number of observations
P	momentum

p	position of the peak on X-axis
x	independent variable, source velocity
y	dependent variable
Γ	width of peak at half maximum amplitude
ϵ	error in y measurement
$\lambda = \frac{\Gamma}{2}$	
μ	magnetic moment of Mössbauer state
ν	frequency
τ	mean lifetime of energy level

Subscripts:

i	observation number
j	absorption peak number
o	nominal conditions

Superscript:

T	transpose of matrix
---	---------------------

PROBLEM DESCRIPTION

Today nuclear resonant scattering of gamma radiation is a technique of major importance in nuclear physics, solid-state physics, theory of relativity, and several other areas. Reviews of this technique, often known as resonance fluorescence or the Mössbauer effect, have been reported by several authors and will not be given herein. In essence, the phenomenon can be described as follows. Various physical systems — nuclei, atoms, and molecules — are characterized by the existence of their discrete energy levels. The energy and momentum of the radiation resulting from the decay of an

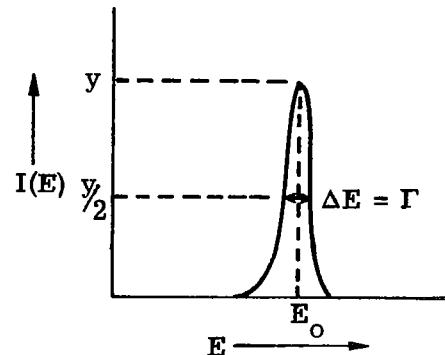
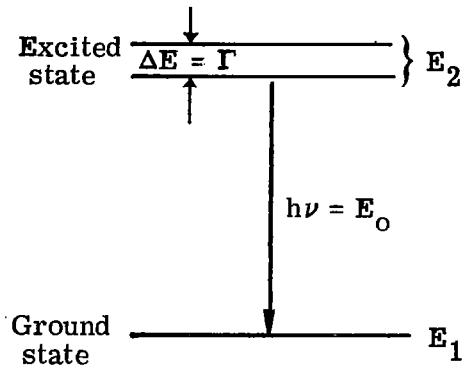


Figure 1.- Energy of an excited state with a mean life τ has a width of Γ . Stable ground state has a sharply defined energy.

excited state to a lower state are not sharply defined. Rather, the emitted radiation spectrum is expected to show a dispersion whose line width Γ is strongly related to the mean life of the excited state, as shown in figure 1. The energy spread ΔE is related to the mean life τ of the energy level by the Heisenberg uncertainty relation

$$\Delta E \gtrsim \frac{\hbar}{\tau} \quad (1)$$

Weisskopf and Wigner (refs. 4 and 5) have treated this problem in detail and have shown that

$$I(E) = \text{Constant} \frac{\Gamma}{2\pi} \frac{1}{(E - E_0)^2 + (\Gamma/2)^2} \quad (2)$$

and that the $I(E)$ curve has a Lorentzian shape. It can be seen from equation (2) that $I(E)$ will be a very sharp function of E if the mean life of the level is very large.

When a system decays from its excited state to a lower state, as a result of the requirement of conservation of linear momentum, a certain amount of energy is used up in providing for its recoil,

$$E_{\text{recoil}} = \frac{(P_{\text{recoil}})^2}{2M} = \frac{E_0^2}{2Mc^2} \quad (3)$$

where M is the mass of the recoiling system and c is the velocity of light. For a decaying nucleus,

$$E_{\text{recoil}}(\text{in eV}) = \frac{(5.37 \times 10^{-4}) E_0^2}{\text{Nuclear mass (in amu)}} \quad (4)$$

where E_0 is measured in keV. Similarly, when the emitted photon is reabsorbed by another nucleus, an equivalent recoil energy must be provided out of the photon energy content. Superimposed on this recoil loss is the energy spread caused by the thermal Doppler broadening of the emitted photons. If, however, the recoil losses at emission and reabsorption can be eliminated — for example, by effectively increasing M — it should be possible to match the emitted photon energy with the resonance energy at the absorber atom by simply giving an appropriate linear velocity to the source atoms. This fact is the basis of the Mössbauer resonance phenomenon. Since the precise emitter or absorber energies are determined by the atomic environments of the respective atoms, any changes in the atomic environments will be reflected in the new Doppler velocity required for the resonance phenomenon.¹ Thus, a Doppler velocity spectrum with an unsplit source is expected to provide useful information on the internal atomic environment of the absorber medium. A manual analysis of the Doppler velocity spectrum is very tedious and subject to large errors. Since the line width is a significant fraction of the bandwidth over which the resonance absorption is observed, it is often necessary that various parameters be estimated to within 0.1 percent, or better, of a line width. This degree of accuracy can be achieved with the help of an electronic computer. Very few programs are currently listed in the literature (ref. 6 and others cited therein), though it can be assumed that almost all laboratories engaged in Mössbauer research have their own computer programs. There are three different approaches to the analysis of a complex Mössbauer spectrum.

1. Computation of Mössbauer spectra from theoretical considerations

Computation of Mössbauer spectra from theoretical considerations is generally useful in sharply defined experimental situations. In structural applications where one is not always aware of the precise environments of the absorber atoms, it is not possible to write the expressions for the pertinent Hamiltonian or include the effects of such factors as absorber thickness and Goldanski effect, which can cause the relative intensities of various hyperfine peaks to differ from the calculated values. (See refs. 6 and 7 for calculational details.)

¹The data are normally obtained in the form of absorption as a function of source-absorber Doppler velocity. It is, however, easy to convert the velocity scale to the energy scale by using $\frac{\Delta E}{E_0} = \frac{v}{c}$ where v is the source-absorber Doppler velocity and c is the velocity of light.

2. Curve fitting of the Mössbauer data by least-squares analysis (with no constraints on the amplitudes, half-widths, and positions of the absorption peaks)

This type of program is suitable when Mössbauer lines are superimposed on a baseline parabola. Two experimental spectra are needed: the spectrum without any absorption and the spectrum with resonance absorption. The spectrum without any absorption can be approximated by a parabola. The spectrum with resonance absorption is actually the absorption peaks superimposed on a baseline parabola. A single absorption peak has a Lorentzian profile:

$$L(x) = \frac{A}{1 + \left(\frac{p - x}{\lambda}\right)^2} \quad (5)$$

where

A peak amplitude

p peak position along X-axis

$$\lambda = \frac{\Gamma}{2}$$

The curve with the absorption peak can be represented by the equation for the parabola plus the Lorentzian profile,

$$y = ax^2 + bx + c + L(x) \quad (6)$$

where a, b, and c are coefficients of the equation of the parabola representing the spectrum without any absorption.

If multiple absorption peaks are present, the absorption data are approximated by a combination of Lorentzian profiles superimposed on a parabola, which may be represented by the following equation:

$$y = (ax^2 + bx + c) + \sum_{j=1}^{N} \frac{A_j}{1 + \left(\frac{p_j - x}{\lambda_j}\right)^2} \quad (7)$$

where N is the number of absorption peaks. Equation (7) is nonlinear and contains $3N + 3$ parameters to be obtained. The technique of least-squares differential correction

is applied to estimate the parameters. A detailed discussion of the least-squares procedure is found in appendix A.

3. Curve fitting of the Mössbauer data by constrained least-squares analysis

This type of analysis is used when the Mössbauer spectrum is too complex to be treated by procedure 2 alone. The constrained program makes use of the theoretical relationship that exists between the parameters of the Mössbauer lines. Thus, for example, a magnetic iron spectrum could be fitted with five parameters (ref. 8) instead of the 21 parameters required in an unconstrained program.

Most of the available programs have been written for specific geometries. The computer program described in this report should be of general use for the reduction of Mössbauer data based on procedure 2. A description of the program and its application to a typical problem at this laboratory are given herein.

PROGRAM DESCRIPTION

The computer program D3290 was written in FORTRAN IV language for the Control Data 6000 series digital computer with the SCOPE 3.0 operating system. With the present dimensions, the program requires approximately 115 000 octal locations of core storage. A typical case with one absorption peak runs in 20 seconds, and a typical case with six absorption peaks runs in 50 seconds. Tape unit 7 is used for temporary storage during job execution.

By using initial estimates for the parameters as input to the program, a solution is obtained and the results are plotted. The amplitude, the position of the peak on the X-axis, and the width of the peak at half maximum amplitude are the main parameters obtained. Values of derived parameters such as quadrupole splitting, isomer shift, and magnetic hyperfine splitting can be obtained from the main parameters. By making use of the input variables IFLAG and IERR (see input description), the same case can be run with statistical errors on the dependent values. This feature is helpful in obtaining a range of error on the solution parameters. The program allows for a maximum of six absorption peaks and 1025 dependent and independent values. DIMENSION statements can be easily changed to allow for a larger number of absorption peaks.

FORTRAN Variable Description

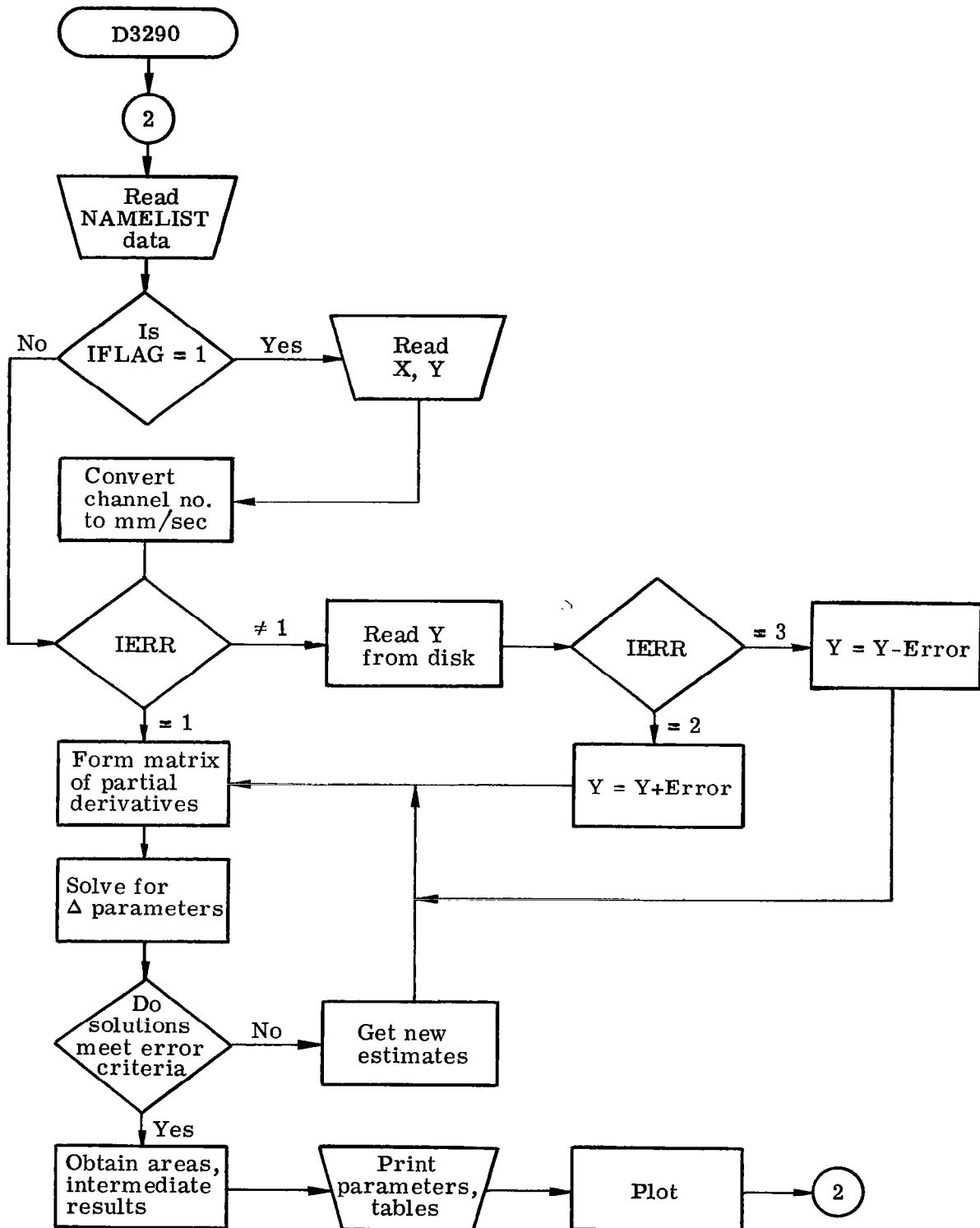
The following list contains a description of the significant FORTRAN variables appearing in the program. The dimensions for each array are beside the variable in the notation $A(m,n)$. The variables which are input will not be presented here, since they are described in the input section.

<u>FORTRAN variable</u>	<u>Description or symbol</u>
A(6)	A_j
AREA(6)	Area between the curve and the parabola for each peak
ARRAY(1025,21)	Matrix of partial derivatives
B(21,22)	Matrix of coefficients for solution of the simultaneous equations
C(21,1)	Right-hand side of solution of the simultaneous equations
CGAM(6)	λ_j
CO	Initial estimate for parameter c in the equation of the parabola
COMPY(1025)	Computed function values (equivalent to the second column of ARRAY)
ITER	Iteration count
P(6)	p_j
PAR(1025)	Baseline parabola (equivalent to the first column of ARRAY)
R(1025)	Residuals
STD	Standard deviation of residuals

Program D3290, Flow Chart, and Listing

Program D3290 is the main program. It reads and prints the input, sets up the iteration loop, solves the set of simultaneous equations, and obtains the parameter values. It evaluates the other parameters desired for output, prints the output, and calls the plotting routines to plot the results.

The following is the flow chart for the program:



The following is the listing of the program:

```
PROGRAM D3290 ( INPUT=201,OUTPUT= 201,TAPE5=INPUT,TAPE6=OUTPUT,
1 SCFILE,TAPE7=SCFILE)
  COMMON A(6),AC(6),AREA(6),ARRAY(1025,21),B(21,21),C(21,1),
1 CGAM(6),CGAMC(6),ERROR(21),P(6),PO(6),R(1025),X(1025),Y(1025)
  DIMENSION CCMPY(1025),PAR(1025),YYPAR(2050)
  DIMENSION PRM(3),XM(2)
  EQUIVALENCE (PRM(1),SAO),(PRM(2),BO),(PRM(3),CO)
  EQUIVALENCE (CCMPY(1),ARRAY(1,1)),(PAR(1),ARRAY(1,2))
  EQUIVALENCE (YYPAR(1),ARRAY(1,3))
  DIMENSION IPIVCT (21),INDEX(21,2)
  EQUIVALENCE (R(1),IPIVOT(1)),(R(22),INDEX(1,1))
  DIMENSION V(21,21)
  EQUIVALENCE (V(1,1),ARRAY(1,4))
  NAMELIST /NAM1/  AO,BO,CGAMO,ERROR,IERR,IFLAG,IPRINT,NP,PO,SAO
1 ,VELB
  DATA XM,YM/20H X VALUES   (MM/SEC),9H Y VALUES/
  NRC=21
  CALL CALCCMF
  CALL LEROY
  CON=1
2 READ (5,NAM1)
  IF (EOF,5) 4,6
4 CALL CALPLT (C,0,999)
  STOP
6 CONTINUE
  IF (IFLAG.NE.1) GO TO 27
  READ (5,S) ID,NO
9 FORMAT (5X,I5,I10)
  IF (NO) 10,15,19
10 NO=-NO
  CON=-1
19 READ (5,11) (X(I),Y(I),I=1,NO)
11 FORMAT (8(F4.0,F6.0))
C SCAN ARRAY AND INTERPOLATE FOR BAD POINTS
  J=1
  DO 18 I=2,NC
  IF (Y(I).EQ.0.) GO TO 16
  IF (J.EQ.1) GO TO 18
  FAC= (Y(I)-Y(K))/J
  J=J-1
  DO 13 N=1,J
13 Y(K+N)=Y(K-1+N)+ FAC
  J=1
  GO TO 18
16 IF (J.EQ.1) K=I-1
  J=J+1
18 CONTINUE
  REWIND 7
  WRITE (7) (Y(I),I=1,NO)
  CO=Y(1)
  ANO=NO-1
  X1=X(1)
  SUM = VELB *2.
  DO 21 I=1,NC
  X(I)= (VELB-SUM* (X(I)-X1)/ANO) *CON
21 CONTINUE
```

```

27  ITER=0
    WRITE (6,27CC) ID,IERR
2700 FORMAT (*1CASE NO.*I5,5X*IERR=*I3)
    IF (IERR.EC.1) GO TO 32
    REWIND 7
    READ (7) (Y(I),I=1,NO)
    GO TO (32,28,29),IERR
28  DO 2810 I=1,NC
    Y(I)=Y(I)+ SQRT(Y(I))
2810 CONTINUE
    GO TO 32
29  DO 2910 I=1,NC
    Y(I)=Y(I)- SQRT(Y(I))
2910 CONTINUE
32  DO 40 I=1,NC
    XSQ=X(I)**2
    ARRAY(I,1)=XSQ
    ARRAY(I,2)= X(I)
    ARRAY(I,3)=1.
    FX= SA0*XSC + BO*X(I)+ CO
    R(I)=(Y(I)- FX)
40  CONTINUE
80  NP3=3*NP+3
    N1=NP3+1
C INITIALIZE PLCT RCUTINE AND SET ORIGIN
    MM=4
    DO 110 M=1,NP
        SAVE= CGAMC(M)**2
        DO 100 I=1,NC
            SAVE1= PO(M)- X(I)
            SAVE2= SAVE +SAVE1**2
            ARRAY(I,MM)= SAVE/SAVE2
            ARRAY(I,MM+1)=-2.0*AO(M)*SAVE*SAVE1/SAVE2**2
            ARRAY(I,MM+2)= 2.0*AO(M)*CGAMO(M)*SAVE1**2/SAVE2**2
            FX= AO(M) *ARRAY(I,MM)
            R(I)=R(I)-FX
100  CONTINUE
    MM=MM+3
110  CONTINUE
C ARRAY TRANSPCSE * ARRAY
    DO 120 K=1,NP3
        DO 118 M=1,NP3
            B(K,M)=0.0
            DO 115 I=1,NO
                B(K,M)=ARRAY(I,K)*ARRAY(I,M) + B(K,M)
115  CONTINUE
118  CONTINUE
120  CONTINUE
C ARRAY TRANSPCSE * R
    DO 129 K=1,NP3
        C(K)=0.0
        DO 125 M=1,NC
125  C(K)=ARRAY(N,K)*R(M) + C(K)
129  CONTINUE
    CALL MATINV (B,NP3,C,1,DET,IPIVOT, INDEX,21,ISCALE)
    ITER=ITER+1
    DO 142 I=1,3
        TEST1= ABS(C(I)/PRM(I))
        IF (TEST1.GT.ERROR(I)) GO TO 800

```

```

142 CONTINUE
MM=4
DO 145 M=1,NP
TEST1= ABS(C(MM)/AO(M))
IF (TEST1.GT.ERROR(MM)) GO TO 800
TEST1= ABS(C(MM+1)/PO(M))
IF (TEST1.GT.ERROR(MM+1)) GO TO 800
TEST1= ABS(C(MM+2)/CGAM0(M))
IF (TEST1.GT.ERROR(MM+2)) GO TO 800
145 CONTINUE
165 MM=4
SAO=SAO+ C(1)
BO=BO+C(2)
CO=CO + C(3)
DO 168 M=1,NP
A(M)= C(MM)+ AO(M)
P(M)= C(MM+1) + PO(M)
CGAM(M)= C(MM+2)+ CGAM0(M)
MM= MM+3
168 CONTINUE
DO 170 I=1,NO
R(I)=Y(I)
170 COMPY(I)=C.0
DO 174 M=1,NP
DO 172 I=1,NC
COMPY(I)=A(M)*CGAM(M)**2/(CGAM(M)**2+(P(M)-X(I))**2)+ COMPY(I)
172 CONTINUE
174 CONTINUE
DO 176 I=1,NC
PAR(I)= SAC*X(I)**2 + BO*X(I) +CO
COMPY(I)= CEMFY(I) + PAR(I)
176 R(I)=R(I)-CCMPY(I)
STD=0.0
DO 178 I=1,NC
178 STD=R(I)**2+ STD
ANN=NO-NP3
STD=STD/ANN
DO 181 I=1,NP3
DO 180 J=1,NP3
V(I,J)=B(I,J)*STD
180 CONTINUE
181 CONTINUE
DO 183 I=1,NP3
183 V(I,1)=SQRT(V(I,1))
STD=SQRT(STD)
P1=VELB**3/3.
P2=VELB**2/2.
AR1=SAO*P1 + BO*P2 + CO*VELB
AR2= -SAO*P1 + BO*P2 -CO *VELB
AREA1= AR1 - AR2
AREA2=0.
WRITE (6,185) SAO,V(1,1),BO,V(2,1),CO,V(3,1),ITER
185 FORMAT (48F0.0,10E15.8, 1H*,19X,1H-,33X,1H-,33X,1H-/*ONO. OF ITERATIONS=*I6)
2 *(T*E9.3,*)*
3           1H+,19X,1H-,33X,1H-,33X,1H-/*ONO. OF ITERATIONS=*I6)

```

```

DO 200 M=1,NP
C
C EVALUATE INTEGRALS TO GET AREAS FOR PHI2
C
C1= A(M)*CGAM(M)**2
AC=CGAM(M)**2 +P(M)**2
BC = -2.0* F(M)
CC = 1.0
Q = 4.0 *AC*CC -BC**2
IF (Q) 186,940,187
186 FAC = 12.*CC + BC
FAC1= SQRT (- Q)
FAC2= (FAC - FAC1) /(FAC + FAC1)
FAC = ALOG (FAC2)
AR1 = FAC / FAC1
FAC = -12.*CC + BC
FAC2= (FAC - FAC1)/ (FAC + FAC1)
FAC = ALOG (FAC2)
AR2 = FAC/ FAC1
AREA(M)=(AR1- AR2) *C1
AREA2= AREA(M) + AREA2
GO TO 189
187 FAC1= SQRT (C)
FAC =(12.*CC + BC )
FAC2=ATAN2(FAC,FAC1)
AR1 = 2.0 * FAC2 / FAC1
FAC =(-12.*CC +BC )
FAC2=ATAN2(FAC,FAC1)
AR2 = 2.0* FAC2/ FAC1
AREA(M)=(AR1- AR2) *C1
AREA2= AREA(M) + AREA2
189 CONTINUE
PHI2=ABS(AREA2/AREA1)
AIS=P(M)
GAM=2.*CGAM(M)
WRITE (6,1SC) M
190 FORMAT (*CPARAMETERS FOR PEAK*I3)
WRITE (6,1SS) AIS,GAM
195 FORMAT (*0IS=*E15.8,5X*GAM=*E15.8)
MS=3*M
WRITE (6,205) A(M),V(MS+1),P(M),V(MS+2),CGAM(M),V(MS+3),AREA(M)
200 WRITE (6,2C4)
204 FORMAT (1H+,1EX,1H-,33X,1H-,36X,1H-)
205 FORMAT (*0A=*E15.8, *(T*E9.3,*)*,5X*P=*E15.8, *(T*E9.3,*)*5X*CGAM=
2*X*E15.8, *(T*E9.3,*)*,5X*AREA=*E15.8)
IF (NP.NE.1) GO TO 207
C EVALUATE THESE PARAMETERS IF ONLY ONE PEAK
YMAX=SAO*P(M)**2 + BO*P(M) + CO
PHI1=A(M)/YMAX
PDP=PHI1/PHI2
WRITE (6,2CE) PHI1,PHI2,PDP
206 FORMAT (*0PHI1=*E15.8,5X*PHI2=*E15.8,5X*PHI1/PHI2=*E15.8)
GO TO 210
C EVALUATE THESE PARAMETERS IF MORE THAN ONE PEAK
207 AIS= .25 *(F(1) + P(2) + P(5) + P(6))
QS=.25*(P(2)+ P(5)- P(1)-P(6))
G01= P(5) - P(3)
G02 = P(4) - P(2)
G1 = P(3) - P(2)

```

```

AM1 = (ABS(A(6)) + ABS(A(1)))/(ABS(A(5)) + ABS(A(2)))
AM2 = (ABS(AREA(1))+ ABS(AREA(6)))/(ABS(AREA(2)) + ABS(AREA(5)))
WRITE (6,205)
209 FORMAT(*OTHERS PARAMETERS HAVE BEEN OBTAINED FOR MULTIPLE PEAKS*)
WRITE (6,208) AIS,QS,G01,G1,AM1,AM2,PHI2
208 FORMAT (*0 IS=*E15.7,5X* QS=*E15.7,5X*G01=*E15.7,5X*G02=*E15.7,5X
1 * G1=*E15.7/* M1=*E15.7,5X* M2=*E15.7,5X*PHI=*E15.7)
210 IF (IPRINT.EQ.0) GO TO 380
WRITE (6,230)
230 FORMAT (*CHANNEL NO.*3X*X MM/SEC*14X*Y*14X*COMPUTED Y*10X
1 *RESIDUALS*10X*PARABOLA*)
DO 315 I=1,NO
WRITE (6,312) I,X(I),Y(I),COMPY(I),R(I) ,PAR(I)
312 FORMAT (I6,5E20.8)
315 CONTINUE
WRITE (6,370) STD
370 FORMAT (*STD=*E15.6)
380 K=1
IF (IERR.NE.1) GO TO 2
C COMPUTE MINIMUMS AND MAXIMUMS
XPG=12.
CALL ASCALE (X,XPG,NO,K,10.)
YPG=10.
NUM=2*NO
DO 400 I=1,NO
400 YYPAR(I)=Y(I)
N1=NO+1
DO 410 I= N1,NUM
410 YYPAR(I)=PAR(I-NO)
CALL ASCALE (YYPAR,YPG,NUM,K,10.)
NP1=NO+1
NP2=NO+2
Y(NP1)=YYPAR(NUM+1)
Y(NP2)=YYPAR(NUM+2)
PAR(NP1)=Y(NP1)
PAR(NP2)=Y(NP2)
COMPY(NP1)=Y(NP1)
COMPY(NP2)=Y(NP2)
C DRAW X AXIS
XDV=10.
XTIC=1.
CALL AXES (C.,0.,0.,XPG,X(NP1),X(NP2),XTIC,XDV,XM,.15,-20)
C DRAW Y AXIS
YDV=10.
YTIC=1.
CALL AXES (C.,C.,90.,YPG,COMPY(NP1),COMPY(NP2),YTIC,YDV,YM,.15,9)
C
C PLOT CURVE
C
CALL PLPT (X,Y,NO)
IF (ITER.GE.3C) GO TO 600
340 CALL LINPLT (X,COMPY,NO,K,0,0,0,0,0)
CALL LINPLT (X,PAR,NO,K,0,0,0,0,0)
C ESTABLISH A NEW REFERENCE POINT FOR THE NEXT GRAPH
600 CALL CALPLT (14.,0.,-3)
GO TO 2

```

```

800 MM=4
    IF (ITER.GE.30) GO TO 1000
    DO 900 M=1,NP
        AO(M)= C(MM)+ AO(M)
        PO(M)=C(MM+1) + PO(M)
        CGAMO(M)=C(MM+2) + CGAMO(M)
    895 MM=MM+3
    900 CONTINUE
    920 SAO=SAO+ C(1)
        BO= BO+ C(2)
        CO =CO+ C(3)
        GO TO 32
    940 WRITE (6,550) A,P,CGAM
    950 FORMAT (*0H*EN EVALUATING THE INTEGRALS Q EQUALS 0., THIS CANNOT
    1 BE, A,P,CGAM ARRAYS FOLLOW */(7E18.6))
        GO TO 2
1000 DO 1020 I=1,NC
1020 PAR(I)=Y(I)
        GO TO 380
    END

```

Subroutine MATINV

Subroutine MATINV is described in detail in appendix B. Program D3290 uses this subroutine to invert and solve the matrix of normal equations.

Plotting Routines

The plotting routines used are from the CalComp software package. Output for plotting is routed to a tape during job execution and after job completion is plotted on a CalComp digital incremental plotter. The arrays X, Y, COMPY, and PAR are used for plotting.

PROGRAM USAGE

Input

The input used for the program is a combination of FORTRAN NAMELIST and FORTRAN READ statements. The NAMELIST data are the first data and are followed by the data cards to be read by READ statements. A deck setup is shown in figure 2, and an example of input data is shown in appendix C.

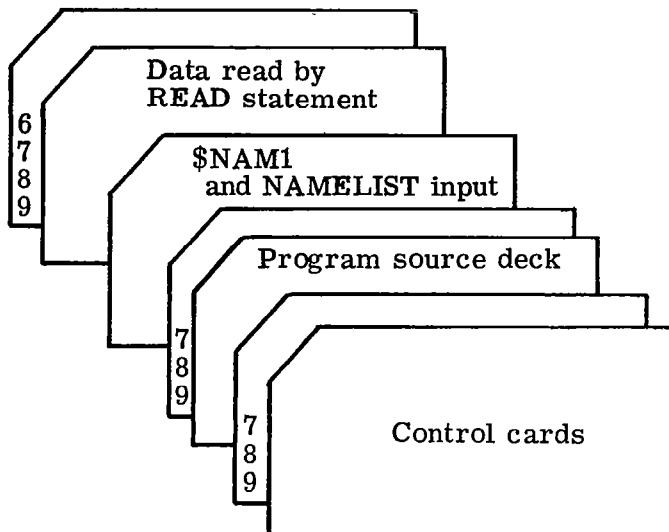


Figure 2.- Deck setup.

NAMELIST data.- The following list contains the input variables loaded by FORTRAN IV NAMELIST with the name NAM1. The size of an array is limited to the dimensions stated in parentheses beside the variable.

<u>FORTRAN variable</u>	<u>Description</u>												
AO(6)	Initial estimate for the amplitude A_j . There will be one for each peak where AO(1) is the estimate for the peak with the lowest channel number. The remaining are listed in ascending order.												
BO	Initial estimate for the coefficient b of the linear term in the parabola												
CGAMO(6)	Initial estimate for the half-width λ_j . There will be one for each peak, where CGAMO(1) is the estimate for the peak with the lowest channel number. The remaining are listed in ascending order.												
ERROR(21)	Relative error for each parameter used to test for convergence <table border="0" style="margin-left: 20px;"> <tr> <td>ERROR(1)</td><td>relative error for a</td></tr> <tr> <td>ERROR(2)</td><td>relative error for b</td></tr> <tr> <td>ERROR(3)</td><td>relative error for c</td></tr> <tr> <td>ERROR(4)</td><td>relative error for A_1</td></tr> <tr> <td>ERROR(5)</td><td>relative error for P_1</td></tr> <tr> <td>ERROR(6)</td><td>relative error for Γ_1</td></tr> </table>	ERROR(1)	relative error for a	ERROR(2)	relative error for b	ERROR(3)	relative error for c	ERROR(4)	relative error for A_1	ERROR(5)	relative error for P_1	ERROR(6)	relative error for Γ_1
ERROR(1)	relative error for a												
ERROR(2)	relative error for b												
ERROR(3)	relative error for c												
ERROR(4)	relative error for A_1												
ERROR(5)	relative error for P_1												
ERROR(6)	relative error for Γ_1												

<u>FORTRAN variable</u>	<u>Description</u>
ERROR(7)	relative error for A_2
ERROR(8)	relative error for P_2
ERROR(9)	relative error for Γ_2
.	
.	
.	
IERR	Integer used to indicate which error calculation is to be made
IERR	$\begin{cases} = 1 & \text{data are to be used with no error added} \\ = 2 & \text{data are to be used with an error } +\sqrt{y_i} \text{ added} \\ & \text{to every } y_i \\ = 3 & \text{data are to be used with an error } -\sqrt{y_i} \text{ added} \\ & \text{to every } y_i \end{cases}$
IFLAG	Integer used to indicate if new independent and dependent variables will be read in
IFLAG	$\begin{cases} = 1 & \text{x and y values will be read in after the} \\ & \text{NAMELIST data} \\ \neq 1 & \text{no new x and y values will be read in} \end{cases}$
IPRINT	Integer to allow for additional printout
IPRINT	$\begin{cases} = 0 & \text{regular printout} \\ \neq 0 & \text{a table of each x value and its y value,} \\ & \text{computed y value, residual, and value of} \\ & \text{the parabola at that point will be printed} \end{cases}$
NP	Number of peaks
PO(6)	Initial estimate for the peak position p_j . There will be one for each peak where PO(1) is the estimate for the peak with the lowest channel number. The remaining are listed in ascending order.
SAO	Initial estimate for the coefficient a of the second-order term in the equation of the parabola
VELB	Maximum value of source-absorber Doppler velocity

READ statement data.— The following variables are input by using a FORTRAN READ statement. The format used is shown in parentheses beside the variable.

<u>Card</u>	<u>Description</u>	<u>FORTRAN variable</u>	<u>Format</u>
First card	ID Case identification number NO Number of x and y values to be read If NO is positive, the first channel number will be converted to +VELB mm/sec. If NO is negative, the first channel number will be converted to -VELB mm/sec.	ID,NO	(5x,I5,I10)
Remaining cards	X Independent variable, read in as a channel number and converted to mm/sec by the program on a velocity axis of -VELB to +VELB mm/sec Y Dependent variable	X,Y	4(F4.0,F6.0)

Output

An example of the output is shown in appendix C. Headings and interpretations are as follows:

<u>Heading</u>	<u>Description</u>
CASE NO.	Identification number
IERR	Identifies if any error was imposed on data (see input variable IERR)
SA	Coefficient of second-order term in equation of the parabola
B	Coefficient of first-order term in equation of the parabola
C	Constant term in equation of the parabola
NO. OF ITERATIONS	Number of iterations necessary for convergence to desired accuracy
IS	Isomer shift of peak
GAM	Γ
A	Amplitude of peak
P	Position of the peak on the velocity axis
CGAM	λ
AREA	Area between curve and parabola for peak

A number appearing in parentheses after a parameter is the estimate of the error bounds for that parameter.

For a single peak the following are printed:

<u>Heading</u>	<u>Description</u>
PHI1	Ratio of amplitude to y value of parabola at peak
PHI2	Ratio of area between curve and parabola to area under parabola
PHI1/PHI2	Ratio of PHI1 to PHI2

For multiple peaks the following derived parameters are printed:

<u>Heading</u>	<u>Description</u>
IS	Isomer shift of the peak, $\frac{1}{4}(p_1 + p_2 + p_{N-1} + p_N)$
QS	Quadrupole splitting in a complex spectrum, $-\frac{1}{4}(p_1 - p_2 + p_N - p_{N-1})$
GO1	Magnetic hyperfine splitting between lines 3 and 5 in Fe^{57} spectrum, $p_{N-1} - p_3$
GO2	Magnetic hyperfine splitting between lines 2 and 4 in Fe^{57} spectrum, $p_{N-2} - p_2$
G1	Magnetic hyperfine splitting between lines 4 and 5 in Fe^{57} spectrum, $p_{N-3} - p_2$
M1	Ratio of intensity of line 1 and line 2; also called I_1/I_2 in Fe^{57} spectrum, $\frac{ A_1 + A_N }{ A_2 + A_{N-1} }$
M2	$\frac{\text{Area of peak 1} + \text{Area of peak } N}{\text{Area of peak 2} + \text{Area of peak } N - 1}$
PHI	$\frac{\sum (\text{Area of peaks})}{\text{Area under parabola}}$

In each case the area of a peak refers to the area between the curve and the parabola.

The following will be printed in six columns if IPRINT ≠ 0:

<u>Heading</u>	<u>Description</u>
CHANNEL NO.	Channel number
X MM/SEC	x
Y	y
COMPUTED Y	Computed function
RESIDUALS	Residuals
PARABOLA	Value of the parabola
STD	Standard deviation of residuals

Diagnostics

The program will stop execution if either of the following two errors occurs:

1. If the number of iterations for convergence exceeds 30, the baseline parabola will be plotted, and the program will go to the next case.
2. If a division by zero occurs in evaluating the areas, a message is printed, the values of the parameters are printed, and the program will go to the next case.

If either of those conditions occurs, new estimates for the parameters can be tried.

Applications

The program described herein has been applied to investigate changes in two types of stainless steels subjected to longitudinal stress in the range of 0 to 10 kbar. The stress-induced extensions in the steel specimen lead to changes in the electronic environment of the absorber iron atoms. These changes are reflected in the position and the shape of the Mössbauer resonance lines. By systematic measurements of the various Mössbauer parameters in the absorption spectra under different stresses, it was hoped to study the dependence of the observed Mössbauer parameters on the applied stress. Such stress-parameter relationships, if proved to be strong, are expected to be useful in remote stress measurements in steel structures.

A schematic diagram of this experimental setup used in measuring Mössbauer spectra is shown in figure 3. A 2-millicurie Co⁵⁷ source in a platinum matrix provided the 14.4-keV radiation, whose energy was Doppler shifted by changing its velocity. Representative Mössbauer spectra in carbon-rich steel (AISI C1095) and noncorrosive, high-strength, nonmagnetic steel (AISI type 316) under different stresses are shown in figures 4 and 5, respectively. All these spectra were analyzed by using the present

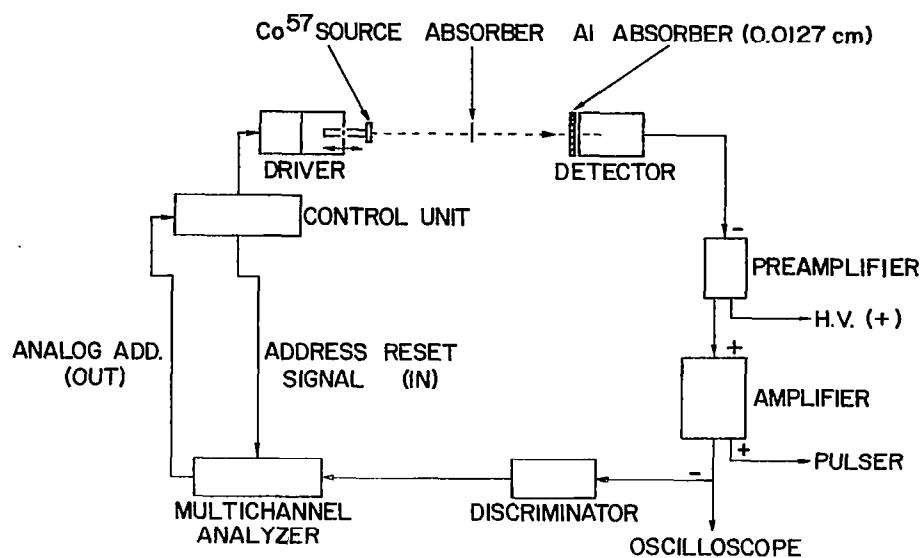


Figure 3.- Schematic diagram of experimental setup for measuring Mössbauer spectra.

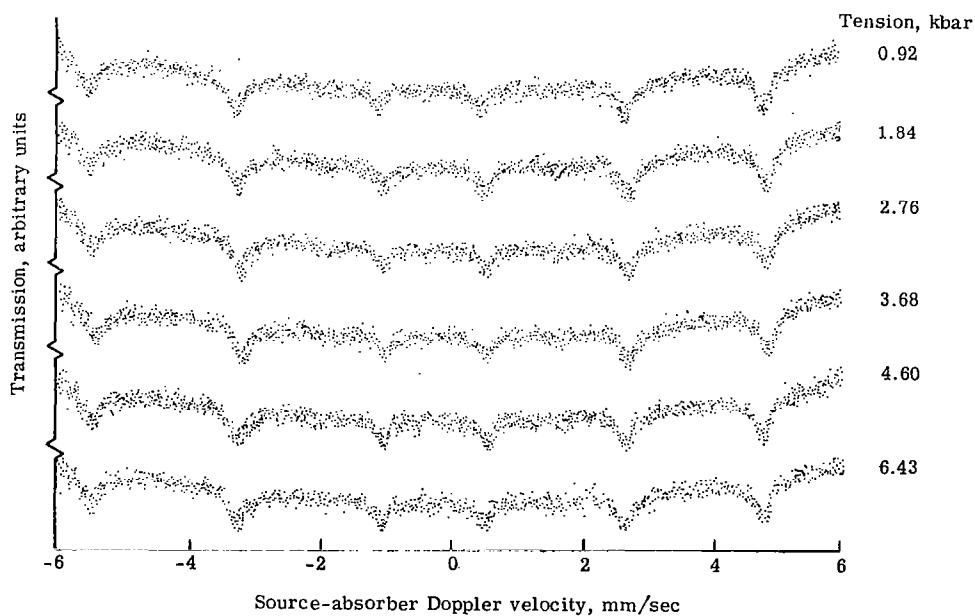


Figure 4.- Mössbauer spectra in carbon-rich steel absorber sample under different tensions. $38\text{-}\mu\text{m}$ -thick AISI C1095 steel.

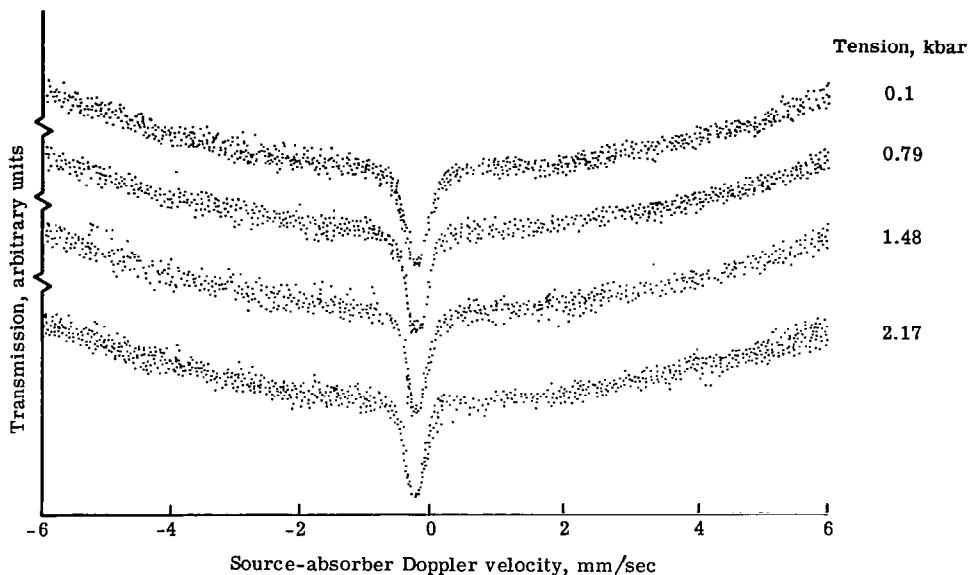


Figure 5.- Mössbauer spectra of stainless steel under different tensions. 25- μm -thick, 5.08-cm-wide type 316 steel.

program, and the values of various parameters (isomer shift, quadropole splitting, $\text{g}\mu\text{H}$, I_1/I_2 , and resonant fraction) were calculated. The parameters are defined in the section entitled "Output," and the results are summarized in table I.

From figures 4 and 5, it is obvious that only a detailed computer analysis can reliably estimate small stress-induced changes in the Mössbauer spectra. A comparison of the present results with similar data reported elsewhere (refs. 9 to 12) and summarized in table I verifies the usefulness of the present program in obtaining reliable estimates of such small changes in the associated Mössbauer parameters. From these data, it may be concluded that I_1/I_2 for carbon-rich steels and the resonant fraction for nickel-chromium steels are the most stress-sensitive parameters. These parameters can serve as the basis of remote uniaxial tension measurements in respective steel structures.

CONCLUDING REMARKS

The least-squares curve-fitting techniques described in this report apply to single-line spectra, single hyperfine spectra, or when the constituent spectra are separated well enough to let the individual absorption peaks stand alone. In most well-tempered structural steels, one usually encounters uniform composition leading to a single hyperfine spectrum or biphasic materials leading to two distinctly separate spectra. If, however, one is concerned with a complex spectrum resulting from the existence of several local

TABLE I.- COMPARISON OF PRESENT RESULTS WITH REPORTED MEASUREMENTS ON PRESSURE DEPENDENCE OF MÖSSBAUER PARAMETERS

Mössbauer parameter ^a	Reference 9	Reference 10	Reference 11	Reference 12	Present results ^b	
					AISI C1095	Type 316
Isomer shift (IS), cm-sec ⁻¹ -kbar ⁻¹	(-7.98 ± 0.31) × 10 ⁻⁵	(1.78 ± 0.56) × 10 ⁻⁴	-8.3 × 10 ⁻⁵	(-7.9 ± 0.8) × 10 ⁻⁵	(-7.19 ± 2.89) × 10 ⁻⁵	(-8.69 ± 5.02) × 10 ⁻⁵
Quadrupole splitting (QS), cm-sec ⁻¹ -kbar ⁻¹	-----	0	<7 × 10 ⁻⁴	(0.96 ± 0.23) × 10 ⁻⁵	(1.06 ± 1.52) × 10 ⁻⁵	-----
gμH (GO1), cm-sec ⁻¹ -kbar ⁻¹	-----	(-1.74 ± 1.91) × 10 ⁻⁵	(-1.69 ± 0.05) × 10 ⁻⁴	(-1.34 ± 0.25) × 10 ⁻⁴	(-7.61 ± 5.03) × 10 ⁻⁵	-----
I ₁ /I ₂ (M1), kbar ⁻¹	-----	-----	Not reported	=0.01 (for 1 to 10 kbar)	(-3.62 ± 1.36) × 10 ⁻²	-----
Resonant fraction (PHI2), kbar ⁻¹	-----	-----	-----	-----	-(5.62 ± 1.98) × 10 ⁻⁵	-(2.59 ± 1.12) × 10 ⁻⁴

^aFORTRAN output heading is given in parentheses after each parameter.^bThe quoted errors on the various coefficients include the effects of individual data point errors.

environments in the absorber iron alloy, the curve-fitting process becomes more complex and will require several trial-and-error solutions based on homogeneous alloy peaks. In that case one should use the procedure of curve fitting of the Mössbauer data by constrained least-squares analysis, as mentioned earlier in this report. The present program has not been adapted for such complex cases.

Langley Research Center,
National Aeronautics and Space Administration,
Hampton, Va., February 22, 1972.

APPENDIX A

THE LEAST-SQUARES SOLUTION

The solution of equation (7) contains $3N + 3$ parameters, which under theoretical conditions are constant. These parameters are a , b , c , A_1 , p_1 , λ_1, \dots, A_N , p_N , and λ_N . A solution of equation (7) can be found with n observations. Associated with y in equation (7) is some measurement error ϵ . Since this error exists, a computational method is needed which yields the best possible results with all the information available. The method of least squares, which is described subsequently, uses a minimum error criterion and has been used in the analysis of these Mössbauer data.

In general, equation (7) with the associated measurement errors can be written as

$$y_i = F(x_i, a, b, c, A_1, p_1, \lambda_1, \dots, A_N, p_N, \lambda_N) + \epsilon_i \quad (A1)$$

where F is a nonlinear function of the parameters, and in order to find an estimate to the parameters of the function, it must be linearized. Expanding equation (7) in a Taylor series about a nominal set of parameters and dropping the higher order terms result in the following linear approximation:

$$\begin{aligned} \Delta y_i &= y_i - y_{i,o} \\ &= b_{i,1}(a - a_o) + b_{i,2}(b - b_o) + b_{i,3}(c - c_o) + b_{i,4}(A_1 - A_{1,o}) \\ &\quad + b_{i,5}(p_1 - p_{1,o}) + b_{i,6}(\lambda_1 - \lambda_{1,o}) + \dots + b_{i,3N+1}(A_N - A_{N,o}) \\ &\quad + b_{i,3N+2}(p_N - p_{N,o}) + b_{i,3N+3}(\lambda_N - \lambda_{N,o}) + \epsilon_i \end{aligned} \quad (A2)$$

APPENDIX A – Continued

where

$$b_{i,1} = \left. \frac{\partial F_i}{\partial a} \right|_0 \quad b_{i,2} = \left. \frac{\partial F_i}{\partial b} \right|_0 \quad b_{i,3} = \left. \frac{\partial F_i}{\partial c} \right|_0$$

$$b_{i,4} = \left. \frac{\partial F_i}{\partial A_1} \right|_0 \quad b_{i,5} = \left. \frac{\partial F_i}{\partial p_1} \right|_0 \quad b_{i,6} = \left. \frac{\partial F_i}{\partial \lambda_1} \right|_0$$

$$\begin{array}{c} \cdot \\ \cdot \\ \cdot \end{array}$$

$$b_{i,3N+1} = \left. \frac{\partial F_i}{\partial A_N} \right|_0 \quad b_{i,3N+2} = \left. \frac{\partial F_i}{\partial p_N} \right|_0 \quad b_{i,3N+3} = \left. \frac{\partial F_i}{\partial \lambda_N} \right|_0$$

If α_j is equal to the $3N + 3$ parameters and

$$\Delta \alpha_1 = a - a_o \quad \Delta \alpha_2 = b - b_o \quad \Delta \alpha_3 = c - c_o$$

$$\Delta \alpha_4 = A_1 - A_{1,o} \quad \Delta \alpha_5 = p_1 - p_{1,o} \quad \Delta \alpha_6 = \lambda_1 - \lambda_{1,o}$$

$$\begin{array}{c} \cdot \\ \cdot \\ \cdot \end{array}$$

$$\Delta \alpha_{3N+1} = A_N - A_{N,o} \quad \Delta \alpha_{3N+2} = p_N - p_{N,o} \quad \Delta \alpha_{3N+3} = \lambda_N - \lambda_{N,o}$$

equation (A2) can be put into the following form:

$$\Delta y_i = \sum_{j=1}^{3N+3} b_{i,j} \Delta \alpha_j + \epsilon_i \quad (i = 1, \dots, n) \quad (A3)$$

For further considerations the linear equation (A3) corresponding to the i th observation is expressed in matrix notation as

APPENDIX A – Continued

$$z_i = B_i \Delta\alpha + e_i \quad (A4)$$

where

$$z_i = \Delta y_i \quad B_i = [b_{i,1}, b_{i,2}, \dots, b_{i,3N+3}]$$

$$\Delta\alpha = \begin{bmatrix} \Delta\alpha_1 \\ \Delta\alpha_2 \\ \vdots \\ \vdots \\ \Delta\alpha_{3N+3} \end{bmatrix} \quad e_i = [e_i]$$

Then for n ($n \geq 3N + 3$) observations, there are n matrix equations of the form of equation (A4) which may be written

$$\bar{z} = \bar{B} \Delta\alpha + \bar{e} \quad (A5)$$

where

$$\bar{z} = \begin{bmatrix} z_1 \\ z_2 \\ \vdots \\ \vdots \\ z_n \end{bmatrix} \quad \bar{B} = \begin{bmatrix} B_1 \\ B_2 \\ \vdots \\ \vdots \\ B_n \end{bmatrix} \quad \bar{e} = \begin{bmatrix} e_1 \\ e_2 \\ \vdots \\ \vdots \\ e_n \end{bmatrix}$$

The problem may be restated: Given \bar{z} and \bar{B} , find the best estimate $\hat{\Delta}\alpha$ for $\Delta\alpha$.

The best estimate $\hat{\Delta}\alpha$ is the value of $\hat{\Delta}\alpha$ which minimizes the sum of the squares of the residuals $\bar{e}^T \bar{e}$ where

APPENDIX A – Continued

$$\bar{e}^T \bar{e} = (\bar{z} - \bar{B} \Delta\alpha)^T (\bar{z} - \bar{B} \Delta\alpha) \quad (A6)$$

In order to minimize equation (A6), the first variation δ with respect to $\Delta\alpha$ must vanish, that is,

$$\left. \begin{aligned} \delta(\bar{e}^T \bar{e}) &= \delta \left[(\bar{z} - \bar{B} \Delta\alpha)^T (\bar{z} - \bar{B} \Delta\alpha) \right] = 0 \\ \delta(\bar{e}^T \bar{e}) &= -2(\bar{z}^T - \Delta\alpha^T \bar{B}^T) \bar{B} \delta \Delta\alpha = 0 \end{aligned} \right\} \quad (A7)$$

Since $\delta \Delta\alpha \neq 0$, equations (A7) can be satisfied if

$$(\bar{z}^T - \Delta\alpha^T \bar{B}^T) \bar{B} = 0$$

or

$$\bar{B}^T \bar{B} \Delta\alpha = \bar{B}^T \bar{z} \quad (A8)$$

Solving for the estimate of $\Delta\alpha$ in equation (A8) gives

$$\hat{\Delta}\alpha = (\bar{B}^T \bar{B})^{-1} \bar{B}^T \bar{z} \quad (A9)$$

A second necessary condition for equation (A6) to be a minimum is that the second variation with respect to $\Delta\alpha$ be positive definite. Upon examination the second variation is

$$\delta^2(\bar{e}^T \bar{e}) = 2\delta \Delta\alpha^T \bar{B}^T \bar{B} \delta \Delta\alpha$$

which is positive definite. Therefore, equation (A9) is a valid expression for $\hat{\Delta}\alpha$.

Since equation (A9) is based on a linear approximation with nominal $\alpha_{j,0}$, $\hat{\Delta}\alpha$ can be used to find the best estimates $\hat{\alpha}_j$. With the relationship $\alpha = \alpha_0 + \Delta\alpha$, the value of $\hat{\Delta}\alpha$ which minimized equation (A6) leads to a new nominal $\alpha_{j,0} = \alpha_{j,0} + \hat{\Delta}\alpha$. This process implies an iterative procedure which continues until $\hat{\Delta}\alpha \rightarrow 0$ and the value of $\alpha_{j,0}$ that leads to this result is the best estimate of $\hat{\alpha}_j$ for α_j .

APPENDIX A – Continued

Error Analysis

Associated with the least-squares solution is the determination of the accuracy of the parameters α . When $\hat{\Delta}\alpha \rightarrow 0$ the best estimate of α is obtained. This estimate is denoted by $\hat{\alpha}^*$ and the associated matrix $\left[\bar{B}^T \bar{B}\right]^{-1*}$ is defined to be the covariance matrix. Multiplying $\left[\bar{B}^T \bar{B}\right]^{-1*}$ by the predicted variance σ^2 , where

$$\sigma^2 = \frac{\bar{e}^T \bar{e}}{(n - k)}$$

yields the covariance matrix V of the estimated parameters (ref. 13),

$$V = \left[\bar{B}^T \bar{B}\right]^{-1*} \sigma^2$$

By examining the diagonal elements of V , estimates of the error in α can be obtained. That is, the square roots of the diagonal elements of V are the estimates of the error bounds of α .

Partial Derivatives

For equation (A1)

$$F = (ax^2 + bx + c) + \sum_{j=1}^N \frac{A_j}{1 + \left(\frac{p_j - x}{\lambda_j}\right)^2}$$

where $\lambda_j = \Gamma_j/2$, the partial derivatives of F with respect to each parameter are as follows:

APPENDIX A – Concluded

$$\frac{\partial F}{\partial a} = x^2$$

$$\frac{\partial F}{\partial b} = x$$

$$\frac{\partial F}{\partial c} = 1$$

$$\left. \begin{aligned} \frac{\partial F}{\partial A_j} &= \frac{\lambda_j^2}{\lambda_j^2 + (p_j - x)^2} \\ \frac{\partial F}{\partial p_j} &= \frac{-2A_j \lambda_j^2 (p_j - x)}{\left[\lambda_j^2 + (p_j - x)^2 \right]^2} \\ \frac{\partial F}{\partial \lambda_j} &= \frac{2A_j \lambda_j (p_j - x)^2}{\left[\lambda_j^2 + (p_j - x)^2 \right]^2} \end{aligned} \right\} \quad (j = 1, 2, \dots, N)$$

APPENDIX B

LANGLEY LIBRARY SUBROUTINE MATINV

Language: FORTRAN

Purpose: MATINV solves the matrix equation $AX = B$, where A is a square coefficient matrix and B is a matrix of constant vectors. The solution to a set of simultaneous equations, the matrix inverse, and the determinant may be obtained. If the user does not want the inverse, use SIMEQ for savings in time and storage. For the determinant only, use DETEV.

Use: CALL MATINV(A,N,B,M,DETERM,IPIVOT,INDEX,NMAX,ISCALE)

A	A two-dimensional array of the coefficients. On return to the calling program, A^{-1} is stored in A
N	The order of A, $1 \leq N \leq NMAX$
B	A two-dimensional array of the constant vectors B. On return to the calling program, X is stored in B
M	The number of column vectors in B. The expression $M = 0$ signals that the subroutine is used solely for inversion; however, in the CALL statement an entry corresponding to B must still be present
DETERM	Gives the value of the determinant by the formula $\text{DET}(A) = (10^{100})\text{ISCALE}(\text{DETERM})$
IPIVOT	A one-dimensional array of temporary storage used by the routine
INDEX	A two-dimensional array of temporary storage used by the routine
NMAX	The maximum order of A as stated in the DIMENSION statement of the calling program
ISCALE	A scale factor computed by the subroutine to keep the results of computation within the floating-point word size of the computer

Restrictions: Arrays A, B, IPIVOT, and INDEX have variable dimensions in the subroutine. The maximum size of these arrays must be specified in a DIMENSION statement of the calling program as A(NMAX,NMAX), B(NMAX,M), IPIVOT(NMAX), and INDEX(NMAX,2). The original matrices A and B are destroyed. They must be saved by the user if there is further need for them. The determinant is set to zero for a singular matrix.

Method: Jordan's method is used to reduce a matrix A to the identity matrix I through a succession of elementary transformations l_n, l_{n-1}, \dots, l_1 . $A = I$. If these transformations are simultaneously applied to I and to a matrix B of constant vectors, the results are A^{-1} and X where $AX = B$. Each transformation is selected so that the largest element is used in the pivotal position. (See ref. (a).)

Accuracy: Total pivotal strategy is used to minimize the rounding errors; however, the accuracy of the final results depends upon how well-conditioned the original matrix is.

Reference: (a) Fox, L.: An Introduction to Numerical Linear Algebra. Oxford Univ. Press, 1965.

Storage: 5428 locations.

Subroutine date: August 1, 1968.

APPENDIX C

SAMPLE CASES

Sample Case 1

Input.-

```

$NAM1 IFLAG=1, IERR=1, IPRINT=1,
NP=1, AO=3000, PO=-.2, CGAMO=-.2, ERROR=6*1.E-6,
SA0=10, BO=3, VELB=6, $
      -993
  2 44664   3 44760   4 447C5   5 44639   6 44812   7 44670   8 44415   9 44142
10 43965   11 44242   12 43662   13 44123   14 44000   15 44170   16 44028   17 44200
18 43714   19 44588   20 44124   21 44495   22 44132   23 44060   24 44266   25 44102
26 44257   27 44392   28 44CC4   29 44161   30 44279   31 44343   32 44000   33 44232
34 44200   35 44200   36 44CCC   37 44000   38 43849   39 43892   40 44050   41 44102
42 43696   43 44155   44 44C15   45 43848   46 43877   47 43863   48 43613   49 43732
50 43839   51 43689   52 44156   53 43941   54 43681   55 43710   56 43726   57 43581
58 44013   59 439E5   60 43662   61 43707   62 43723   63 43978   64 43939   65 43846
66 43982   67 43990   68 43088   69 43800   70 43352   71 43244   72 43629   73 43395
74 44020   75 43671   76 43403   77 43984   78 43617   79 43700   80 43736   81 43721
82 43581   83 43683   84 437C5   85 43340   86 43550   87 43628   88 43459   89 43555
90 43638   91 43101   92 42332   93 43476   94 43333   95 43555   96 43156   97 43007
98 43604   99 43502  100 436C2  101 43163  102 43834  103 43613  104 42965  105 43396
106 43445  107 43301  108 436C7  109 431E9  110 43495  111 43644  112 43093  113 43616
114 43184  115 43715  116 43370  117 43022  118 43318  119 43696  120 43240  121 43220
122 43120  123 433E0  124 43141  125 43174  126 43019  127 43007  128 43212  129 43630
130 43192  131 43105  132 43113  133 43316  134 43066  135 43202  136 43099  137 42993
138 42947  139 43137  140 43275  141 43181  142 43011  143 43298  144 43060  145 42940
146 43129  147 42700  148 42763  149 43257  150 42902  151 43363  152 42978  153 43195
154 42455  155 43149  156 43102  157 42769  158 42857  159 42950  160 43019  161 42830
162 43156  163 42779  164 42354  165 42811  166 43167  167 42530  168 42539  169 42744
170 43168  171 42990  172 42590  173 42751  174 42762  175 42605  176 42604  177 42922
178 42721  179 42615  180 42280  181 42858  182 42657  183 42482  184 42600  185 42522
186 42335  187 42842  188 42631  189 42350  190 42770  191 43037  192 42635  193 42921
194 42463  195 42580  196 42975  197 42643  198 42878  199 42779  200 42637  201 42996
202 42552  203 42779  204 42631  205 42572  206 42527  207 42920  208 42910  209 42609
210 42436  211 42736  212 42694  213 42684  214 42790  215 42192  216 42540  217 42505
218 42525  219 42523  220 42561  221 42164  222 42372  223 42738  224 42804  225 42441
226 42645  227 42218  228 42692  229 42303  230 42540  231 42121  232 42574  233 42407
234 42122  235 42306  236 42637  237 42288  238 42360  239 42549  240 42518  241 42230
242 42183  243 42367  244 42F20  245 42565  246 42246  247 42196  248 42326  249 42173
250 42522  251 42430  252 42192  253 42171  254 42563  255 41864  256 42125  257 42517
258 42268  259 42603  260 42350  261 42316  262 42622  263 42230  264 42087  265 42606
266 42799  267 41920  268 42570  269 42113  270 42040  271 42105  272 42326  273 42086
274 41985  275 41916  276 421C7  277 42168  278 42232  279 42187  280 41995  281 42265
282 41776  283 42156  284 42150  285 42444  286 42476  287 41856  288 41911  289 42143
290 42189  291 42231  292 42410  293 42291  294 42023  295 42128  296 41873  297 42211
298 41994  299 42091  300 42C95  301 41973  302 41662  303 42190  304 42376  305 42101
306 42206  307 42133  308 42CCC0  309 42122  310 41832  311 41825  312 42387  313 42153
314 42178  315 42328  316 42C44  317 41803  318 42082  319 41912  320 42078  321 41959
322 41844  323 41793  324 42135  325 41871  326 42120  327 41712  328 42002  329 41931
330 41668  331 41630  332 42189  333 42040  334 41931  335 41892  336 42245  337 42003
338 42385  339 41726  340 41843  341 41438  342 42271  343 41963  344 41925  345 41787
346 42436  347 42000  348 4192C  349 41883  350 41797  351 41790  352 42125  353 41804

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APPENDIX C – Continued

354 41575 355 41874 356 41614 357 41618 358 42043 359 41803 360 41915 361 41687
 362 41848 363 41845 364 41739 365 41723 366 41862 367 41824 368 41682 369 41962
 370 41884 371 41^o59 372 41618 373 42040 374 42270 375 41716 376 41651 377 41430
 378 41765 379 41662 380 41779 381 41717 382 41857 383 41629 384 41910 385 41468
 386 41645 387 41986 388 42013 389 +1803 390 41825 391 42181 392 41804 393 41944
 394 41935 395 41575 396 42013 397 +1882 398 42094 399 41925 400 41518 401 41545
 402 42087 403 42145 404 41532 405 41952 406 41795 407 41562 408 41930 409 42094
 410 41246 411 41536 412 42256 413 41790 414 42083 415 41758 416 41809 417 42071
 418 41890 419 41523 420 42054 421 42193 422 41894 423 41851 424 41634 425 41669
 426 41599 427 41782 428 41621 429 41905 430 41854 431 42170 432 42032 433 42230
 434 42235 435 41952 436 41591 437 42156 438 41996 439 42014 440 42126 441 41876
 442 41415 443 42185 444 41620 445 +2183 446 41734 447 42030 448 42057 449 42329
 450 41676 451 42292 452 42545 453 42789 454 42601 455 43089 456 42983 457 43112
 458 42936 459 42831 460 43294 461 43275 462 43867 463 44003 464 43966 465 44666
 466 44846 467 44684 468 45054 469 45397 470 45293 471 45495 472 45467 473 46027
 474 45587 475 45670 476 45251 477 45256 478 45700 479 45547 480 45788 481 44800
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 514 41585 515 41660 516 41558 517 41995 518 41494 519 41596 520 41660 521 41940
 522 41592 523 41771 524 41513 525 41697 526 41628 527 41457 528 41624 529 41659
 530 41601 531 41866 532 41530 533 41415 534 41818 535 41718 536 41854 537 41551
 538 41398 539 41566 540 41611 541 41823 542 41490 543 41619 544 41491 545 41825
 546 41726 547 41862 548 41937 549 42207 550 42077 551 41327 552 41764 553 41650
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 578 41402 579 41937 580 41450 581 41564 582 41423 583 41752 584 41932 585 41794
 586 41363 587 41445 588 41911 589 41561 590 41927 591 41505 592 41602 593 41678
 594 41713 595 41600 596 41565 597 41524 598 41527 599 41835 600 41723 601 41897
 602 41729 603 41488 604 41614 605 41883 606 41942 607 41480 608 41720 609 41503
 610 41759 611 41456 612 41570 613 41807 614 41973 615 41415 616 41598 617 41919
 618 41624 619 42149 620 41825 621 41651 622 42063 623 41668 624 41988 625 41577
 626 41737 627 41753 628 41764 c29 41834 630 41939 631 41696 632 41647 633 41770
 634 41738 635 41901 636 41855 637 42163 638 41852 639 42117 640 41853 641 41983
 642 41821 643 41455 644 42069 645 41875 646 41683 647 42032 648 42229 649 41981
 650 41953 651 42034 652 41753 653 41709 654 41668 655 42048 656 42029 657 41398
 658 41876 659 41849 660 41876 661 41931 662 42237 663 41547 664 41770 665 42172
 666 41737 667 41798 668 42060 669 41925 670 42247 671 41680 672 41800 673 41913
 674 42014 675 42116 676 42046 677 42077 678 41700 679 41687 680 42161 681 41741
 682 41828 683 41^o71 684 42050 685 42043 686 42013 687 42000 688 41676 689 41982
 690 42035 691 42115 692 42253 693 41963 694 42081 695 41813 696 41650 697 41715
 698 42066 699 42020 700 42020 701 42086 702 41963 703 42000 704 42396 705 42027
 706 41963 707 42021 708 42157 709 41963 710 41923 711 42290 712 41884 713 42191
 714 42334 715 42235 716 42043 717 42176 718 42257 719 41899 720 41839 721 42131
 722 42056 723 42335 724 42140 725 42114 726 42039 727 42028 728 42234 729 41914
 730 41880 731 42021 732 42267 733 42152 734 41982 735 42130 736 42415 737 42173
 738 41851 739 42303 740 42227 741 42391 742 41740 743 42253 744 42438 745 42068
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 762 42374 763 42171 764 42358 765 42217 766 42567 767 42530 768 42241 769 42021
 770 42488 771 42550 772 42242 773 42480 774 42206 775 42546 776 42325 777 42117
 778 42527 779 42214 780 42758 781 42157 782 42303 783 42412 784 42600 785 42991
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 794 42537 795 42588 796 42516 797 42804 798 42557 799 42418 800 42308 801 42719
 802 42241 803 42805 804 42678 805 42634 806 42511 807 42944 808 42527 809 42924
 810 42644 811 42600 812 42302 813 42760 814 42940 815 42653 816 42816 817 42742
 818 42765 819 42574 820 42155 821 43221 822 42628 823 42664 824 42773 825 42946
 826 43017 827 42669 828 42647 829 42430 830 42822 831 42695 832 43027 833 42810
 834 42723 835 42639 836 43353 837 43016 838 43043 839 42911 840 42445 841 42983
 842 42742 843 42889 844 43058 845 43284 846 42811 847 42866 848 42711 849 43299
 850 43031 851 42856 852 43013 853 42806 854 43129 855 42872 856 42626 857 43070
 858 43127 859 43062 860 43305 861 43349 862 42^o73 863 43225 864 42751 865 42509

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866 43158 867 43162 668 43137 869 43130 870 42966 871 43140 872 42953 873 42837
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882 43140 883 43316 884 43318 885 43387 886 42693 887 43390 888 43325 889 43571
890 43231 891 42951 892 42350 893 42984 894 43373 895 43419 896 43159 897 43262
898 43729 899 42918 900 43050 901 43371 902 43452 903 43443 904 43809 905 43328
906 43754 907 43371 908 42524 909 43051 910 43329 911 43334 912 43472 913 43581
914 43144 915 43754 916 43325 917 43643 918 43612 919 43570 920 43186 921 43544
922 43500 923 43465 924 43561 925 43501 926 43429 927 43493 928 43868 929 44069
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938 43753 939 43618 940 43813 941 43863 942 44009 943 43675 944 43715 945 44103
946 44185 947 43914 948 44227 949 43625 950 44007 951 43802 952 43559 953 44041
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962 44111 963 43863 964 44237 965 44092 966 43772 967 44038 968 44290 969 43913
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978 44195 979 44080 980 44356 981 44227 982 43937 983 44262 984 44063 985 43911
986 44244 987 44343 988 44411 989 44359 990 44601 991 44223 992 44338 993 44365
994 44462
$NAM1
  IFLAG=0,
  IPRINT=0,
  IERR=2,
  $
$NAM1
  IERR=3,
  $

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Output with tables printed.- The computer values given below do not include the velocity calibration correction factor of 1.274. Figure 6 is included as a sample computer plot.

```

CASE NO.    1      IERR= 1

COEFFICIENTS OF PARABOLA   Y= SA*X**2 + BX + C
SA= 7.87263350E+01(±6.815E-01)      B=-8.05921646E+00(±1.926E+00)      C= 4.15600451E+04(±1.187E+01)

NO. OF ITERATIONS= 9

PARAMETERS FOR PEAK 1

IS=-2.82731447E-01      GAM= 2.90415888E-01

A= 4.32422708E+03(±6.853E+01)      P=-2.82731447E-01(±2.300E-03)      CGAM= 1.45207944E-01(±3.545E-03)      AREA= 1.94218988E+03

PHI1= 1.04026244E-01      PHI2= 3.80778889E-03      PHI1/PHI2= 2.73193308E+01

CHANNEL NO. X MM/SEC          Y          COMPUTED Y          RESIDUALS          PARABOLA
  1  -6.00000000E+00  4.46640000E+04  4.44453360E+04  2.18663971E+02  4.44425484E+04
  2  -5.98790323E+00  4.47600000E+04  4.44338339E+04  3.26166131E+02  4.44310344E+04
  3  -5.97580645E+00  4.47050000E+04  4.44223548E+04  2.82645176E+02  4.44195435E+04
  4  -5.96370968E+00  4.46390000E+04  4.44108989E+04  2.28101104E+02  4.44080756E+04
  5  -5.95161290E+00  4.48120000E+04  4.43994661E+04  4.12533916E+02  4.43966307E+04
  6  -5.93951613E+00  4.46700000E+04  4.43880564E+04  2.81943610E+02  4.43852089E+04
  7  -5.92741935E+00  4.44150000E+04  4.43766698E+04  3.83301849E+01  4.43738101E+04
  8  -5.91532258E+00  4.41420000E+04  4.43653064E+04  -2.23306359E+02  4.43624344E+04
  9  -5.90322581E+00  4.39650000E+04  4.43539660E+04  -3.88966022E+02  4.43510817E+04
  10  -5.89112903E+00  4.42420000E+04  4.43426488E+04  -1.00648806E+02  4.43397520E+04
  11  -5.87903226E+00  4.36620000E+04  4.43313547E+04  -6.69354711E+02  4.43284454E+04
  12  -5.86693548E+00  4.41230000E+04  4.43200837E+04  -1.97083738E+02  4.43171618E+04
  13  -5.85483871E+00  4.40000000E+04  4.43088659E+04  -3.08835887E+02  4.43059012E+04
  14  -5.84274194E+00  4.41700000E+04  4.429761112E+04  -1.27611159E+02  4.42946637E+04

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APPENDIX C – Continued

15	-5.83064516E+00	4.40280000E+04	4.42864096E+04	-2.58409555E+02	4.42834493E+04
16	-5.81854839E+00	4.42000000E+04	4.42752311E+04	-7.52310764E+01	4.42722579E+04
17	-5.80645161E+00	4.37140000E+04	4.42640757E+04	-5.50075723E+02	4.42610895E+04
18	-5.79435484E+00	4.45880000E+04	4.42529435E+04	3.35056505E+02	4.42499441E+04
19	-5.78225806E+00	4.41240000E+04	4.42418344E+04	-1.17834395E+02	4.42388218E+04
20	-5.77016129E+00	4.44950000E+04	4.42307484E+04	2.64251578E+02	4.42277226E+04
21	-5.75806452E+00	4.41320000E+04	4.42196856E+04	-8.76855775E+01	4.42166464E+04
22	-5.74596774E+00	4.40600000E+04	4.42086459E+04	-1.48645862E+02	4.42055932E+04
23	-5.73387097E+00	4.42660000E+04	4.41976293E+04	6.83707229E+01	4.41946530E+04
24	-5.72177419E+00	4.41020000E+04	4.41866358E+04	-8.46358226E+01	4.41835559E+04
25	-5.70967742E+00	4.42570000E+04	4.41756655E+04	8.13345002E+01	4.41725719E+04
26	-5.69758065E+00	4.43920000E+04	4.41647183E+04	2.27281691E+02	4.41616109E+04
27	-5.68548387E+00	4.40040000E+04	4.41537943E+04	-1.49794252E+02	4.41506729E+04
28	-5.67338710E+00	4.41610000E+04	4.4128933E+04	1.81066707E+01	4.41397579E+04
29	-5.66129032E+00	4.42790000E+04	4.41320155E+04	1.46984459E+02	4.41288660E+04
30	-5.64919355E+00	4.43430000E+04	4.41211609E+04	2.21839111E+02	4.41179972E+04
31	-5.63709677E+00	4.40000000E+04	4.41103294E+04	-1.10329373E+02	4.41071514E+04
32	-5.62500000E+00	4.42320000E+04	4.40995210E+04	1.32479005E+02	4.40963286E+04
33	-5.61290323E+00	4.42000000E+04	4.40887358E+04	1.11264245E+02	4.40855289E+04
34	-5.60806465E+00	4.42000000E+04	4.40779737E+04	1.22026345E+02	4.40747522E+04
35	-5.58870568E+00	4.40000000E+04	4.40672347E+04	-6.72346945E+01	4.40639985E+04
36	-5.57661290E+00	4.40000000E+04	4.40565189E+04	-5.65188753E+01	4.40522679E+04
37	-5.56451613E+00	4.38490000E+04	4.40458262E+04	-1.96826198E+02	4.40425603E+04
38	-5.55241935E+00	4.38920000E+04	4.40351567E+04	-1.43156664E+02	4.40318758E+04
39	-5.54032258E+00	4.40500000E+04	4.40245103E+04	2.54897264E+01	4.40212143E+04
40	-5.52822581E+00	4.41020000E+04	4.40138870E+04	8.81129718E+01	4.40105758E+04
41	-5.51612903E+00	4.36960000E+04	4.40032869E+04	-3.07286929E+02	4.3999604E+04
42	-5.50403226E+00	4.41550000E+04	4.39927100E+04	1.62290024E+02	4.39893681E+04
43	-5.49193548E+00	4.40150000E+04	4.39821562E+04	3.28438292E+01	4.39787987E+04
44	-5.47983671E+00	4.38480000E+04	4.39716255E+04	-1.23625515E+02	4.39682524E+04
45	-5.46774194E+00	4.38770000E+04	4.39611180E+04	-8.41180081E+01	4.39577292E+04
46	-5.45564516E+00	4.38630000E+04	4.39506337E+04	-8.76336525E+01	4.39472290F+04
47	-5.44354839E+00	4.36130000E+04	4.39401724E+04	-3.27172449E+02	4.39367519E+04
48	-5.43145161E+00	4.37320000E+04	4.39297344E+04	-1.97734398E+02	4.39262977E+04
49	-5.41935484E+00	4.38390000E+04	4.39193195E+04	-8.03195011E+01	4.39158666E+04
50	-5.40725806E+00	4.36890000E+04	4.39089278E+04	-2.1927759E+02	4.39054585E+04
51	-5.39516129E+00	4.41560000E+04	4.38985592E+04	2.57440826E+02	4.38950735E+04
52	-5.38036452E+00	4.39410000E+04	4.38882137E+04	5.27862548E+01	4.38847116E+04
53	-5.37096774E+00	4.36810000E+04	4.38778915E+04	-1.96891475E+02	4.38743726E+04
54	-5.35887097E+00	4.37100000E+04	4.38675924E+04	-1.57592364E+02	4.38640567E+04
55	-5.34677419E+00	4.37260000E+04	4.38751714E+04	-1.31316414E+02	4.38537619E+04
56	-5.33467742E+00	4.35310000E+04	4.38470636E+04	-2.66063626E+02	4.38434941E+04
57	-5.32258065E+00	4.40130000E+04	4.38368340E+04	1.76165999E+02	4.38332473E+04
58	-5.31048387E+00	4.39850000E+04	4.38266275E+04	1.58372461E+02	4.38230236E+04
59	-5.29838710E+00	4.36620000E+04	4.38164442E+04	-1.54444243E+02	4.38128229E+04
60	-5.28629032E+00	4.37070000E+04	4.38062841E+04	-9.92841139E+01	4.38026453E+04
61	-5.27419355E+00	4.37230000E+04	4.37961472E+04	-7.31471521E+01	4.37924906E+04
62	-5.26209677E+00	4.39780000E+04	4.37860334E+04	1.91966641E+02	4.37823591E+04
63	-5.25000000E+00	4.39390000E+04	4.37759427E+04	1.63057263E+02	4.37722506E+04
64	-5.23790323E+00	4.38460000E+04	4.37658753E+04	8.01247144E+01	4.37621651F+04
65	-5.22580645E+00	4.39820000E+04	4.37558310E+04	2.26168993E+02	4.37521026E+04
66	-5.21370968E+00	4.35900000E+04	4.37458099E+04	2.44190097E+02	4.37420632E+04
67	-5.20161290E+00	4.36880000E+04	4.37358120E+04	-4.78119739E+01	4.37320469F+04
68	-5.18951613E+00	4.38000000E+04	4.37258372E+04	7.41627783E+01	4.37220535E+04
69	-5.17741935E+00	4.33520000E+04	4.37158856E+04	-3.63885648E+02	4.37120833E+04
70	-5.16532258E+00	4.32440000E+04	4.37059573E+04	-6.1957253E+02	4.37021360F+04
71	-5.15322581E+00	4.36290000E+04	4.36960520E+04	-6.70520388E+01	4.36922118F+04
72	-5.14112903E+00	4.33950000E+04	4.36861700E+04	-2.91170007E+02	4.36823106E+04
73	-5.12903226E+00	4.40200000E+04	4.36763112E+04	3.43688841E+02	4.36724325E+04
74	-5.11693548E+00	4.36710000E+04	4.36664755E+04	4.52450420E+00	4.36625774E+04
75	-5.10483871E+00	4.34090000E+04	4.36566630E+04	-2.47663019E+02	4.36527454E+04
76	-5.09274194E+00	4.35840000E+04	4.36468737E+04	3.37126269E+02	4.36429364E+04
77	-5.08064516E+00	4.36170000E+04	4.36371076E+04	-2.01076314E+01	4.36331504E+04
78	-5.06854839E+00	4.37000000E+04	4.36273647E+04	7.26352768E+01	4.36233875E+04

79	-5.05645161E+00	4.37360000E+04	4.36176450E+04	1.18354993E+02	4.36136476E+04
80	-5.04435484E+00	4.37210000E+04	4.36079485E+04	1.13051514E+02	4.36039308E+04
81	-5.03225806E+00	4.35810000E+04	4.35982752E+04	-1.72751597E+01	4.35942370E+04
82	-5.02016129E+00	4.36830000E+04	4.35886250E+04	9.43749692E+01	4.35845662E+04
83	-5.00806452E+00	4.37050000E+04	4.35789981E+04	1.26001895E+02	4.35749185E+04
84	-4.99596774E+00	4.33400000E+04	4.35693944E+04	-2.29394371E+02	4.35652939E+04
85	-4.98387097E+00	4.35500000E+04	4.35598138E+04	-9.81384336E+00	4.35556922E+04
86	-4.97177419E+00	4.36280000E+04	4.35502565E+04	7.77434805E+01	4.35461136E+04
87	-4.9567742E+00	4.34590000E+04	4.35407224E+04	-8.17224010E+01	4.35365581E+04
88	-4.94758065E+00	4.35550000E+04	4.35312115E+04	2.37885103E+01	4.35270255E+04
89	-4.93548387E+00	4.36380000E+04	4.35217238E+04	1.16276213E+02	4.35175161E+04
90	-4.92338710E+00	4.31010000E+04	4.35122593E+04	-4.11259255E+02	4.35080296E+04
91	-4.91129032E+00	4.33320000E+04	4.35028180E+04	-1.70818016E+02	4.34985662E+04
92	-4.89919355E+00	4.34760000E+04	4.34934000E+04	-1.73999507E+01	4.34891259E+04
93	-4.88709677E+00	4.33330000E+04	4.34840051E+04	-1.51005101E+02	4.34797086E+04
94	-4.87500000E+00	4.35550000E+04	4.34746335E+04	8.03665259E+01	4.34703143E+04
95	-4.86290323E+00	4.31560000E+04	4.34652851E+04	-3.09285059E+02	4.34609431E+04
96	-4.85080645E+00	4.30070000E+04	4.34559599E+04	-4.48959869E+02	4.34515949E+04
97	-4.83870956E+00	4.36040000E+04	4.34466579E+04	1.57342098E+02	4.34422697E+04
98	-4.82661290E+00	4.35020000E+04	4.34373792E+04	6.46208384E+01	4.34329676E+04
99	-4.81451613E+00	4.36020000E+04	4.34281236E+04	1.73876352E+02	4.34236885E+04
100	-4.80241935E+00	4.31630000E+04	4.34188914E+04	-2.55891365E+02	4.34144325E+04
101	-4.79032258E+00	4.38340000E+04	4.34096823E+04	4.24317688E+02	4.34051095E+04
102	-4.77822581E+00	4.36130000E+04	4.34004965E+04	2.12503506E+02	4.33955806E+04
103	-4.76612903E+00	4.29650000E+04	4.33913339E+04	-4.26333911E+02	4.33868026E+04
104	-4.75403226E+00	4.33960000E+04	4.33821946E+04	1.38054344E+01	4.33776388E+04
105	-4.74193548E+00	4.34450000E+04	4.33730785E+04	7.19215396E+01	4.33684979E+04
106	-4.72483871E+00	4.33010000E+04	4.33639856E+04	-6.29855973E+01	4.33593802E+04
107	-4.71774194E+00	4.36070000E+04	4.32549160E+04	2.52084021E+02	4.33502854E+04
108	-4.70564516E+00	4.31990000E+04	4.33458696E+04	-1.46869606E+02	4.33412137E+04
109	-4.69354839E+00	4.34350000E+04	4.33368465E+04	1.58153517E+02	4.3321650F+04
110	-4.68145161E+00	4.36440000E+04	4.32784666E+04	3.16153390E+02	4.32231394E+04
111	-4.66935484E+00	4.30390000E+04	4.33188700E+04	-2.25869992E+02	4.33141368E+04
112	-4.65725806E+00	4.36160000E+04	4.33099166E+04	3.06083372E+02	4.32051573E+04
113	-4.64516129E+00	4.31840000E+04	4.33009865E+04	-1.16986523E+02	4.32962008E+04
114	-4.63306452E+00	4.37180000E+04	4.32920797E+04	4.25920321E+02	4.32872673E+04
115	-4.62096774E+00	4.33700000E+04	4.32831961E+04	8.68039024E+01	4.32783569E+04
116	-4.60887097E+00	4.30220000E+04	4.32743358E+04	-2.52335782E+02	4.32694695E+04
117	-4.59677419E+00	4.33180000E+04	4.32654987E+04	5.25012661E+01	4.32606051E+04
118	-4.58467742E+00	4.36960000E+04	4.32566850E+04	4.39315043E+02	4.32517638E+04
119	-4.57258065E+00	4.32400000E+04	4.32478945E+04	-7.89445272E+00	4.32429456E+04
120	-4.56048387E+00	4.32200000E+04	4.32391272E+04	-1.91272246E+01	4.32341503E+04
121	-4.54838710E+00	4.31200000E+04	4.32303833E+04	-1.10383275E+02	4.32253782E+04
122	-4.53629032E+00	4.33800000E+04	4.32216626E+04	1.58337394E+02	4.32166290E+04
123	-4.52419355E+00	4.31410000E+04	4.32129652E+04	-7.19652270E+01	4.32C79029E+04
124	-4.51209677E+00	4.31740000E+04	4.32042911E+04	-3.02911243E+01	4.31991998E+04
125	-4.50000000E+00	4.30190000E+04	4.31956403E+04	-1.76640316E+02	4.31905198E+04
126	-4.48790323E+00	4.36070000E+04	4.31870128E+04	-1.80012800E+02	4.31818628E+04
127	-4.47580645E+00	4.32120000E+04	4.31784086E+04	3.35914199E+01	4.31732289E+04
128	-4.46370968E+00	4.36300000E+04	4.31698277E+04	4.60172342E+02	4.31646180E+04
129	-4.45161290E+00	4.31920000E+04	4.31612700E+04	3.07299627E+01	4.31560301E+04
130	-4.43951613E+00	4.31080000E+04	4.31527357E+04	-4.47357208E+01	4.31474653E+04
131	-4.42741935E+00	4.31130000E+04	4.31442247E+04	-3.12247118E+01	4.31289235E+04
132	-4.41532258E+00	4.33160000E+04	4.31357370E+04	1.80262987E+02	4.31304048E+04
133	-4.40322581E+00	4.30660000E+04	4.31272726E+04	-6.12726284E+01	4.31219091E+04
134	-4.39112903E+00	4.32020000E+04	4.31188316E+04	8.31684395E+01	4.31134364E+04
135	-4.37903226E+00	4.30990000E+04	4.31104138E+04	-1.14138128E+01	4.31049868E+04
136	-4.36693548E+00	4.29930000E+04	4.31020194E+04	-1.09019389E+02	4.30965602E+04
137	-4.35483871E+00	4.25470000E+04	4.30936483E+04	-1.46648291E+02	4.30881567E+04
138	-4.34274194E+00	4.31370000E+04	4.30853005E+04	5.16994759E+01	4.3C797762E+04
139	-4.33064516E+00	4.32750000E+04	4.30769761E+04	1.98023909E+02	4.30714187E+04
140	-4.31854839E+00	4.31810000E+04	4.30686750E+04	1.12325005E+02	4.30630843E+04
141	-4.30645161E+00	4.30110000E+04	4.30603972E+04	-4.93972303E+01	4.30547729E+04

APPENDIX C – Continued

142	-4.29435484E+00	4.32980000E+04	4.30521428E+04	2.45857172E+02	4.30464846E+04
143	-4.28225806E+00	4.30600000E+04	4.30439118E+04	1.60882343E+01	4.30382193E+04
144	-4.27016129E+00	4.29400000E+04	4.30357041E+04	-9.57040548E+01	4.30299770E+04
145	-4.25806452E+00	4.31290000E+04	4.30275197E+04	1.01480300E+02	4.30217578E+04
146	-4.24596774E+00	4.27000000E+04	4.30193587E+04	-3.19358704E+02	4.30135617E+04
147	-4.23387097E+00	4.27610000E+04	4.30112211E+04	-2.50221071E+02	4.30053885E+04
148	-4.22177419E+00	4.32570000E+04	4.30031068E+04	2.53893194E+02	4.29972384E+04
149	-4.20967742E+00	4.29020000E+04	4.29950159E+04	-9.30159126E+01	4.29891114E+04
150	-4.19758065E+00	4.33630000E+04	4.29869484E+04	3.76051606E+02	4.29810074E+04
151	-4.18548387E+00	4.29780000E+04	4.29789043E+04	-9.04255845E-01	4.29729264E+04
152	-4.17338710E+00	4.31950000E+04	4.29708835E+04	2.24116499E+02	4.29648685E+04
153	-4.16129032E+00	4.24550000E+04	4.29628861E+04	-5.07886134E+02	4.29568336E+04
154	-4.14919355E+00	4.31490000E+04	4.29549122E+04	1.94087840E+02	4.29488217E+04
155	-4.13709677E+00	4.31020000E+04	4.29469616E+04	1.55038417E+02	4.29408329E+04
156	-4.12500000E+00	4.27690000E+04	4.29390344E+04	-1.70034407E+02	4.29328671E+04
157	-4.11290323E+00	4.26570000E+04	4.29311306E+04	-7.41306371E+01	4.29249244E+04
158	-4.10080645E+00	4.29500000E+04	4.29232503E+04	2.67497224E+01	4.29170047E+04
159	-4.08870968E+00	4.30190000E+04	4.29153933E+04	1.03606667E+02	4.29091080E+04
160	-4.07661290E+00	4.28300000E+04	4.29075598E+04	-7.75598093E+01	4.29012344E+04
161	-4.06451613E+00	4.31560000E+04	4.28997497E+04	2.56250290E+02	4.28933839E+04
162	-4.05241935E+00	4.27790000E+04	4.28919630E+04	-1.12963041E+02	4.28855563E+04
163	-4.04032258E+00	4.23540000E+04	4.28841998E+04	-5.30199806E+02	4.28777518E+04
164	-4.02822581E+00	4.28110000E+04	4.28764600E+04	-6.54600113E+01	4.28699704E+04
165	-4.01612903E+00	4.31670000E+04	4.28687437E+04	2.98256338E+02	4.28622120E+04
166	-4.00403226E+00	4.25300000E+04	4.28610508E+04	-3.31050762E+02	4.28547666E+04
167	-3.99193548E+00	4.25390000E+04	4.28533813E+04	-3.14381319E+02	4.28467643E+04
168	-3.97983871E+00	4.27440000E+04	4.28545735E+04	-1.01735336E+02	4.28390750E+04
169	-3.96771494E+00	4.31680000E+04	4.28381128E+04	3.29887179E+02	4.28314088E+04
170	-3.95564516E+00	4.29900000E+04	4.28305138E+04	1.59486223E+02	4.28237656E+04
171	-3.94354839E+00	4.25900000E+04	4.28229382E+04	-2.32938212E+02	4.28161454E+04
172	-3.93145161E+00	4.21510000E+04	4.28153861E+04	-6.43861298E+01	4.28085483E+04
173	-3.91935484E+00	4.27620000E+04	4.28078575E+04	-4.58575377E+01	4.28009742E+04
174	-3.90725806E+00	4.26050000E+04	4.28003524E+04	-1.95352441E+02	4.27934231E+04
175	-3.89516129E+00	4.26040000E+04	4.27928708E+04	-1.88870846E+02	4.27858951E+04
176	-3.88306452E+00	4.29220000E+04	4.27854128E+04	1.36587240E+02	4.27783902E+04
177	-3.87096774E+00	4.27210000E+04	4.27779782E+04	-5.69781870E+01	4.27709082E+04
178	-3.85887097E+00	4.26150000E+04	4.27705671E+04	-1.55567135E+02	4.27634493E+04
179	-3.84677419E+00	4.22800000E+04	4.27631796E+04	-4.81379610E+02	4.27560135E+04
180	-3.83467742E+00	4.28580000E+04	4.27558156E+04	1.02184381E+02	4.27486007E+04
181	-3.82258065E+00	4.26570000E+04	4.27484752E+04	-9.14751687E+01	4.27412109E+04
182	-3.81048387E+00	4.24820000E+04	4.27411583E+04	-2.59158266E+02	4.27338442E+04
183	-3.79838710E+00	4.26000000E+04	4.27338649E+04	-1.33864917E+02	4.27265005E+04
184	-3.78629032E+00	4.25220000E+04	4.27265951E+04	-2.04595129E+02	4.27191759E+04
185	-3.77419355E+00	4.23350000E+04	4.27193489E+04	-3.84348911E+02	4.27118823E+04
186	-3.76209677E+00	4.28430000E+04	4.27121263E+04	1.30873732E+02	4.27046077E+04
187	-3.75000000E+00	4.26310000E+04	4.27049272E+04	-7.39272084E+01	4.26973556E+04
188	-3.73790323E+00	4.23300000E+04	4.26977517E+04	-3.67751740E+02	4.26901277E+04
189	-3.725806452E+00	4.27700000E+04	4.26905999E+04	7.94001294E+01	4.26829223E+04
190	-3.71370968E+00	4.30370000E+04	4.26834716E+04	3.53528392E+02	4.26757399E+04
191	-3.70161290E+00	4.26350000E+04	4.26763670E+04	-4.13669594E+01	4.26685805E+04
192	-3.68951613E+00	4.29210000E+04	4.26692859E+04	2.517130466E+02	4.26614442E+04
193	-3.67741935E+00	4.24630000E+04	4.26622285E+04	-1.99228540E+02	4.26543309E+04
194	-3.66532258E+00	4.25800000E+04	4.26551948E+04	-7.51947846E+01	4.26472407E+04
195	-3.65322581E+00	4.29750000E+04	4.26481847E+04	3.26815322E+02	4.26401735E+04
196	-3.64112593E+00	4.26430000E+04	4.26611982E+04	1.80177211E+00	4.26331293E+04
197	-3.62903226E+00	4.28780000E+04	4.26342354E+04	2.43764556E+02	4.26261082E+04
198	-3.61693548E+00	4.27790000E+04	4.26272963E+04	1.51703666E+02	4.26191101E+04
199	-3.60483871E+00	4.26370000E+04	4.26203809E+04	1.66190910E+01	4.26121351E+04
200	-3.59274194E+00	4.29960000E+04	4.26134892E+04	3.82510823E+02	4.26051831E+04
201	-3.58064516E+00	4.25520000E+04	4.26066211E+04	-5.46211483E+02	4.25982542E+04
202	-3.56854839E+00	4.27790000E+04	4.25997768E+04	1.79223168E+02	4.25913482E+04
203	-3.55645161E+00	4.26310000E+04	4.25929562E+04	3.80437613E+01	4.25844654E+04
204	-3.54435484E+00	4.25720000E+04	4.25861594E+04	-1.41593781E+01	4.25776055E+04
205	-3.53225806E+00	4.25270000E+04	4.25793863E+04	-5.23862605E+01	4.25707687E+04

206	-3.52016129E+00	4.29200000E+04	4.25726369E+04	3.47363103E+02	4.25639550E+04
207	-3.50806452E+00	4.29100000E+04	4.25659113E+04	3.44088703E+02	4.25571643E+04
208	-3.49596774E+00	4.26090000E+04	4.25592095E+04	4.97905278E+01	4.25503966E+04
209	-3.48387097E+00	4.24360000E+04	4.25525314E+04	-1.16531434E+02	4.25436520E+04
210	-3.47177419E+00	4.27360000E+04	4.25458772E+04	1.90122807E+02	4.25369304E+04
211	-3.45967742E+00	4.26940000E+04	4.25392468E+04	1.54753239E+02	4.25302318E+04
212	-3.44758065E+00	4.26840000E+04	4.25326402E+04	1.51359850E+02	4.25235563E+04
213	-3.43548387E+00	4.27900000E+04	4.25260574E+04	2.63942628E+02	4.25169038E+04
214	-3.42338710E+00	4.21920000E+04	4.25194984E+04	-3.27498439E+02	4.25102744E+04
215	-3.41129032E+00	4.25400000E+04	4.25129634E+04	2.70366374E+01	4.25036680E+04
216	-3.39919355E+00	4.25050000E+04	4.25064522E+04	-1.45215661E+00	4.24970847E+04
217	-3.38709677E+00	4.25250000E+04	4.24999648E+04	2.50351665E+01	4.24905243E+04
218	-3.37500000E+00	4.25230000E+04	4.24935014E+04	2.94985935E+01	4.24839871E+04
219	-3.36290323E+00	4.25610000E+04	4.24870619E+04	7.39381110E+01	4.24774728E+04
220	-3.35080645E+00	4.21640000E+04	4.24806463E+04	-3.16646295E+02	4.24709817E+04
221	-3.33870968E+00	4.23720000E+04	4.24742546E+04	-1.02254638E+02	4.24645135E+04
222	-3.32661290E+00	4.27380000E+04	4.24678869E+04	2.70113068E+02	4.24580684E+04
223	-3.31451613E+00	4.28040000E+04	4.24615432E+04	3.42456808E+02	4.24516463E+04
224	-3.30241935E+00	4.24410000E+04	4.24552234E+04	-1.42234326E+01	4.24452473E+04
225	-3.29032258E+00	4.26450000E+04	4.24489277E+04	1.96072331E+02	4.24388713E+04
226	-3.27822581E+00	4.22180000E+04	4.24426559E+04	-2.24655917E+02	4.24325184E+04
227	-3.26612903E+00	4.26920000E+04	4.24364082E+04	2.55591808E+02	4.24261885E+04
228	-3.25403226E+00	4.23030000E+04	4.24301845E+04	-1.27184509E+02	4.24198816E+04
229	-3.24193548E+00	4.25400000E+04	4.24239849E+04	1.16015114E+02	4.24135978E+04
230	-3.22983871E+00	4.21210000E+04	4.24178093E+04	-2.96809339E+02	4.24073370E+04
231	-3.21774194E+00	4.25740000E+04	4.24116579E+04	1.62342115E+02	4.24010992E+04
232	-3.20564516E+00	4.24070000E+04	4.24055305E+04	1.46945880E+00	4.23948845E+04
233	-3.19354839E+00	4.21220000E+04	4.23994273E+04	-2.77427326E+02	4.23886929E+04
234	-3.18145161E+00	4.23060000E+04	4.23933483E+04	-8.73482566E+01	4.23825242E+04
235	-3.16935484E+00	4.26370000E+04	4.23872934E+04	2.49706648E+02	4.23763787E+04
236	-3.15725806E+00	4.22880000E+04	4.23812626E+04	-9.32626315E+01	4.23702561E+04
237	-3.14516129E+00	4.23600000E+04	4.23752561E+04	-1.52561138E+01	4.23641566E+04
238	-3.13306452E+00	4.25490000E+04	4.23692738E+04	1.79726181E+02	4.23580802E+04
239	-3.12096774E+00	4.25180000E+04	4.23633158E+04	1.54684233E+02	4.23520267E+04
240	-3.10887097E+00	4.22300000E+04	4.23573820E+04	-1.27381978E+02	4.23459963E+04
241	-3.09677419E+00	4.21830000E+04	4.23514725E+04	-1.68472473E+02	4.23399890E+04
242	-3.08467742E+00	4.23670000E+04	4.23455873E+04	2.14127260E+01	4.23340047E+04
243	-3.07258065E+00	4.25200000E+04	4.23397264E+04	1.80273597E+02	4.23280434E+04
244	-3.06048387E+00	4.25650000E+04	4.23338899E+04	2.31110119E+02	4.23221052E+04
245	-3.04838710E+00	4.22460000E+04	4.23280777E+04	-8.20777331E+01	4.23161900E+04
246	-3.03629032E+00	4.21960000E+04	4.23222990E+04	-1.26289981E+02	4.23102979E+04
247	-3.02419355E+00	4.23260000F+04	4.23165266E+04	9.47335126E+00	4.23044288E+04
248	-3.01209677E+00	4.21730000E+04	4.23107878E+04	-1.37787761E+02	4.22985827E+04
249	-3.00000000E+00	4.25220000E+04	4.23050733E+04	2.16926657E+02	4.22927597E+04
250	-2.98790323E+00	4.24300000E+04	4.22993834E+04	1.30616580E+02	4.22869597E+04
251	-2.97580645E+00	4.21920000E+04	4.22937180E+04	-1.01718017E+02	4.22811828E+04
252	-2.96370568E+00	4.21710000E+04	4.22880772E+04	-1.17077163E+02	4.22754289E+04
253	-2.95161290E+00	4.25630000E+04	4.22824609E+04	2.80539117E+02	4.22696981F+04
254	-2.93951613E+00	4.18640000E+04	4.22768692E+04	-4.12869206E+02	4.22639902E+04
255	-2.92741935E+00	4.21250000E+04	4.22713022E+04	-1.46302160E+02	4.22583055E+04
256	-2.91532258E+00	4.25170000E+04	4.22657598E+04	2.51240225E+02	4.22526437E+04
257	-2.90322581E+00	4.22680000E+04	4.22602421E+04	7.75791985E+00	4.22470050E+04
258	-2.89112903E+00	4.26030000E+04	4.22547491E+04	3.48250894E+02	4.22413894E+04
259	-2.87903226E+00	4.23900000E+04	4.22492809E+04	1.40719116E+02	4.22357968E+04
260	-2.86693548E+00	4.23160000E+04	4.22438374E+04	7.21625543E+01	4.22302272E+04
261	-2.85483871E+00	4.26220000E+04	4.22384188E+04	3.83581176E+02	4.22246806E+04
262	-2.84274194E+00	4.22300000E+04	4.22330251E+04	-3.02505289E+00	4.22191572E+04
263	-2.83064516E+00	4.20870000E+04	4.22276562E+04	-1.40656166E+02	4.22136567E+04
264	-2.81854839E+00	4.26060000E+04	4.22231222E+04	3.83687801E+02	4.22081793E+04
265	-2.80645161E+00	4.27990000E+04	4.22169932E+04	5.82006813E+02	4.22027249E+04
266	-2.79435484E+00	4.19200000E+04	4.22116992E+04	-9.16959167E+02	4.21972936F+04
267	-2.78225806E+00	4.25700000E+04	4.22064302E+04	3.63569823E+02	4.21918853E+04
268	-2.77016129E+00	4.21130000E+04	4.22011863E+04	-8.81862555E+01	4.21865000E+04
269	-2.75806452E+00	4.20400000E+04	4.21959674E+04	-1.5596742E+02	4.21811378E+04

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270	-2.74596774E+00	4.21050000E+04	4.21907738E+04	-8.51737770E+01	4.21757987E+04
271	-2.73387079E+00	4.23260000E+04	4.21856053E+04	1.40394698E+02	4.21704825E+04
272	-2.72177419E+00	4.20860000E+04	4.21804621E+04	-9.44620591E+01	4.21651849E+04
273	-2.70567742E+00	4.19580000E+04	4.21753441E+04	-1.90344092E+02	4.21591945E+04
274	-2.69758065E+00	4.19190000E+04	4.21702514E+04	-2.51251446E+02	4.21546724E+04
275	-2.68548387E+00	4.21070000E+04	4.21651842E+04	-5.81841665E+01	4.21494484E+04
276	-2.67338710E+00	4.21620000E+04	4.21601423E+04	7.85770005E+00	4.21442475F+04
277	-2.66129032E+00	4.22320000E+04	4.21551259E+04	7.68741052E+01	4.21390696F+04
278	-2.64919355E+00	4.21870000E+04	4.20101350E+04	3.68649996E+01	4.21339147E+04
279	-2.63709677E+00	4.19950000E+04	4.21451697E+04	-1.50169667E+02	4.21287829E+04
280	-2.62500000E+00	4.22650000E+04	4.21402299E+04	1.24770053E+02	4.21236742E+04
281	-2.61290323E+00	4.17760000E+04	4.21353159E+04	-3.59315893E+02	4.21185884E+04
282	-2.6008645E+00	4.21560000E+04	4.21304276E+04	2.55724392E+01	4.21135257E+04
283	-2.58870968E+00	4.21900000E+04	4.21255650E+04	6.44349949E+01	4.21084861E+04
284	-2.57661290E+00	4.24440000E+04	4.21207283E+04	3.23271716E+02	4.21034695E+04
285	-2.56451613E+00	4.24760000E+04	4.21159175E+04	3.60082544E+02	4.20984759E+04
286	-2.55241935E+00	4.18560000E+04	4.21111326E+04	-2.55132583E+02	4.20935054E+04
287	-2.54032258E+00	4.19110000E+04	4.21063737E+04	-1.95373725E+02	4.20885579E+04
288	-2.52822581E+00	4.21430000E+04	4.21016409E+04	4.13590519E+01	4.20836335E+04
289	-2.51612903E+00	4.21890000E+04	4.20969340E+04	9.20656834E+01	4.20787321E+04
290	-2.50403226E+00	4.22310000E+04	4.20922539E+04	1.38746102E+02	4.20738537E+04
291	-2.49193548E+00	4.24100000E+04	4.20875998E+04	3.22400238E+02	4.20689984E+04
292	-2.47983871E+00	4.22910000E+04	4.20829720E+04	2.08028021E+02	4.20641661E+04
293	-2.46774195E+00	4.20230000E+04	4.20783707E+04	-5.53706224E+01	4.20593568E+04
294	-2.45564516E+00	4.21280000E+04	4.20737958E+04	5.42042327E+01	4.20545706E+04
295	-2.44354839E+00	4.18730000E+04	4.20692475E+04	-1.96247491E+02	4.20498075E+04
296	-2.43145161E+00	4.22110000E+04	4.20647259E+04	1.46274128E+02	4.20450674E+04
297	-2.41935484E+00	4.19940000E+04	4.20602310E+04	-6.62309923E+01	4.20403503E+04
298	-2.40725806E+00	4.22910000E+04	4.20557629E+04	3.52370640E+01	4.20356562E+04
299	-2.39516129E+00	4.20970000E+04	4.20513218E+04	4.56782109E+01	4.20309852E+04
300	-2.38306452E+00	4.19730000E+04	4.20469076E+04	-7.39076404E+01	4.20263373E+04
301	-2.37096774E+00	4.18620000E+04	4.20425206E+04	-1.80520581E+02	4.20217124E+04
302	-2.35887097E+00	4.21900000E+04	4.20381607E+04	1.51839295E+02	4.20171105E+04
303	-2.34677419E+00	4.23760000E+04	4.20338281E+04	3.42171892E+02	4.20125316E+04
304	-2.33467742E+00	4.21010000E+04	4.20295229E+04	7.14771088E+01	4.20079758E+04
305	-2.3225E0656E+00	4.22060000E+04	4.20252452E+04	1.80754844E+02	4.20034431E+04
306	-2.31048387E+00	4.21330000E+04	4.20209950E+04	1.12004993E+02	4.19989324E+04
307	-2.29838710E+00	4.20000000E+04	4.20167726E+04	-1.67725542E+01	4.19944467E+04
308	-2.28629032E+00	4.21220000E+04	4.20125779E+04	1.09422091E+02	4.19899830E+04
309	-2.27419355E+00	4.18320000E+04	4.20084112E+04	-1.76411185E+02	4.19855424E+04
310	-2.26209677E+00	4.18250000E+04	4.20042725E+04	-1.79272504E+02	4.19811249E+04
311	-2.25000000E+00	4.23870000E+04	4.20001620E+04	3.86838015E+02	4.19767304E+04
312	-2.23790323E+00	4.21530000E+04	4.19960798E+04	1.56920244E+02	4.19723589E+04
313	-2.22580645E+00	4.21780000E+04	4.19920259E+04	1.85974054E+02	4.19680105E+04
314	-2.21370968E+00	4.23280000E+04	4.19880007E+04	3.39999310E+02	4.19636851E+04
315	-2.20161290E+00	4.20400000E+04	4.19840041E+04	5.99958754E+01	4.19593827E+04
316	-2.18951613E+00	4.18030000E+04	4.19800364E+04	-1.77036393E+02	4.19551034E+04
317	-2.17741935E+00	4.20820000E+04	4.19760976E+04	1.05902357E+02	4.19508471E+04
318	-2.16532258E+00	4.19120000E+04	4.19721880E+04	-6.01880256E+01	4.19466139E+04
319	-2.15322581E+00	4.21C780000E+04	4.19683077E+04	1.09692303E+02	4.19424037E+04
320	-2.14112903E+00	4.19590000E+04	4.19644568E+04	-5.45681938E+00	4.19382165E+04
321	-2.12903226E+00	4.18440000E+04	4.19606356E+04	-1.16355559E+02	4.19340524E+04
322	-2.11693548E+00	4.17930000E+04	4.19568441E+04	-1.63844089E+02	4.19299113E+04
323	-2.10483871E+00	4.21350000E+04	4.19530826E+04	1.81917414E+02	4.19257933E+04
324	-2.09274194E+00	4.18710000E+04	4.19493512E+04	-7.83512351E+01	4.19216983E+04
325	-2.08064516E+00	4.21200000E+04	4.19456502E+04	1.74349774E+02	4.19176264E+04
326	-2.06854839E+00	4.17120000E+04	4.19419798E+04	-2.29979754E+02	4.19135775E+04
327	-2.05645161E+00	4.20020000E+04	4.19383400E+04	6.36599765E+01	4.19095516E+04
328	-2.04435484E+00	4.19310000E+04	4.19347312E+04	-3.73124355E+00	4.19055488E+04
329	-2.03225806E+00	4.16680000E+04	4.19311536E+04	-2.63153631E+02	4.19015690E+04
330	-2.02016129E+00	4.16300000E+04	4.19276074E+04	-2.97607412E+02	4.18976122E+04
331	-2.00806452E+00	4.21850000E+04	4.19240928E+04	2.60907184E+02	4.18936785E+04
332	-1.99596774E+00	4.20400000E+04	4.19206101E+04	1.19389914E+02	4.18897678E+04
333	-1.98387097E+00	4.19310000E+04	4.19171595E+04	1.38405298E+01	4.18858802E+04

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334	-1.97177419E+00	4.18920000E+04	4.19137412E+04	-2.17412256E+01	4.18820156E+04
335	-1.95967742E+00	4.22450000E+04	4.19103556E+04	3.34644380E+02	4.18781741E+04
336	-1.94758065E+00	4.20300000E+04	4.19070029E+04	9.59970715E+01	4.18743556E+04
337	-1.93548387E+00	4.23850000E+04	4.19036834E+04	4.81316561E+02	4.18705601E+04
338	-1.92338710E+00	4.17260000E+04	4.19003974E+04	-1.74397448E+02	4.18667877E+04
339	-1.91129032E+00	4.18430000E+04	4.18971453E+04	-5.41452625E+01	4.18630383E+04
340	-1.89919355E+00	4.14380000E+04	4.18939727E+04	-4.55927203E+02	4.18593119E+04
341	-1.88709677E+00	4.22710000E+04	4.18907436E+04	3.80256401E+02	4.18556086E+04
342	-1.87500000E+00	4.18630000E+04	4.18875948E+04	-2.45947959E+01	4.18519284E+04
343	-1.86290323E+00	4.19250000E+04	4.18844811E+04	4.05188512E+01	4.18482711E+04
344	-1.85080645E+00	4.17870000E+04	4.18814030E+04	-9.44020280E+01	4.18446370E+04
345	-1.83870968E+00	4.24380000E+04	4.18783608E+04	5.59639182E+02	4.18410258E+04
346	-1.82661290E+00	4.20000000E+04	4.18753549E+04	1.24645083E+02	4.18374377E+04
347	-1.81451613E+00	4.19200000E+04	4.18723857E+04	4.76142591E+01	4.18338726E+04
348	-1.80241935E+00	4.18890000E+04	4.18694537E+04	1.95462804E+01	4.18303306E+04
349	-1.79032258E+00	4.17970000E+04	4.18665593E+04	-6.95593015E+01	4.18268116E+04
350	-1.77822581E+00	4.17900000E+04	4.18637030E+04	-7.37029521E+01	4.18233157E+04
351	-1.76612903E+00	4.21250000E+04	4.18608852E+04	2.64114844E+02	4.18198428E+04
352	-1.75403226E+00	4.18040000E+04	4.18581046E+04	-5.41064173E+01	4.18163929E+04
353	-1.74193548E+00	4.15750000E+04	4.18553673E+04	-2.80367261E+02	4.18129661E+04
354	-1.72983871E+00	4.18740000E+04	4.18526682E+04	2.13317679E+01	4.18095623E+04
355	-1.71774194E+00	4.16140000E+04	4.18500999E+04	-2.360099C1E+02	4.18061816E+04
356	-1.70564516E+00	4.16180000E+04	4.18473929E+04	-2.29392859E+02	4.18028239E+04
357	-1.69354839E+00	4.20430000E+04	4.18448177E+04	1.98182274E+02	4.17994892E+04
358	-1.68145161E+00	4.18030000E+04	4.18422851E+04	-3.92851432E+01	4.17961776E+04
359	-1.66935484E+00	4.19150000E+04	4.18397958E+04	7.52042161E+01	4.17928890E+04
360	-1.65725806E+00	4.16870000E+04	4.18373503E+04	-1.50350348E+02	4.17896235F+04
361	-1.64516129E+C0	4.18480000E+04	4.18349496E+04	1.30504329E+01	4.17863810E+04
362	-1.63306452E+00	4.18450000E+04	4.18325945E+04	1.24057959E+01	4.17831615E+04
363	-1.62096774E+00	4.17390000E+04	4.18302851E+04	-9.12850561E+01	4.17799651E+04
364	-1.60887097E+00	4.17230000E+04	4.18280230E+04	-1.05022956E+02	4.17767917E+04
365	-1.59677419E+C0	4.18620000E+04	4.18125808E+04	3.61912259E+01	4.17736414E+04
366	-1.58467742E+00	4.18240000E+04	4.18236434E+04	3.56579612E-01	4.17705141E+04
367	-1.57258065E+00	4.16820000E+04	4.18215278E+04	-1.39527847E+02	4.17674098E+04
368	-1.56048387E+00	4.19620000E+04	4.18194630E+04	1.42536951E+02	4.17643286E+04
369	-1.54838710E+00	4.18840000E+04	4.18174501E+04	6.65499302E+01	4.17612704E+04
370	-1.53629032E+00	4.19390000E+04	4.18154900E+04	1.23509999E+02	4.17582353E+04
371	-1.52419355E+00	4.16180000E+04	4.18135840E+04	-1.95583986E+02	4.17552232E+04
372	-1.51209677E+C0	4.20400000E+04	4.18117332E+04	2.28266777E+02	4.17522342E+04
373	-1.50000000E+00	4.22700000E+04	4.18099390E+04	4.60061029E+02	4.17492681E+04
374	-1.48790323E+C0	4.17160000E+04	4.18082025E+04	-9.22025460E+01	4.17463252E+04
375	-1.47580645E+00	4.16510000E+04	4.18065253E+04	-1.55525333E+02	4.17434052E+04
376	-1.46370968E+00	4.14300000E+04	4.18049088E+04	-3.74908786E+02	4.17405083E+04
377	-1.45161290E+00	4.17650000E+04	4.18033544E+04	-3.83544293E+01	4.17376345F+04
378	-1.43951613E+00	4.16620000E+04	4.18018639E+04	-1.39863868E+02	4.17347837E+04
379	-1.42741935E+00	4.17790000E+04	4.18004388E+04	-2.14387878E+01	4.17319559E+04
380	-1.41532258E+00	4.17170000E+04	4.17998010E+04	-8.20809636E+01	4.17291512E+04
381	-1.40322581E+00	4.18570000E+04	4.17977923E+04	5.92077378E+01	4.17263695E+04
382	-1.39112903E+00	4.16290000E+04	4.17965747E+04	-1.67574650E+02	4.17236108E+04
383	-1.37903226E+C0	4.18100000E+04	4.17954302E+04	1.45698013E+01	4.17208752E+04
384	-1.36693548E+00	4.14680000E+04	4.17943611E+04	-3.26361092E+02	4.17181626E+04
385	-1.35483871E+00	4.16450000E+04	4.17933696E+04	-1.48369633E+02	4.17154731E+04
386	-1.34274194E+00	4.18860000E+04	4.17924583E+04	9.35417473E+01	4.17128066E+04
387	-1.33064516E+00	4.20130000E+04	4.17916295E+04	2.21370483E+02	4.17101632E+04
388	-1.31854839E+00	4.18030000E+04	4.17908861E+04	1.21138621E+01	4.17075428E+04
389	-1.30645161E+00	4.18250000E+04	4.17902310E+04	3.47690189E+01	4.17049454E+04
390	-1.29435484E+C0	4.21810000E+04	4.17896671E+04	3.91332921E+02	4.17023711E+04
391	-1.28225806E+00	4.18040000E+04	4.17891976E+04	1.48023610E+01	4.16998198E+04
392	-1.27016129E+C0	4.19440000E+04	4.1788261E+04	1.55173939E+02	4.16972915E+04
393	-1.25806452E+00	4.19350000E+04	4.17885595E+04	1.46444055E+02	4.16947863E+04
394	-1.24596774E+00	4.15750000E+04	4.17883911E+04	-2.13391110E+02	4.169230425E+04
395	-1.23367097E+00	4.20130000E+04	4.17883356E+04	2.24664393E+02	4.16898450E+04
396	-1.22177419E+00	4.18820000E+04	4.17883937E+04	9.36062592E+01	4.16874089E+04
397	-1.20967742E+00	4.2C9400000E+04	4.17885701E+04	3.05429919E+02	4.16849959E+04

APPENDIX C – Continued

398	-1.19758065E+00	4.19250000E+04	4.17888695E+04	1.36130510E+32	4.16826059E+04
399	-1.18548387E+00	4.15180000E+04	4.17892171E+04	-2.71297139E+02	4.16802389E+04
400	-1.17338710E+00	4.15450000E+04	4.17898585E+04	-2.44858538E+02	4.16778950F+04
401	-1.16129C32E+00	4.2C870000E+04	4.17905596E+04	2.96440446E+02	4.16755741E+04
402	-1.14919355E+00	4.21450000E+04	4.17914064E+04	3.53593550E+02	4.16732763E+04
403	-1.13709677E+00	4.15320000E+04	4.17924059E+04	-2.604059C5E+02	4.16710015E+04
404	-1.12500000E+00	4.15520000E+04	4.17935651E+04	1.58434942E+02	4.16687497E+04
405	-1.11290323E+00	4.17950000E+04	4.17948915E+04	1.08462012E-01	4.16665210E+04
406	-1.10080645E+00	4.15620000E+04	4.17963935E+04	-2.34393509E+02	4.16643153E+04
407	-1.08870968E+00	4.19300000E+04	4.17980797E+04	1.31920286E+02	4.16621326E+04
408	-1.07661290E+00	4.2C940000E+04	4.17995955E+04	2.94040476E+02	4.16599730E+04
409	-1.06451613E+00	4.12460000E+04	4.18020430E+04	-5.56042991E+02	4.16578365E+04
410	-1.05241935E+00	4.15380000E+04	4.1803409E+04	-2.66340911E+02	4.16557230E+04
411	-1.04032258E+00	4.22960000E+04	4.18068649E+04	4.89135113E+02	4.16536325E+04
412	-1.02822581E+00	4.17900000E+04	4.18096274E+04	-1.96274013E+01	4.16515650F+04
413	-1.01612903E+00	4.2C830000E+04	4.18126419E+04	2.70358103E+02	4.16495206E+04
414	-1.00403226E+00	4.17590000E+04	4.18159229E+04	-5.79228673E+01	4.16474993E+04
415	-9.91935484E-01	4.18030000E+04	4.18194860E+04	-1.04859504E+01	4.16455010E+04
416	-9.79838710E-01	4.20710000E+04	4.18233480E+04	2.47651958E+02	4.16435257E+04
417	-9.67741935E-01	4.18900000E+04	4.18275274E+04	6.24725874E+01	4.16415734E+04
418	-9.55645161E-01	4.15230000E+04	4.18302438E+04	-3.09043846E+02	4.16396442E+04
419	-9.43548387E-01	4.2C940000E+04	4.18369188E+04	2.57081217E+02	4.16377381E+04
420	-9.31451613E-01	4.21930000E+04	4.18421755E+04	3.50824506E+02	4.16358550E+04
421	-9.19354839E-C1	4.18940000E+04	4.18478393E+04	4.61607386E+01	4.16339949E+04
422	-9.07258065E-01	4.1E510000E+04	4.18539376E+04	-2.93758647E+00	4.16321579E+04
423	-8.95161290E-01	4.16340000E+04	4.18605004E+04	-2.26500425E+02	4.16303439E+04
424	-8.83064516E-01	4.16690000E+04	4.18675604E+04	-1.98560446E+02	4.16285529E+04
425	-8.70967742E-01	4.15990000E+04	4.18751533E+04	-2.76153324E+02	4.16267850E+04
426	-8.58870968E-01	4.17320000E+04	4.18833181E+04	-1.01318071E+02	4.16250401E+04
427	-8.46774194E-01	4.16310000E+04	4.18920974E+04	-2.61097401E+02	4.16233143E+04
428	-8.34677419E-01	4.19090000E+04	4.19015382E+04	7.46184666E+00	4.16216105E+04
429	-8.22580645E-01	4.1E540000E+04	4.19116918E+04	-5.67916707E+01	4.16199437E+04
430	-8.10483871E-01	4.21700000E+04	4.19226148E+04	2.47385218E+02	4.16182910E+04
431	-7.98387097E-01	4.2C320000E+04	4.19346956E+04	9.76304961E+01	4.16166613E+04
432	-7.86290323E-01	4.22300000E+04	4.19470246E+04	2.82975372E+02	4.16150547E+04
433	-7.74193548E-01	4.22350000E+04	4.19606560E+04	2.74343957E+02	4.16134711F+04
434	-7.62096774E-01	4.19520000E+04	4.19753477E+04	-2.33477056E+01	4.16119105E+04
435	-7.50000000E-01	4.15910000E+04	4.19911926E+04	-4.00192643E+02	4.16103730F+04
436	-7.37903226E-01	4.21560000E+04	4.20082941E+04	1.477059C5E+02	4.16088586F+04
437	-7.258C6452E-C1	4.19960000E+04	4.20267668E+04	-3.07668115E+01	4.16073671E+04
438	-7.13709677E-C1	4.2C140000E+04	4.20467385E+04	-3.27385342E+01	4.16058987E+04
439	-7.01612903E-01	4.21260000E+04	4.20683517E+04	5.76483132E+01	4.16045344E+04
440	-6.89516129E-01	4.1E790000E+04	4.20917653E+04	-2.12765300E+02	4.16030311E+04
441	-6.77419355E-01	4.14150000E+04	4.21171572E+04	-7.02157208E+02	4.16016318E+04
442	-6.65322581E-C1	4.21350000E+04	4.21447265E+04	4.02734534E+01	4.16002556E+04
443	-6.53225806E-01	4.16200000E+04	4.21746966E+04	-5.54696593E+02	4.15989024E+04
444	-6.41129C32E-01	4.21830000E+04	4.22073180E+04	-2.43179895E+01	4.15C75722F+04
445	-6.29032258E-01	4.17340000E+04	4.22428724E+04	-5.08872377E+02	4.15962651F+04
446	-6.16354838E-01	4.20300000E+04	4.22816765E+04	-2.51676482E+02	4.15949811F+04
447	-6.04838710E-01	4.2C570000E+04	4.23240867E+04	-2.67086670E+02	4.15C37200E+04
448	-5.92741935E-01	4.23290000E+04	4.23705040E+04	-4.15039673E+01	4.15924820F+04
449	-5.80645161E-01	4.18760000E+04	4.24213795E+04	-5.45379518E+02	4.15C12671E+04
450	-5.68548387E-01	4.22920000E+04	4.24772204E+04	-1.85220378E+02	4.15C00752E+04
451	-5.56451613E-C1	4.25450000E+04	4.25385955E+04	6.40452591E+00	4.15R89063E+04
452	-5.44354839E-01	4.27890000E+04	4.26061414E+04	1.828585C4E+02	4.15877605E+04
453	-5.32258065E-01	4.26010000E+04	4.26805676E+04	-7.95675695E+01	4.15866377F+04
454	-5.20161290E-01	4.3C890000E+04	4.27626598E+04	3.26340218E+02	4.15855380E+04
455	-5.08064516E-01	4.29300000E+04	4.28532812E+04	1.29718838E+02	4.15844613E+04
456	-4.95567742E-01	4.31120000E+04	4.29533684E+04	1.58631621E+02	4.15834076E+04
457	-4.83870968E-01	4.29360000E+04	4.30639206E+04	-1.27920567E+02	4.15823770F+04
458	-4.71774194E-01	4.28310000E+04	4.31859770E+04	-3.54977016E+02	4.15813644E+04
459	-4.59677419E-01	4.32940000E+04	4.33205783E+04	-2.65783396E+01	4.15803848E+04
460	-4.47580645E-01	4.32750000E+04	4.34687040E+04	-1.93704007E+02	4.15794233E+04
461	-4.35483871E-01	4.38670000E+04	4.36311773E+04	2.35822657E+02	4.15784849E+04

462	-4.23387097E-01	4.4C030000E+04	4.38085276E+04	1.94472417E+02	4.15775694F+04
463	-4.11290323E-01	4.35660000E+04	4.40007985E+04	-3.47984974E+01	4.15766771E+04
464	-3.99193548E-01	4.46660000E+04	4.42072960E+04	4.58703955E+02	4.15758077E+04
465	-3.87096774E-01	4.48460000E+04	4.4262762E+04	4.19723802E+02	4.15749614E+04
466	-3.75000000E-01	4.46840000E+04	4.46545917E+04	2.94083339E+01	4.15741382E+04
467	-3.62903226E-01	4.50540000E+04	4.4887345E+04	1.66654546E+02	4.15733379E+04
468	-3.50806452E-01	4.53470000E+04	4.51176390E+04	2.79361005E+02	4.15725608E+04
469	-3.38709677E-01	4.52990000E+04	4.53365438E+04	-3.75438083E+01	4.15718066E+04
470	-3.26612903E-01	4.54950000E+04	4.55334461E+04	-3.84460802E+01	4.15710755E+04
471	-3.14516129E-01	4.54670000E+04	4.56968802E+04	-2.29880193E+02	4.15703675E+04
472	-3.02419355E-01	4.60270000E+04	4.58158518E+04	2.11148173E+02	4.15696824E+04
473	-2.90322581E-01	4.55870000E+04	4.58814618E+04	-2.94461829E+02	4.15690205E+04
474	-2.78225806E-01	4.56700000E+04	4.58884493E+04	-2.18449274E+02	4.15683815E+04
475	-2.66129032E-01	4.53510000E+04	4.58361933E+04	-4.85193280E+02	4.15677656E+04
476	-2.54032258E-01	4.52390000E+04	4.57288355E+04	-4.89835470E+02	4.15671728E+04
477	-2.41935484E-01	4.57000000E+04	4.55744799E+04	1.2552009E+02	4.15666029E+04
478	-2.29838710E-01	4.55470000E+04	4.53837454E+04	1.63254607E+02	4.15660562E+04
479	-2.17741935E-01	4.57880000E+04	4.51681200E+04	6.19880049E+02	4.15655324E+04
480	-2.05645161E-01	4.48000000E+04	4.49385346E+04	-1.38534572E+02	4.15650317E+04
481	-1.93548387E-01	4.49810000E+04	4.47043984E+04	2.76601650E+02	4.15645541E+04
482	-1.81451613E-01	4.43470000E+04	4.44731372E+04	-1.26137164E+02	4.15640995E+04
483	-1.69354839E-01	4.44000000E+04	4.42501410E+04	1.49859019E+02	4.15636679E+04
484	-1.57258065E-01	4.42280000E+04	4.40389724E+04	1.89027634E+02	4.15632503E+04
485	-1.45161290E-01	4.40930000E+04	4.38416989E+04	2.51301128E+02	4.15628735E+04
486	-1.33064516E-01	4.36920000E+04	4.36592506E+04	3.27494456E+01	4.15625114E+04
487	-1.20967742E-01	4.38240000E+04	4.34917454E+04	3.32254635E+02	4.15621720E+04
488	-1.08870968E-01	4.33810000E+04	4.33387574E+04	4.22426221E+01	4.15618556E+04
489	-9.67741935E-02	4.31290000E+04	4.31959232E+04	-7.05232254E+01	4.15615623E+04
490	-8.46774194E-02	4.29810000E+04	4.30730927E+04	-9.20927209E+01	4.15612920E+04
491	-7.25806452E-02	4.31380000E+04	4.29584338E+04	1.79566211E+02	4.15610447E+04
492	-6.04838710E-02	4.26230000E+04	4.28545023E+04	-2.31502310E+02	4.15608205E+04
493	-4.83870968E-02	4.27710000E+04	4.27602862E+04	1.07137637E+01	4.15606193E+04
494	-3.62903226E-02	4.25810000E+04	4.26748315E+04	-9.38315441E+01	4.15604412E+04
495	-2.41935484E-02	4.26460000E+04	4.25972558E+04	4.87442381E+01	4.15602861E+04
496	-1.20967742E-02	4.24550000E+04	4.25267533E+04	-7.17532920E+01	4.15601541E+04
497	0.	4.24050000E+04	4.24625955E+04	-5.75955074E+01	4.15600451E+04
498	1.20967742E-02	4.23710000E+04	4.24041277E+04	-3.31276856F+01	4.15599591E+04
499	2.41935484E-02	4.21210000E+04	4.23507642E+04	-2.29764174E+02	4.15598962E+04
500	3.62903226E-02	4.24840000E+04	4.23019827E+04	1.82017300E+02	4.15598563E+04
501	4.83870968E-02	4.21890000E+04	4.22573184E+04	-6.83184215E+01	4.15598394E+04
502	6.04838710E-02	4.21270000E+04	4.22163581E+04	-8.93580619E+01	4.15598456E+04
503	7.25806452E-02	4.19830000E+04	4.21787344E+04	-1.95734360E+02	4.15598748E+04
504	8.46774194E-02	4.20080000E+04	4.21441209E+04	-1.36120929E+02	4.15599271E+04
505	9.67741935E-02	4.20830000E+04	4.21122276E+04	-2.92275862E+01	4.15600024E+04
506	1.08870968E-01	4.18620000E+04	4.20827961E+04	-2.20796145E+02	4.15601008E+04
507	1.20967742E-01	4.22640000E+04	4.2055967E+04	2.08403329E+02	4.15602222E+04
508	1.33064516E-01	4.19210000E+04	4.20304242E+04	-1.09424154E+02	4.15603666E+04
509	1.45161290E-01	4.19730000E+04	4.20070956E+04	-3.40955770E+01	4.15605341E+04
510	1.57258065E-01	4.20630000E+04	4.19854473E+04	7.75526664E+01	4.15607246E+04
511	1.69354839E-01	4.20560000E+04	4.19653330E+04	9.06670428E+01	4.15609381E+04
512	1.81451613E-01	4.19920000E+04	4.19466211E+04	4.53788697E+01	4.15611747E+04
513	1.93548387E-01	4.15890000E+04	4.19291939E+04	-3.40193938E+02	4.15614344E+04
514	2.05645161E-01	4.16600000E+04	4.19129453E+04	-2.52945334E+02	4.15617171E+04
515	2.17741935E-01	4.15980000E+04	4.18977798E+04	-2.99779802E+02	4.15620228E+04
516	2.29838710E-01	4.19550000E+04	4.18836112E+04	1.11388829E+02	4.15623515E+04
517	2.41935484E-01	4.14940000E+04	4.18703616E+04	-3.76361583E+02	4.15627033E+04
518	2.54032258E-01	4.15960000E+04	4.18579606E+04	-2.61960581E+02	4.15630782E+04
519	2.66129032E-01	4.16600000E+04	4.18463443E+04	-1.86344311E+02	4.15634760E+04
520	2.78225806E-01	4.19400000E+04	4.18354548E+04	1.04545189E+02	4.15638970E+04
521	2.90322581E-01	4.15920000E+04	4.18252394E+04	-2.33239397E+02	4.15643409E+04
522	3.02419355E-01	4.17710000E+04	4.18156501E+04	-4.46501036E+01	4.15648079E+04
523	3.14516129E-01	4.15130000E+04	4.18066432E+04	-2.93643206E+02	4.15652979E+04
524	3.26612903E-01	4.16970000E+04	4.17981788E+04	-1.01178786E+02	4.15658110E+04
525	3.38709677E-01	4.18280000E+04	4.17902203E+04	3.77796510E+01	4.15663471E+04

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526	3.50806452E-01	4.14570000E+04	4.17827345E+04	-3.25734490E+02	4.15669063E+04
527	3.62903226E-01	4.16240000E+04	4.17756906E+04	-1.51690586E+02	4.15674885E+04
528	3.75000000E-01	4.16590000E+04	4.17690605E+04	-1.10060534E+02	4.15680937E+04
529	3.87096774E-01	4.18010000E+04	4.17628185E+04	3.81814954E+01	4.15687220E+04
530	3.99193548E-01	4.18660000E+04	4.17569407E+04	1.09059265E+02	4.15693733E+04
531	4.11290323E-01	4.15300000E+04	4.17514053E+04	-2.21405332E+02	4.15700477E+04
532	4.23387097E-01	4.14150000E+04	4.17461921E+04	-3.31192105E+02	4.15707451E+04
533	4.35483871E-01	4.18180000E+04	4.17412824E+04	7.67175882E+01	4.15714656E+04
534	4.47580645E-01	4.17180000E+04	4.17366590E+04	-1.86590168E+01	4.15722090E+04
535	4.59677419E-01	4.18540000E+04	4.17323060E+04	1.21694028E+02	4.15729756E+04
536	4.71774194E-01	4.15510000E+04	4.17282085E+04	-1.77208501E+02	4.15737651E+04
537	4.83870968E-01	4.13980000E+04	4.17243529E+04	-3.26352904E+02	4.15745777E+04
538	4.95967742E-01	4.15660000E+04	4.17207265E+04	-1.54726459E+02	4.15754134E+04
539	5.08064516E-01	4.16110000E+04	4.17173173E+04	-1.06317348E+02	4.15762721E+04
540	5.20161290E-01	4.18230000E+04	4.17141146E+04	1.08885426E+02	4.15771538E+04
541	5.32258065E-01	4.14900000E+04	4.17111079E+04	-2.21107902E+02	4.15780585E+04
542	5.44354839E-01	4.16190000E+04	4.17082878E+04	-8.92877930E+01	4.15789863E+04
543	5.56451613E-01	4.14910000E+04	4.17056453E+04	-2.14645348E+02	4.15799372E+04
544	5.68548387E-01	4.18250000E+04	4.17031723E+04	2.1287740E+02	4.15809111E+04
545	5.80645161E-01	4.17260000E+04	4.17008608E+04	2.51392331E+01	4.15819080E+04
546	5.92741935E-01	4.18620000E+04	4.16987036E+04	1.63296390E+02	4.15829280E+04
547	6.04838710E-01	4.19370000E+04	4.16966940E+04	2.40306006E+02	4.15839710E+04
548	6.16935484E-01	4.22070000E+04	4.16948256E+04	5.12174445E+02	4.15850370E+04
549	6.29032258E-01	4.20770000E+04	4.16930923E+04	3.83907673F+02	4.15861261E+04
550	6.41129032E-01	4.13270000E+04	4.16914887E+04	-3.64488712E+02	4.15872382E+04
551	6.53225806E-01	4.17640000E+04	4.16900095E+04	7.39905463E+01	4.15883734E+04
552	6.65322581E-01	4.16590000E+04	4.16886496E+04	-2.96496141E+01	4.15895316E+04
553	6.77419355E-01	4.20540000E+04	4.16874045E+04	3.66595450E+02	4.15907129E+04
554	6.89516129E-01	4.16930000E+04	4.16862699E+04	6.73010879E+00	4.15919172E+04
555	7.01612903E-01	4.14590000E+04	4.16852415E+04	-2.26241524E+02	4.15931445E+04
556	7.13709677E-01	4.16350000E+04	4.16843156E+04	-4.93155726E+01	4.15943949E+04
557	7.25806452E-01	4.20400000E+04	4.16834884E+04	3.56511619E+02	4.15956683E+04
558	7.37903226E-01	4.19180000E+04	4.16827565E+04	2.35243500E+02	4.15969647E+04
559	7.50000000E-01	4.15210000E+04	4.16821167E+04	-1.61116675E+02	4.15982842E+04
560	7.62096774E-01	4.17570000E+04	4.16815658E+04	7.54341709E+01	4.15996267E+04
561	7.74193548E-01	4.19280000E+04	4.16811011E+04	2.46898944E+02	4.16009923E+04
562	7.86290323E-01	4.18090000E+04	4.16807196E+04	1.28280395E+02	4.16123809E+04
563	7.98387097E-01	4.15260000E+04	4.16804189E+04	-1.54418873E+02	4.16037926E+04
564	8.10483871E-01	4.15770000E+04	4.16801964E+04	-1.03196397E+02	4.16052273E+04
565	8.22580645E-01	4.16480000E+04	4.16800498E+04	-3.20498420E+01	4.16066850E+04
566	8.34677419E-01	4.11770000E+04	4.16799770E+04	-5.02976993E+02	4.16081658E+04
567	8.46774194E-01	4.20200000E+04	4.16799758E+04	3.40024248E+02	4.16096656E+04
568	8.58870968E-01	4.16190000E+04	4.16800441E+04	-6.10441258E+01	4.16111965E+04
569	8.70967742E-01	4.17150000E+04	4.16801802E+04	3.48197777E+01	4.16127463E+04
570	8.83064516E-01	4.22250000E+04	4.16803822E+04	5.44617756E+02	4.16143193E+04
571	8.95161290E-01	4.15520000E+04	4.16806485E+04	-1.28648483E+02	4.16159153E+04
572	9.07258065E-01	4.15230000E+04	4.16809773E+04	-1.57977315F+02	4.16175343E+04
573	9.19354839E-01	4.19400000E+04	4.16813672E+04	2.586328C6E+02	4.16179176E+04
574	9.31451613E-01	4.15590000E+04	4.16818166E+04	2.77183351E+02	4.16208414E+04
575	9.43548387E-01	4.18010000F+04	4.16823243E+04	1.18675722E+02	4.16225296E+04
576	9.55645161E-01	4.17240000E+04	4.16828887E+04	4.11112521E+01	4.16242407E+04
577	9.67741935E-01	4.14020000E+04	4.16835088E+04	-2.81508785E+02	4.16259750E+04
578	9.79838710E-01	4.19370000E+04	4.16841832E+04	2.52816823E+02	4.16277322E+04
579	9.91935484E-01	4.14900000E+04	4.16849108E+04	-1.94910765E+02	4.16295125E+04
580	1.00403226E+00	4.15640000E+04	4.16856904E+04	-1.21690445E+02	4.16313159E+04
581	1.01612903E+00	4.14230000E+04	4.16865212E+04	-2.63521163E+02	4.16331422E+04
582	1.02822581E+00	4.17520000F+04	4.16874019E+04	6.45580850E+01	4.16349917E+04
583	1.04032258E+00	4.19320000E+04	4.16883317E+04	2.43668274E+02	4.16368641F+04
584	1.05241935E+00	4.17940000E+04	4.16893097E+04	1.04690313E+02	4.16387596E+04
585	1.06451613E+00	4.13630000E+04	4.16903349E+04	-2.27334914E+02	4.16406782E+04
586	1.07661290E+00	4.14450000E+04	4.16914066E+04	-2.46406565E+02	4.16426197E+04
587	1.08670568E+00	4.19110000E+04	4.16925238E+04	2.18476165E+02	4.16445844F+04
588	1.10080445E+00	4.15610000E+04	4.16936860E+04	2.67314050E+02	4.16465720E+04

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589	1.11290323E+00	4.19270000E+04	4.16948922E+04	2.32107827E+02	4.16485827E+04
590	1.12500000E+00	4.15050000E+04	4.16961418E+04	-1.91141794E+02	4.16506165E+04
591	1.13709677E+00	4.16020000E+04	4.16974341E+04	-9.54341361E+01	4.16526732E+04
592	1.14919355E+00	4.16790000E+04	4.16987685E+04	-2.07685470E+01	4.16547531E+04
593	1.16129032E+00	4.17110000E+04	4.17001444E+04	1.08555971E+01	4.16568559E+04
594	1.17338710E+00	4.16000000E+04	4.17015611E+04	-1.01561105E+02	4.16589818E+04
595	1.18548387E+00	4.15650000E+04	4.17030191E+04	-1.38018078E+02	4.16611308E+04
596	1.197580C65E+00	4.15240000E+04	4.17045148E+04	-1.80514770E+02	4.16632028E+04
597	1.20967742E+00	4.15270000E+04	4.17060507E+04	-1.79050652E+02	4.16654978E+04
598	1.22177419E+00	4.18350000E+04	4.17076252E+04	1.27374786E+02	4.16677159E+04
599	1.23387097E+00	4.17280000E+04	4.17092380E+04	1.87620342E+01	4.16699570E+04
600	1.24596774E+00	4.18970000E+04	4.17108884E+04	1.86111562E+02	4.16722211E+04
601	1.258C6452E+00	4.17290000E+04	4.17125762E+04	1.64238220E+01	4.16745083E+04
602	1.27016129E+00	4.14880000E+04	4.17143008E+04	-2.26300751E+02	4.16768185E+04
603	1.28225806E+00	4.16140000E+04	4.17160617E+04	-1.02061737E+02	4.16791518E+04
604	1.29435484E+00	4.18830000E+04	4.17178587E+04	1.65141266E+02	4.16815081E+04
605	1.30645161E+00	4.19420000E+04	4.17196914E+04	2.22308645E+02	4.16838874E+04
606	1.31854839E+00	4.14800000E+04	4.17215592E+04	-2.41559224E+02	4.16862898E+04
607	1.330E4516E+00	4.17200000E+04	4.17234620E+04	-3.46198359E+00	4.16887153E+04
608	1.34274194E+00	4.15030000E+04	4.17253993E+04	-2.22399286E+02	4.16911637E+04
609	1.35483871E+00	4.17590000E+04	4.17273708E+04	3.16292036E+01	4.16936352E+04
610	1.36693548E+00	4.14980000E+04	4.17293762E+04	-2.31376194E+02	4.16961298E+04
611	1.37903226E+00	4.15700000E+04	4.17314152E+04	-1.61415167E+02	4.16986474E+04
612	1.39112903E+00	4.18070000E+04	4.17348746E+04	7.35125843E+01	4.17011880E+04
613	1.40322581E+00	4.19730000E+04	4.17355927E+04	2.37407348E+02	4.17C37517E+04
614	1.41532258E+00	4.14150000E+04	4.17377306E+04	-3.22730596E+02	4.17063384E+04
615	1.42741935E+00	4.15980000E+04	4.17399010E+04	-1.41900980E+02	4.17C89481E+04
616	1.43951613E+00	4.19190000E+04	4.17421035E+04	1.76896459E+02	4.17115809E+04
617	1.45161290E+00	4.16240000E+04	4.17443380E+04	-1.20338031E+02	4.17142368E+04
618	1.46370568E+00	4.21490000E+04	4.17466042E+04	4.02395754E+02	4.17169156E+04
619	1.47580645E+00	4.18250000E+04	4.17489018E+04	7.60981683E+01	4.17196175E+04
620	1.48790323E+00	4.16510000E+04	4.17512307E+04	-1.00230682E+02	4.17223425E+04
621	1.50000000E+00	4.20630000E+04	4.17535905E+04	3.09409463E+02	4.17250905E+04
622	1.51209677E+00	4.16680000E+04	4.17559812E+04	-8.79811864E+01	4.17278151E+04
623	1.52419355E+00	4.15880000E+04	4.17584024E+04	2.29597575E+02	4.17306556E+04
624	1.53629032E+00	4.15770000E+04	4.17608541E+04	-1.83854054E+02	4.1734727E+04
625	1.54838710E+00	4.17370000E+04	4.17633359E+04	-2.63358826E+01	4.17363129E+04
626	1.56048387E+00	4.17530000E+04	4.17658477E+04	-1.28477254E+01	4.173C1761E+04
627	1.57258065E+00	4.17640000E+04	4.17683894E+04	-4.38940289E+00	4.17420623E+04
628	1.58467742E+00	4.18340000E+04	4.17709607E+04	6.30392587E+01	4.17449716E+04
629	1.59677419E+00	4.19390000E+04	4.17735616E+04	1.65438427E+02	4.17479019E+04
630	1.60887097E+00	4.16960000E+04	4.17761917E+04	-8.01917336E+01	4.17508552E+04
631	1.62096774E+00	4.16470000E+04	4.17788511E+04	-1.31851067E+02	4.17538376E+04
632	1.63306452E+00	4.17700000E+04	4.17815394E+04	-1.15394190E+01	4.17568391E+04
633	1.64516129E+00	4.17380000E+04	4.17842566E+04	-4.62566422E+01	4.17598638E+04
634	1.65725806E+00	4.19010000E+04	4.17870026E+04	1.12597407E+02	4.17629111E+04
635	1.66935484E+00	4.18950000E+04	4.17897771E+04	1.05222868E+02	4.17659816E+04
636	1.68145161E+00	4.21630000E+04	4.17925801E+04	3.70419877E+02	4.17690752E+04
637	1.69354839E+00	4.18520000E+04	4.17954114E+04	5.65885625E+01	4.17721919E+04
638	1.70564516E+00	4.21170000E+04	4.17982709E+04	3.18729053E+02	4.17753316E+04
639	1.71774194E+00	4.18530000E+04	4.18011585E+04	5.18414720E+01	4.17784943E+04
640	1.72583871E+00	4.19830000E+04	4.18040741E+04	1.78925938E+02	4.17816800E+04
641	1.74193548E+00	4.18210000E+04	4.18070174E+04	1.39825683E+01	4.17848888E+04
642	1.75403226E+00	4.14530000E+04	4.18099885E+04	-3.56988525E+02	4.17881207E+04
643	1.76612903E+00	4.20690000E+04	4.18129872E+04	2.56012766E+02	4.17913756E+04
644	1.77822581E+00	4.18750000E+04	4.18160135E+04	5.89865459E+01	4.17946535E+04
645	1.79032258E+00	4.16830000E+04	4.18190671E+04	-1.36067072E+02	4.17979544E+04
646	1.80241935E+00	4.20320000E+04	4.18221480E+04	2.09852020E+02	4.18012784E+04
647	1.81451613E+00	4.22290000E+04	4.18252561E+04	4.03743868E+02	4.18046255E+04
648	1.82661290E+00	4.19810000E+04	4.18283914E+04	1.52608621E+02	4.18079956E+04
649	1.83870968E+00	4.19530000E+04	4.18315536E+04	1.21446353E+02	4.18113887E+04
650	1.85080645E+00	4.20340000E+04	4.18347428E+04	1.99257153E+02	4.18148049E+04
651	1.86290323E+00	4.17530000E+04	4.18379589E+04	-8.49588920E+01	4.18182441E+04
652	1.87500000E+00	4.17080000E+04	4.18412017E+04	-1.33201697E+02	4.18217063E+04

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653	1.88709677E+00	4.16680000E+04	4.18444712E+04	-1.76471181E+02	4.18251916E+04
654	1.89919355E+00	4.20480000E+04	4.18477673E+04	2.00232736E+02	4.18286999E+04
655	1.91129032E+00	4.20290000E+04	4.18510899E+04	1.77910133E+02	4.18322313E+04
656	1.92338710E+00	4.13980000E+04	4.18544389E+04	-4.56438915E+02	4.18357857E+04
657	1.93548387E+00	4.18760000E+04	4.18578143E+04	1.81856644E+01	4.18393631E+04
658	1.94758065E+00	4.18490000E+04	4.18612161E+04	-1.22160561E+01	4.18429636E+04
659	1.95967742E+00	4.18760000E+04	4.18646440E+04	1.13559930E+01	4.18465871E+04
660	1.97177419E+00	4.19310000E+04	4.18680981E+04	6.29018793E+01	4.18502337E+04
661	1.98387097E+00	4.22370000E+04	4.18715783E+04	3.65421669E+02	4.18539033E+04
662	1.99596774E+00	4.15470000E+04	4.18750846E+04	-3.28084574E+02	4.18575960E+04
663	2.00806452E+00	4.17700000E+04	4.18786168E+04	-1.08616786E+02	4.18613117E+04
664	2.02016129E+00	4.21720000E+04	4.18821749E+04	2.89825092E+02	4.18650504E+04
665	2.03225806E+00	4.17370000E+04	4.18857589E+04	-1.48758878E+02	4.18688122E+04
666	2.04435484E+00	4.17980000E+04	4.18893686E+04	-9.13686408E+01	4.18725970E+04
667	2.05645161E+00	4.20600000E+04	4.18930041E+04	1.66995862E+02	4.18764048E+04
668	2.06854839E+00	4.19250000E+04	4.18966653E+04	2.83346843E+01	4.18802357E+04
669	2.08064516E+00	4.22470000E+04	4.19003521E+04	3.46647880E+02	4.18840896E+04
670	2.09274194E+00	4.16800000E+04	4.19040645E+04	-2.24064498E+02	4.18879666E+04
671	2.10483871E+00	4.18000000E+04	4.19078024E+04	-1.07802400E+02	4.18918666E+04
672	2.11693548E+00	4.19130000E+04	4.19115658E+04	1.43422368E+00	4.18957897E+04
673	2.12903226E+00	4.20140000E+04	4.19153546E+04	9.86454224E+01	4.18997358E+04
674	2.14112903E+00	4.21160000E+04	4.19196168E+04	1.96831243E+02	4.19037049E+04
675	2.15322581E+00	4.20460000E+04	4.19230083E+04	1.22991731E+02	4.19076971E+04
676	2.16532258E+00	4.20770000E+04	4.19268731E+04	1.50126932E+02	4.19117123E+04
677	2.17741935E+00	4.17000000E+04	4.19307631E+04	-2.30763110E+02	4.19157505E+04
678	2.18951613E+00	4.16870000E+04	4.19346784E+04	-2.47678353E+02	4.19198118E+04
679	2.20161290E+00	4.21610000E+04	4.19386188E+04	2.22381245E+02	4.19238962E+04
680	2.21370968E+00	4.171410000E+04	4.19425843E+04	-2.01584275E+02	4.19280035E+04
681	2.22580645E+00	4.18280000E+04	4.19465749E+04	-1.18574874E+02	4.19321339E+04
682	2.23790323E+00	4.19710000E+04	4.19505905E+04	2.04094883E+01	4.19362874E+04
683	2.25000000E+00	4.20500000E+04	4.19546312E+04	9.53688484E+01	4.19404639E+04
684	2.26209677E+00	4.20430000E+04	4.19586968E+04	8.43032438E+01	4.19446634E+04
685	2.27419355E+00	4.20130000E+04	4.19627873E+04	5.02127106E+01	4.19488860E+04
686	2.28629032E+00	4.20000000E+04	4.19669027E+04	3.30972841E+01	4.19531316E+04
687	2.29838710E+00	4.16760000E+04	4.19710430E+04	-2.95043001E+02	4.19574003E+04
688	2.31048387E+00	4.15820000E+04	4.19752081E+04	6.79188834E+00	4.19616920E+04
689	2.32258065E+00	4.20350000E+04	4.19793980E+04	5.56019856E+01	4.19660067E+04
690	2.33467742E+00	4.21150000E+04	4.19836127E+04	1.31387323E+02	4.19703445E+04
691	2.34677419E+00	4.20530000E+04	4.19878521E+04	6.51479313E+01	4.19747053E+04
692	2.35887097E+00	4.19630000E+04	4.19921162E+04	-2.91161582E+01	4.19790892E+04
693	2.37096774E+00	4.2C810000E+04	4.19964049E+04	8.45950843E+01	4.19834961E+04
694	2.38306452E+00	4.18130000E+04	4.20007183E+04	-1.87718312E+02	4.19879260E+04
695	2.39516129E+00	4.16500000E+04	4.20050563E+04	-3.55056318E+02	4.19923790E+04
696	2.40725806E+00	4.17150000E+04	4.20094189E+04	-2.94418906E+02	4.19968550E+04
697	2.41935484E+00	4.20660000E+04	4.20138060E+04	5.21939513E+01	4.20013541E+04
698	2.43145161E+00	4.20000000E+04	4.20182177E+04	-1.82177190E+01	4.20058762E+04
699	2.44354839E+00	4.20000000E+04	4.20226539E+04	-2.26538909E+01	4.20104213E+04
700	2.45564516E+00	4.2C860000E+04	4.20271145E+04	5.88854614E+01	4.20149895E+04
701	2.46677419E+00	4.19630000E+04	4.20315996E+04	-6.85996372E+01	4.20195807E+04
702	2.47983871E+00	4.20000000E+04	4.20361092E+04	-3.61091620E+01	4.20241950E+04
703	2.49193548E+00	4.23960000E+04	4.20406431E+04	3.55356911E+02	4.20288323E+04
704	2.50403226E+00	4.20270000E+04	4.20452014E+04	-1.82013949E+01	4.20334926E+04
705	2.51612903E+00	4.19630000E+04	4.20497841E+04	-8.67840565E+01	4.20381760E+04
706	2.52822581E+00	4.20610000E+04	4.20543911E+04	6.60894856E+00	4.20428824E+04
707	2.54032258E+00	4.21570000E+04	4.20590224E+04	9.79776424E+01	4.20476119E+04
708	2.55241935E+00	4.19630000E+04	4.20636780E+04	-1.00677954E+02	4.20523644E+04
709	2.56451613E+00	4.19230000E+04	4.20683578E+04	-1.45357818E+02	4.20571399E+04
710	2.57661290E+00	4.22900000E+04	4.20730619E+04	2.16938069E+02	4.20619385E+04
711	2.58670968E+00	4.18840000E+04	4.20777903E+04	-1.93790271E+02	4.20667602E+04
712	2.60080645E+00	4.21910000E+04	4.20825428E+04	1.08457181E+02	4.20716048E+04
713	2.61290323E+00	4.23340000E+04	4.20873196E+04	2.46680444E+02	4.20764725E+04
714	2.62500000E+00	4.22350000E+04	4.20921205E+04	1.42879538E+02	4.20813633E+04
715	2.63709677E+00	4.20430000E+04	4.20969455E+04	-5.39455196E+01	4.20862771E+04
716	2.64919355E+00	4.21760000E+04	4.21017947E+04	7.42052903E+01	4.20912139E+04

717	2.66129032E+00	4.222570000E+04	4.21066680E+04	1.50331985E+02	4.20961728E+04
718	2.67338710E+00	4.18990000E+04	4.21115654E+04	-2.12565417E+02	4.21011567F+04
719	2.68548387E+00	4.10390000E+04	4.21164869E+04	-2.77486900E+02	4.21061626E+04
720	2.69758065E+00	4.21310000E+04	4.21214324E+04	9.56755365E+00	4.21111916E+04
721	2.70967742E+00	4.20560000E+04	4.21264020E+04	-7.04020398E+01	4.21162436E+04
722	2.72177419E+00	4.23350000E+04	4.21313957E+04	2.03604336E+02	4.21213187E+04
723	2.73387097E+00	4.21400000E+04	4.21364133E+04	3.58669633E+00	4.21264168E+04
724	2.74596774E+00	4.21140000E+04	4.21414549E+04	-2.74549429E+01	4.21315380F+04
725	2.75806452E+00	4.20390000E+04	4.21465206E+04	-1.07520567E+02	4.21366821E+04
726	2.771016129E+00	4.20280000E+04	4.21516102E+04	-1.23610160E+02	4.21418454E+04
727	2.78225806E+00	4.22340000E+04	4.21567237E+04	7.72762916E+01	4.21470396E+04
728	2.79435484E+00	4.19140000E+04	4.21618612E+04	-2.47861158E+02	4.21522530E+04
729	2.80645161E+00	4.18800000E+04	4.21670226E+04	-2.87022613E+02	4.21574893E+04
730	2.81854839E+00	4.20210000E+04	4.21722079E+04	-1.51207942E+02	4.21627487E+04
731	2.83046451E+00	4.23070000E+04	4.21774172E+04	1.29582829E+02	4.21680311E+04
732	2.842747194E+00	4.21520000E+04	4.21826503E+04	-3.06502851E+01	4.21733366E+04
733	2.85483871E+00	4.19820000E+04	4.21879073E+04	-2.05907273E+02	4.21786651F+04
734	2.86693548E+00	4.21300000E+04	4.21931881E+04	-6.31881214E+01	4.21840167E+04
735	2.87903226E+00	4.24150000E+04	4.21984928E+04	2.16507182E+02	4.21893913E+04
736	2.89112903E+00	4.21730000E+04	4.22038214E+04	-3.08213501E+01	4.21947889E+04
737	2.90322581E+00	4.18510000E+04	4.22091737E+04	-3.58173706E+02	4.22020966E+04
738	2.91532258E+00	4.23030000E+04	4.22145499E+04	8.84501257E+01	4.22056533E+04
739	2.92741935E+00	4.22270000E+04	4.22199498E+04	7.05015711E+00	4.22111200E+04
740	2.93951613E+00	4.23910000E+04	4.22253736E+04	1.65626399E+02	4.22166098E+04
741	2.95161290E+00	4.17400000E+04	4.22308211E+04	-4.90821136E+02	4.22221227E+04
742	2.96370968E+00	4.22530000E+04	4.22362924E+04	1.67075613E+01	4.22276586F+04
743	2.97580645E+00	4.24380000E+04	4.22417875E+04	1.98212502E+02	4.22332175E+04
744	2.98790323E+00	4.20680000E+04	4.2247306302E+04	-1.79306302E+02	4.22387994E+04
745	3.00000000E+00	4.23910000E+04	4.22528488E+04	1.38151158E+02	4.22444044E+04
746	3.01209677E+00	4.20540000E+04	4.22584151E+04	-2.04415108E+02	4.22500325E+04
747	3.02419355E+00	4.21810000E+04	4.22640051E+04	-8.30050881E+01	4.22556835F+04
748	3.03629032E+00	4.25570000E+04	4.22696188E+04	2.87981226E+02	4.22613577E+04
749	3.04838710E+00	4.21910000E+04	4.22752562E+04	-8.42561560E+01	4.22670548E+04
750	3.06048387E+00	4.22830000E+04	4.22809172E+04	2.08277571E+00	4.22727750E+04
751	3.07258065E+00	4.22490000E+04	4.22866020E+04	-3.76019698E+01	4.22785183E+04
752	3.08467742E+00	4.24940000E+04	4.22923104E+04	2.01689617E+02	4.22842845E+04
753	3.09677419E+00	4.20140000E+04	4.22980425E+04	-2.84042456E+02	4.22900739E+04
754	3.10887097E+00	4.289490000E+04	4.23037982E+04	5.45201821E+02	4.22958862E+04
755	3.12096774E+00	4.20390000E+04	4.23095775E+04	-2.70577543E+02	4.23017216E+04
756	3.13306452E+00	4.24070000E+04	4.23153805E+04	9.16194587E+01	4.23075801E+04
757	3.14516129E+00	4.25080000E+04	4.23212072E+04	1.86792836E+02	4.23134615E+04
758	3.15725806E+00	4.24900000E+04	4.23270574E+04	1.62942597E+02	4.23193661E+04
759	3.16935484E+00	4.25550000E+04	4.23329313E+04	2.22068748E+02	4.23252936F+04
760	3.18145161E+00	4.22050000E+04	4.23388287E+04	-1.33828700E+02	4.23312442E+04
761	3.19354839E+00	4.23740000E+04	4.23447497E+04	2.92502577E+01	4.23372179E+04
762	3.20564516E+00	4.21710000E+04	4.23506944E+04	-1.79694370E+02	4.23432146F+04
763	3.21774194E+00	4.23980000E+04	4.23566626E+04	4.13374254E+01	4.23492343F+04
764	3.22983871E+00	4.22170000E+04	4.23626544E+04	-1.46564350E+02	4.23552770E+04
765	3.24193548E+00	4.25670000E+04	4.23686697E+04	1.9830311E+02	4.23613429E+04
766	3.25403226E+00	4.25300000E+04	4.23747086E+04	1.55291416E+02	4.23674317E+04
767	3.26612903E+00	4.22410000E+04	4.23807710E+04	-1.39771028E+02	4.23735436F+04
768	3.27822581E+00	4.20210000E+04	4.23868570E+04	-3.65857014E+02	4.23796785E+04
769	3.29032258E+00	4.24880000E+04	4.23929665E+04	9.50334637E+01	4.23858365E+04
770	3.30241935E+00	4.25500000E+04	4.23990996E+04	1.50900413E+02	4.23920175E+04
771	3.31451613E+00	4.22420000E+04	4.24052562E+04	-1.63256160E+02	4.23982215E+04
772	3.32661290E+00	4.24800000E+04	4.24114362E+04	6.85637513E+01	4.24044486F+04
773	3.33870968E+00	4.22060000E+04	4.24176398E+04	-2.11639847E+02	4.24106987F+04
774	3.35080645E+00	4.25460000E+04	4.24238669E+04	1.22133051E+02	4.24169719E+04
775	3.36290323E+00	4.23250000E+04	4.24301175E+04	-1.05117548E+02	4.24232681E+04
776	3.37500000E+00	4.21170000E+04	4.24363916E+04	-3.19391638E+02	4.24295874E+04
777	3.38709677E+00	4.25270000E+04	4.24426892E+04	8.43107872E+01	4.24359297E+04
778	3.39919355E+00	4.22140000E+04	4.24490103E+04	-2.35010267E+02	4.24422950F+04
779	3.41129032E+00	4.27590000E+04	4.24553548E+04	3.02645204E+02	4.24486834E+04
780	3.42338710E+00	4.21570000E+04	4.24617228E+04	-3.04722792E+02	4.24550948E+04

APPENDIX C – Continued

781	3.43548387E+00	4.23030000E+04	4.24681143E+04	-1.65114251E+02	4.24615292E+04
782	3.44758065E+00	4.24120000E+04	4.24745292E+04	-6.25291673E+01	4.24679867E+04
783	3.45967742E+00	4.26000000E+04	4.24809675E+04	1.19032465E+02	4.24744672E+04
784	3.47177419E+00	4.25910000E+04	4.24874293E+04	5.03570651E+02	4.24809708E+04
785	3.48387097E+00	4.24190000E+04	4.24939146E+04	-7.49146047E+01	4.24874974E+04
786	3.49596774E+00	4.19760000E+04	4.25004233E+04	-5.24423296E+02	4.24940471E+04
787	3.50806452E+00	4.22080000E+04	4.25069554E+04	-2.98955419E+02	4.25006198E+04
788	3.52016129E+00	4.29440000E+04	4.25135110E+04	4.30489032E+02	4.25072155E+04
789	3.53225806E+00	4.24650000E+04	4.25200899E+04	-5.50899377E+01	4.25138343E+04
790	3.54435484E+00	4.26650000E+04	4.25266923E+04	1.38307676E+02	4.25204761E+04
791	3.55645161E+00	4.26180000E+04	4.25333181E+04	8.46818775E+01	4.25271409E+04
792	3.56854839E+00	4.23840000E+04	4.25399673E+04	-1.55967328E+02	4.2538288E+04
793	3.58064516E+00	4.25370000E+04	4.25466399E+04	-9.63993574E+00	4.25405398E+04
794	3.59274194E+00	4.25880000E+04	4.25533359E+04	3.46640584E+01	4.25472737E+04
795	3.60483871E+00	4.25160000E+04	4.25600553E+04	-4.40553411E+01	4.25540308E+04
796	3.61693548E+00	4.28040000E+04	4.25667981E+04	2.37201870E+02	4.25608108E+04
797	3.62903226E+00	4.25570000E+04	4.25735643E+04	-1.65643035E+01	4.25676139E+04
798	3.64112903E+00	4.24180000E+04	4.25803539E+04	-1.62353858E+02	4.25744400E+04
799	3.65322581E+00	4.23080000E+04	4.25871668E+04	-2.79166789E+02	4.25812892E+04
800	3.66532258E+00	4.27190000E+04	4.25940031E+04	1.24996908E+02	4.25881614E+04
801	3.67741935E+00	4.22410000E+04	4.26008628E+04	-3.59862763E+02	4.25950567E+04
802	3.68951613E+00	4.28050000E+04	4.26077485E+04	1.97254201E+02	4.26019750E+04
803	3.70161290E+00	4.26790000E+04	4.261616522E+04	6.33478041E+01	4.26089163E+04
804	3.71370968E+00	4.26340000E+04	4.26215819E+04	1.24180510E+01	4.26158807E+04
805	3.727580645E+00	4.25110000E+04	4.26285351E+04	-1.17535055E+02	4.26228681E+04
806	3.73790323E+00	4.29440000E+04	4.26355115E+04	3.08488490E+02	4.26298786E+04
807	3.75000000E+00	4.25270000E+04	4.26425113E+04	-1.15511310E+02	4.26369121E+04
808	3.76209677E+00	4.29240000E+04	4.26495345E+04	2.74465548E+02	4.26439686E+04
809	3.77419355E+00	4.26440000E+04	4.26565809E+04	-1.25809325E+01	4.26510482E+04
810	3.78629032E+00	4.26000000E+04	4.26636507E+04	-6.36507473E+01	4.26581508E+04
811	3.79838710E+00	4.23020000E+04	4.26707439E+04	-3.68743893E+02	4.26652765E+04
812	3.81048387E+00	4.27600000E+04	4.26778604E+04	8.21396330E+01	4.26724252E+04
813	3.82250656E+00	4.29400000E+04	4.26850002E+04	2.54999835E+02	4.26795969E+04
814	3.83467742E+00	4.26530000E+04	4.26921633E+04	-3.91632842E+01	4.26867917E+04
815	3.84677419E+00	4.28160000E+04	4.26993497E+04	1.16650279E+02	4.26940095E+04
816	3.85887097E+00	4.27420000E+04	4.27065595E+04	3.54405276E+01	4.27012504E+04
817	3.87096774E+00	4.27650000E+04	4.27137925E+04	5.12074650E+01	4.27085143E+04
818	3.88306452E+00	4.25740000E+04	4.27210489E+04	-1.47048906E+32	4.27158012E+04
819	3.89516129E+00	4.27550000E+04	4.27283286E+04	2.66714181E+01	4.27231112E+04
820	3.90725806E+00	4.32210000E+04	4.27356316E+04	4.85368440E+02	4.27304443E+04
821	3.91935484E+00	4.26280000E+04	4.27429578E+04	-1.14957837E+02	4.27378003E+04
822	3.93145161E+00	4.26640000E+04	4.27503740E+04	-8.63074102E+01	4.27451794E+04
823	3.94354839E+00	4.27730000E+04	4.27576803E+04	1.53197234E+01	4.27525816E+04
824	3.95564516E+00	4.29460000E+04	4.27650764E+04	1.80923567E+02	4.27600068E+04
825	3.96774194E+00	4.30170000E+04	4.27724959E+04	2.44504123E+02	4.27674550E+04
826	3.97983871E+00	4.26690000E+04	4.27799386E+04	-1.10938606E+02	4.27749262E+04
827	3.99193548E+00	4.26470000E+04	4.27874046E+04	-1.40404617E+02	4.27824206E+04
828	4.00432266E+00	4.24300000E+04	4.27948939E+04	-3.64893937E+02	4.27899379E+04
829	4.01612903E+00	4.28220000E+04	4.28024065E+04	1.95935268E+01	4.27974783E+04
830	4.02822581E+00	4.26950000E+04	4.28099423E+04	-1.14942314E+02	4.28050417E+04
831	4.04032258E+00	4.30270000E+04	4.28175014E+04	2.09498575E+02	4.28126282E+04
832	4.05241935E+00	4.28160000E+04	4.28250838E+04	-1.50838054E+01	4.28202377E+04
833	4.06451613E+00	4.27230000E+04	4.28326895E+04	-1.09689452E+02	4.28278702E+04
834	4.07661290E+00	4.26390000E+04	4.28403184E+04	-2.01318362E+02	4.28355258E+04
835	4.08870968E+00	4.33530000E+04	4.28479705E+04	5.05029467E+02	4.28422045E+04
836	4.10080645E+00	4.30160000E+04	4.28556460E+04	1.60354037E+02	4.28509061E+04
837	4.11290323E+00	4.30430000E+04	4.28633446E+04	1.79655350E+02	4.28586308E+04
838	4.12500000E+00	4.29110000E+04	4.28710666E+04	3.99334098E+01	4.28663786E+04
839	4.13709677E+00	4.24450000E+04	4.28788118E+04	-4.33811782E+02	4.28741494E+04
840	4.14919355E+00	4.29830000E+04	4.28865802E+04	9.64197761E+01	4.28819432E+04
841	4.16112903E+00	4.27420000E+04	4.28943719E+04	-1.52371913E+02	4.28897601E+04
842	4.17338710E+00	4.28890000E+04	4.29021868E+04	-1.31868461E+01	4.28976000E+04
843	4.18548387E+00	4.30980000E+04	4.29100250E+04	1.897974978E+02	4.29054629E+04
844	4.19758065E+00	4.32840000E+04	4.29178864E+04	3.66113561E+02	4.29133489E+04

845	4.20967742E+00	4.28110000E+04	4.29257711E+04	-1.14771094E+02	4.29212580E+04
846	4.22177419E+00	4.28660000E+04	4.29336790E+04	-6.76789852E+01	4.29291900E+04
847	4.23387097E+00	4.27110000E+04	4.29416101E+04	-2.30610111E+02	4.29371452E+04
848	4.24596774E+00	4.32990000E+04	4.29495645E+04	3.49435532E+02	4.29451233E+04
849	4.258C6452E+CC	4.30310000E+04	4.29575421E+04	7.34579445E+01	4.29531245F+04
850	4.27016129E+00	4.28560000E+04	4.29655429E+04	-1.09542871E+02	4.29611487E+04
851	4.28225806E+CC	4.30130000E+04	4.29735669E+04	3.94330875E+01	4.29651960E+04
852	4.29435484E+00	4.28060000E+04	4.29816142E+04	-1.75614178E+02	4.29772663E+04
853	4.30645161E+00	4.31290000E+04	4.29896847E+04	1.39315334E+02	4.29853597E+04
854	4.31854639E+00	4.28720000E+04	4.29977784E+04	-1.25778374E+02	4.29934761E+04
855	4.33064516E+00	4.26260000E+04	4.30058953E+04	-3.79895300E+02	4.30016155E+04
856	4.34274194E+00	4.3C790000E+04	4.30140354E+04	6.49645570F+01	4.30097780E+04
857	4.35483871E+00	4.31270000E+04	4.30221988E+04	1.04801199E+02	4.30179635E+04
858	4.36693548E+00	4.3C620000E+04	4.30303854E+04	3.16146291E+01	4.30261721E+04
859	4.37903226E+00	4.33050000E+04	4.30385952E+04	2.66404848E+02	4.30344037E+04
860	4.39112503E+00	4.33490000E+04	4.30468281E+04	3.02171857E+02	4.30426583E+04
861	4.40322581E+00	4.29730000E+04	4.30550843E+04	-8.20843415E+01	4.30509360E+04
862	4.41532258E+00	4.32250000E+04	4.30633637E+04	1.61636254E+02	4.30592367E+04
863	4.42741935E+00	4.27510000E+04	4.30716664E+04	-3.20666354E+02	4.30675605F+04
864	4.43951613E+00	4.25090000E+04	4.30799922E+04	-5.70992165E+02	4.30759073E+04
865	4.45161290E+00	4.31580000E+04	4.30883412E+04	6.96588235E+01	4.30842771E+04
866	4.46370968E+00	4.31620000E+04	4.30967134E+04	6.52866126E+01	4.30926700E+04
867	4.47580645E+00	4.31370000E+04	4.31051088E+04	3.18912041E+01	4.31010859E+04
868	4.48790323E+00	4.31300000E+04	4.31135274E+04	1.64725996E+01	4.31095249E+04
869	4.50CCCC00E+00	4.25660000E+04	4.31219692E+04	-1.55969199E+02	4.31179869E+04
870	4.51209677E+00	4.31400000E+04	4.31304342E+04	9.56580891E+00	4.31264719E+04
871	4.52419355E+00	4.29530000E+04	4.31389224E+04	-1.85922374E+02	4.31349800E+04
872	4.53629032E+00	4.28370000E+04	4.31474337E+04	-3.10433747E+02	4.31435111E+04
873	4.54838710E+00	4.32910000E+04	4.31559683E+04	1.35031691E+02	4.31520653E+04
874	4.56048387E+00	4.30650000E+04	4.31645261E+04	-9.95260568E+01	4.31606425E+04
875	4.57258065E+00	4.29360000E+04	4.31731070E+04	-2.37106950E+02	4.31692427E+04
876	4.58467742E+00	4.31610000E+04	4.31817111E+04	-2.07111080E+01	4.31778660E+04
877	4.59677419E+00	4.34290000E+04	4.31903384E+04	2.38661592E+02	4.31865123E+04
878	4.60887097E+00	4.35400000E+04	4.31989889E+04	3.41011111E+02	4.31951817E+04
879	4.62096774E+00	4.30590000E+04	4.32076626E+04	-1.48662551E+02	4.32038741E+04
880	4.633C6452E+00	4.30420000E+04	4.32163594E+04	-1.74359390E+02	4.32125896E+04
881	4.64516129E+00	4.31400000E+04	4.32250794E+04	-8.50794066E+01	4.32213280E+04
882	4.65723580E+00	4.33160000E+04	4.32332822E+04	8.21774012E+01	4.32300866E+04
883	4.66935484E+00	4.33180000E+04	4.32425890E+04	7.54110346E+01	4.32388741E+04
884	4.68145161E+00	4.33870000E+04	4.32513785E+04	1.35621495E+02	4.32476817E+04
885	4.69354839E+CC	4.26930000E+04	4.32601912E+04	-5.67191217E+02	4.32565124E+04
886	4.70564516E+00	4.33900000E+04	4.32690271E+04	1.20972901E+02	4.32653661E+04
887	4.71774194E+00	4.32500000E+04	4.32778862E+04	4.71138499E+01	4.32742428E+04
888	4.72983871E+00	4.35710000E+04	4.32867684E+04	2.84231631E+02	4.32831426E+04
889	4.74193548E+00	4.32310000E+04	4.32956738E+04	-6.46737557E+01	4.32920654E+04
890	4.75403226E+00	4.29910000E+04	4.33046023E+04	-3.13602307E+02	4.33010112E+04
891	4.76612903E+00	4.33500000E+04	4.33135540E+04	3.64459764E+01	4.33099801E+04
892	4.77822581E+00	4.29840000E+04	4.33225289E+04	-3.38528903E+02	4.33189720F+04
893	4.79032258E+00	4.33730000E+04	4.33315269E+04	4.14730556E+01	4.33279870E+04
894	4.80241935E+CC	4.34190000E+04	4.33405481E+04	7.84518532E+01	4.33370250E+04
895	4.81451613E+00	4.31590000E+04	4.33495925E+04	-1.09592509E+02	4.33460861F+04
896	4.82661290E+00	4.32620000E+04	4.33586600E+04	-9.66600296E+01	4.33551702E+04
897	4.83870968E+00	4.37290000E+04	4.33677507E+04	3.61249292E+02	4.33642773E+04
898	4.85080645E+00	4.29180000E+04	4.33768645E+04	-4.58864542E+02	4.33734075E+04
899	4.86290323E+00	4.3C900000E+04	4.33860015E+04	-2.96001532E+02	4.33825607E+04
900	4.87500000E+00	4.33710000E+04	4.33951617E+04	-2.41616765E+01	4.33917369E+04
901	4.88709677E+00	4.34520000E+04	4.34043450E+04	4.76550261E+01	4.34009362E+04
902	4.89919355E+00	4.34430000E+04	4.34135514E+04	2.94485766E+01	4.34101586E+04
903	4.91129032E+00	4.38090000E+04	4.34227810E+04	3.86218976E+02	4.34194039E+04
904	4.92338710E+00	4.33280000E+04	4.34320338E+04	-1.04033775E+02	4.34286723E+04
905	4.93548387E+00	4.37540000E+04	4.34413097E+04	3.12690326E+02	4.34379638E+04
906	4.94758065E+00	4.33710000E+04	4.34506087E+04	-7.96087221E+01	4.34472783E+04
907	4.95567742E+00	4.35240000E+04	4.34599309E+04	6.40690831E+01	4.34566158E+04
908	4.97177419E+00	4.30510000E+04	4.34692763E+04	-4.18276258E+02	4.34659764E+04

APPENDIX C – Continued

909	4.98387097E+00	4.33290000E+04	4.34786447E+04	-1.49644744E+02	4.34753600E+04
910	4.99596774E+00	4.33340000E+04	4.34880336E+04	-1.54036374E+02	4.34847667E+04
911	5.00806452E+00	4.34720000E+04	4.34974511E+04	-2.54511472E+01	4.34941964E+04
912	5.02016129E+00	4.35810000E+04	4.35068891E+04	7.41109372E+01	4.35036491E+04
913	5.03225806E+00	4.31440000E+04	4.35163501E+04	-3.72350120E+02	4.35131249E+04
914	5.04435484E+00	4.37540000E+04	4.35258343E+04	2.28165683E+02	4.35226237E+04
915	5.05645161E+00	4.33350000E+04	4.35353417E+04	-2.00341654E+02	4.35321456E+04
916	5.06854839E+00	4.36430000E+04	4.35448721E+04	9.81278706E+01	4.35416905E+04
917	5.08064516E+00	4.36120000E+04	4.35544257E+04	5.75742574E+01	4.35512584E+04
918	5.09274194E+00	4.35700000E+04	4.35640025E+04	5.99750730E+00	4.35608494E+04
919	5.10483871E+00	4.31860000E+04	4.35736024E+04	-3.87602379E+02	4.35704634E+04
920	5.11693548E+00	4.35440000E+04	4.35832254E+04	-3.92254000E+01	4.35801005E+04
921	5.12903226E+00	4.35000000E+04	4.35929716E+04	-9.28715556E+01	4.35897606E+04
922	5.14112903E+00	4.34650000E+04	4.36025408E+04	-1.37540845E+02	4.35994437E+04
923	5.15322581E+00	4.35610000E+04	4.36122333E+04	-5.12332662E+01	4.36091499E+04
924	5.16532258E+00	4.35010000E+04	4.36219488E+04	-1.20948820E+02	4.36188701E+04
925	5.17741935E+00	4.34290000E+04	4.36316875E+04	-2.02687504E+02	4.36286314E+04
926	5.18951613E+00	4.34930000E+04	4.36414493E+04	-1.48449319E+02	4.36384067E+04
927	5.20161290E+00	4.36680000E+04	4.36512343E+04	2.16765737E+02	4.36482050E+04
928	5.21370596E+00	4.40690000E+04	4.36610423E+04	4.07957664E+02	4.36580264E+04
929	5.22580645E+00	4.35880000E+04	4.36708735E+04	3.17126464E+02	4.36678708E+04
930	5.23790323E+00	4.34520000E+04	4.36807279E+04	-2.28727864E+02	4.36777383E+04
931	5.25000000E+00	4.39630000E+04	4.36906053E+04	2.72394682E+02	4.36876288E+04
932	5.26209677E+00	4.37000000E+04	4.37005059E+04	-5.05897611E-01	4.36975423E+04
933	5.27419355E+00	4.33760000E+04	4.37104296E+04	-3.34429602E+02	4.37074789E+04
934	5.28629032E+00	4.38140000E+04	4.37203764E+04	9.36235693E+01	4.37174385E+04
935	5.29838710E+00	4.37960000E+04	4.37303464E+04	6.56536173E+01	4.37274212E+04
936	5.31048387E+00	4.37880000E+04	4.37403395E+04	4.76605426E+01	4.37274269E+04
937	5.32258065E+00	4.37530000E+04	4.37503557E+04	2.64434559E+00	4.37474557E+04
938	5.33467742E+00	4.36180000E+04	4.37603950E+04	-1.42394972E+02	4.37575074E+04
939	5.34677419E+00	4.38180000E+04	4.37704574E+04	4.75425896E+01	4.37675823E+04
940	5.35887C97E+00	4.36630000E+04	4.37805453E+04	8.24570312E+01	4.37776801E+04
941	5.37096774E+00	4.40090000E+04	4.37906516E+04	2.18348354E+02	4.37878010E+04
942	5.38306452E+00	4.36750000E+04	4.38007834E+04	-1.25783442E+02	4.37979450E+04
943	5.39516129E+00	4.37150000E+04	4.38109384E+04	-9.59383565E+01	4.38081120E+04
944	5.40725806E+00	4.41030000E+04	4.38211164E+04	2.81883612E+02	4.38183020E+04
945	5.41935484E+00	4.41850000E+04	4.38313175E+04	3.53682465E+02	4.38285151E+04
946	5.43145161E+00	4.39140000E+04	4.38415418E+04	7.24582009E+01	4.38387512E+04
947	5.44354839E+00	4.42270000E+04	4.38517892E+04	3.75210822E+02	4.38490103E+04
948	5.45564516E+00	4.36250000E+04	4.38620597E+04	-2.37059672E+02	4.38592925E+04
949	5.46774194E+00	4.40700000E+04	4.38723533E+04	1.34646721E+02	4.38695977E+04
950	5.47983871E+00	4.38020000E+04	4.38826700E+04	-8.06700004E+01	4.38792960E+04
951	5.49193548E+00	4.35590000E+04	4.38930098E+04	-3.34009834E+02	4.38902773E+04
952	5.50403226E+00	4.40410000E+04	4.39033722E+04	1.37627220E+02	4.39006517E+04
953	5.51612903E+00	4.35770000E+04	4.39137588E+04	6.32411621E+01	4.39110491E+04
954	5.52822581E+00	4.43200000E+04	4.39241680E+04	3.95831953E+02	4.39214695E+04
955	5.54032258E+00	4.40570000E+04	4.39346003E+04	1.22399714E+02	4.39319130E+04
956	5.55241935E+00	4.41870000E+04	4.39450557E+04	2.41944326E+02	4.39423795E+04
957	5.56451613E+00	4.38020000E+04	4.39553542E+04	-1.53534173E+02	4.39528690E+04
958	5.57661290E+00	4.36270000E+04	4.39660358E+04	-3.39035780E+02	4.39633876E+04
959	5.58870968E+00	4.42280000E+04	4.39765605E+04	2.51439505E+02	4.39739173E+04
960	5.60080645E+00	4.40960000E+04	4.39871083E+04	1.088916P3E+02	4.39844759E+04
961	5.61290323E+00	4.41110000E+04	4.39976792E+04	1.13320753E+02	4.39950577E+04
962	5.62500000E+00	4.38930000E+04	4.40082733E+04	-1.25273283E+02	4.40056624E+04
963	5.63709677E+00	4.42370000E+04	4.40188904E+04	2.18109575E+02	4.40162025E+04
964	5.64919355E+00	4.40920000E+04	4.40295307E+04	6.24693277E+01	4.40269410E+04
965	5.66129032E+00	4.37720000E+04	4.40401940E+04	-2.68194025E+02	4.404776149E+04
966	5.67338710E+00	4.40380000E+04	4.40508805E+04	-1.28804813E+01	4.40483118E+04
967	5.68548387E+00	4.42900000E+04	4.40615900E+04	2.28409958E+02	4.40590318E+04
968	5.69758065E+00	4.39130000E+04	4.40723227E+04	-1.59322706E+02	4.40697748E+04
969	5.70967742E+00	4.42590000E+04	4.40830785E+04	1.75921528E+02	4.40805408E+04
970	5.72177419E+00	4.41650000E+04	4.40938573E+04	7.11426587E+01	4.40913299E+04
971	5.73387097E+00	4.39910000E+04	4.41046593E+04	-1.13659312E+02	4.41021420E+04
972	5.74566774E+00	4.41810000E+04	4.41154844E+04	6.55156158E+01	4.41129772E+04

973	5.75806452E+00	4.42690000E+04	4.41263326E+04	1.42667443E+02	4.41238354E+04
974	5.77016129E+00	4.41950000E+04	4.41372038E+04	5.77961694E+01	4.41347166E+04
975	5.78225806E+00	4.44190000E+04	4.41480982E+04	2.70901796E+02	4.41456209E+04
976	5.79435484E+00	4.45170000E+04	4.41590157E+04	3.57984324E+02	4.41565482E+04
977	5.80645161E+00	4.41950000E+04	4.41699562E+04	2.50437520E+01	4.41674086E+04
978	5.81854839E+00	4.44C900000E+04	4.41809199E+04	-1.00919918E+02	4.41784720E+04
979	5.83064516E+00	4.43560000E+04	4.41919067E+04	1.64093314E+02	4.41B94684E+04
980	5.84274194E+00	4.42270000E+04	4.42029166E+04	2.40834483E+01	4.42004879E+04
981	5.85483871E+00	4.35370000E+04	4.42139495E+04	-2.76949514E+02	4.42115304E+04
982	5.86693548E+00	4.42620000E+04	4.42250056E+04	3.69944262E+01	4.42225960E+04
983	5.87903226E+00	4.40630000E+04	4.42360847E+04	-1.73084729E+02	4.42336846E+04
984	5.89112903E+00	4.39110000E+04	4.42471870E+04	-3.36186981E+02	4.42447962E+04
985	5.90322581E+00	4.42440000E+04	4.42583123E+04	-1.43123276E+01	4.42559309E+04
986	5.91532258E+C0	4.43430000E+04	4.42694608E+04	7.35392308E+01	4.42670886E+04
987	5.92741935E+C0	4.44110000E+04	4.42806323E+04	1.30367695E+02	4.427826C4E+04
988	5.93951613E+00	4.43590000E+04	4.42918269E+04	6.71730643E+01	4.42894732E+04
989	5.95161290E+00	4.46010000E+04	4.43030447E+04	2.97955340E+02	4.43007000E+04
990	5.96370968E+00	4.42230000E+04	4.43142855E+04	-9.12854768E+01	4.43119499E+04
991	5.97580645E+00	4.43380000E+04	4.43255494E+04	1.24506132E+01	4.43232229E+04
992	5.98790323E+00	4.43650000E+04	4.43368364E+04	2.81636107E+01	4.43345188E+04
993	6.00000000E+C0	4.44620000E+04	4.43481465E+04	1.13953516E+02	4.43458378E+04

STD= 2.103220E+02

CASE NO. 1 IERR= 2

COEFFICIENTS OF PARABOLA Y= SA*X**2 + B*X + C
 SA= 7.89164728E+01 (+6.832E-C1) B=-8.07869030E+00 (+1.931E+00) C= 4.17639214E+04 (+1.190E+01)

NO. OF ITERATIONS= 2

PARAMETERS FOR PEAK 1

IS=-2.82731400E-01 GAM= 2.90420241E-01
 A= 4.33457466E+03 (+6.869E+C1) P=-2.92731400E-01 (+2.301E-03) CGAM= 1.45210120E-01 (+3.545E-03) ARFA= 1.94686613E+03
 PHI1= 1.03766191E-01 PHI2= 3.79853320E-03 PHI1/PHI2= 2.73174370E+01

CASE NO. 1 IERR= 3

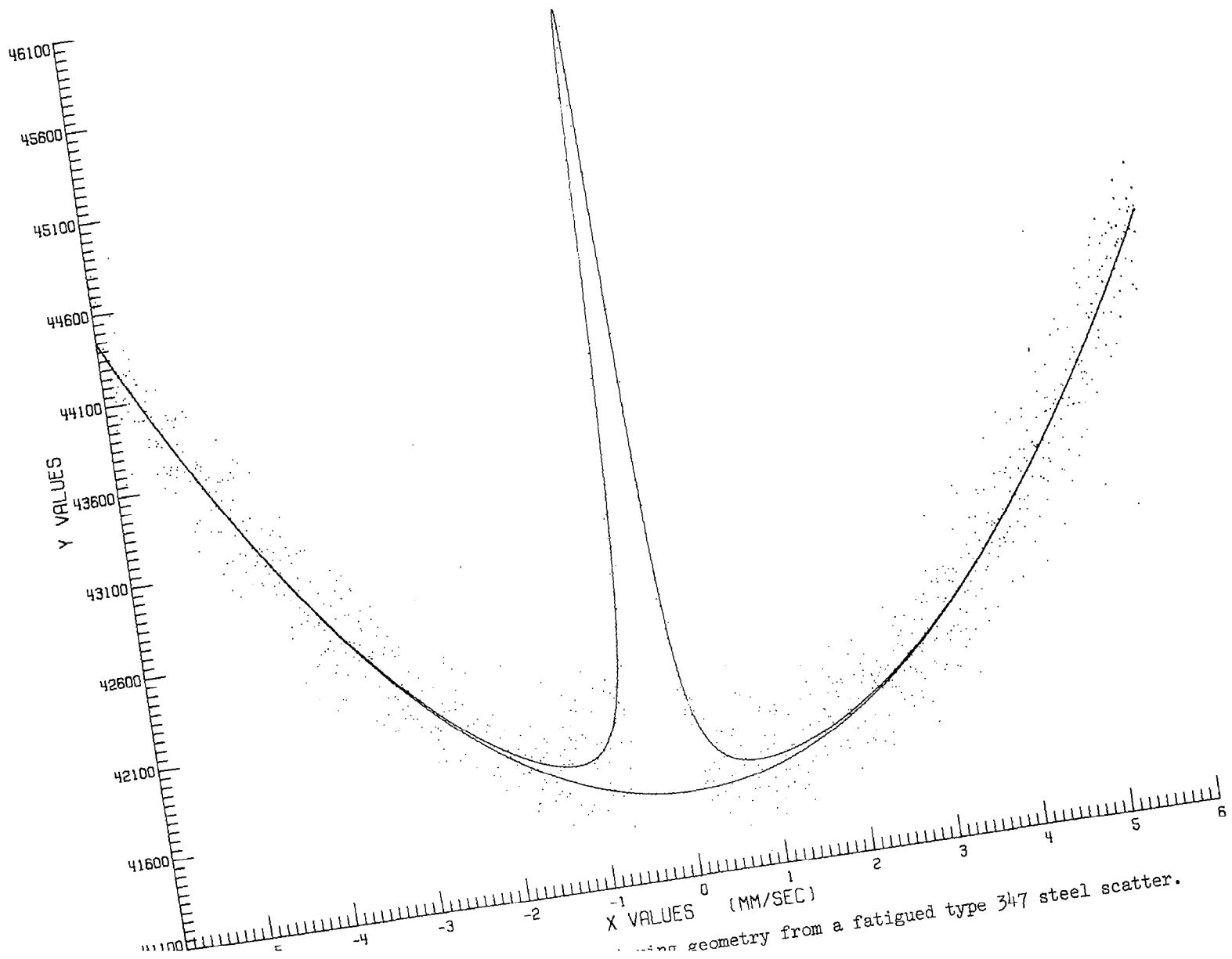
COEFFICIENTS OF PARABOLA Y= SA*X**2 + B*X + C
 SA= 7.85361965E+01 (+6.759E-C1) B=-8.03974281E+00 (+1.922E+00) C= 4.13561687E+04 (+1.184E+01)

NO. OF ITERATIONS= 3

PARAMETERS FOR PEAK 1

IS=-2.82731494E-01 GAM= 2.90411489E-01
 A= 4.31387967E+03 (+6.836E+C1) P=-2.82731494E-01 (+2.300E-03) CGAM= 1.45205744E-01 (+3.544E-03) AREA= 1.93751354E+03
 PHI1= 1.04288865E-01 PHI2= 3.81713460E-03 PHI1/PHI2= 2.73212437E+01

APPENDIX C - Continued



Sample Case 2

Input. -

```

$NAM1 IFLAG=1, IERR=1, IPRT=0,
NP=1, ERROR=6*1.E-6,
AO=-1000, PO=-.2, CGAMD=.2,
SAO=10, BO=3, VELB=6, $
      2        1000
      2 24219   3 24215   4 24207   5 24305   6 24109   7 24438   8 24205   9 24336
     10 24402   11 24216   12 23899   13 24326   14 24497   15 24217   16 24381   17 24335
     18 24392   19 24400   20 24320   21 24261   22 24631   23 24394   24 24391   25 24374
     26 24341   27 24346   28 24172   29 24233   30 24062   31 24238   32 24415   33 24404
     34 24380   35 24476   36 24436   37 24205   38 24413   39 24533   40 24300   41 24343
     42 24443   43 24112   44 24507   45 24421   46 24316   47 24233   48 24616   49 24515
     50 24091   51 24298   52 24324   53 24162   54 24115   55 24222   56 24515   57 24740
     58 24441   59 24598   60 24597   61 24360   62 24437   63 24561   64 24344   65 24648
     66 24379   67 24312   68 24099   69 24354   70 24360   71 24378   72 24570   73 24132
     74 24544   75 24226   76 24508   77 24107   78 24509   79 24093   80 24592   81 24802
     82 24319   83 24534   84 24327   85 24679   86 24143   87 24580   88 24536   89 24495
     90 24454   91 24413   92 24385   93 24338   94 24574   95 24584   96 24595   97 24766
    98 24354   99 24507  100 24519  101 24531  102 24525  103 24619  104 24502  105 24521
   106 24288  107 24592  108 24305  109 24560  110 24443  111 24504  112 24533  113 24390
   114 24445  115 24619  116 24559  117 24335  118 24570  119 24556  120 24183  121 24323
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   130 24706  131 24578  132 24158  133 24488  134 24282  135 24201  136 24756  137 24288
   138 24321  139 24599  140 24403  141 24688  142 24610  143 24927  144 24495  145 24653
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   162 24694  163 24548  164 24512  165 24597  166 24803  167 24584  168 24455  169 24497
   170 24820  171 24368  172 24809  173 24668  174 24652  175 24267  176 24488  177 24789
   178 24595  179 24935  180 24564  181 24676  182 24761  183 24543  184 24617  185 24455
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   210 24819  211 24708  212 24778  213 24678  214 24612  215 24761  216 24585  217 24702
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   226 24729  227 24702  228 24885  229 24466  230 24639  231 24793  232 24333  233 24620
   234 25016  235 24455  236 24936  237 24682  238 24693  239 24737  240 24465  241 24753
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   250 24830  251 24753  252 24913  253 24844  254 24849  255 24697  256 24691  257 24930
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   290 24448  291 25057  292 24585  293 24978  294 24854  295 24648  296 24910  297 24550
   298 24911  299 24920  300 24626  301 24814  302 24789  303 24678  304 24873  305 24747
   306 24731  307 24632  308 24786  309 24798  310 24757  311 24883  312 24791  313 25008
   314 24690  315 24914  316 24878  317 24995  318 25089  319 24669  320 24776  321 24868
   322 24650  323 24839  324 24807  325 24944  326 24658  327 24915  328 24725  329 24902
   330 24678  331 24848  332 25008  333 24933  334 24812  335 24897  336 24944  337 24758
   338 24978  339 24986  340 24945  341 24695  342 25076  343 24862  344 24991  345 24958
   346 24630  347 25115  348 24883  349 24945  350 24870  351 24927  352 24823  353 24632
   354 24569  355 25241  356 24691  357 24823  358 25020  359 24944  360 24692  361 24854
   362 24897  363 24704  364 24663  365 24920  366 25146  367 24724  368 24605  369 24969
   370 24873  371 24923  372 24774  373 24845  374 24915  375 24826  376 24954  377 24981
   378 25145  379 25144  380 24997  381 25134  382 24921  383 25018  384 24726  385 25113
   386 24610  387 24625  388 24971  389 25060  390 25003  391 24918  392 24537  393 24827
   394 25005  395 24916  396 24513  397 24905  398 25162  399 24782  400 24863  401 24873
   402 24828  403 25026  404 24959  405 24888  406 25009  407 25031  408 25029  409 24954
   410 25142  411 25017  412 24923  413 25055  414 25031  415 24864  416 24925  417 24837

```

APPENDIX C – Continued

418	25C86	419	24959	420	24664	421	24989	422	25122	423	24948	424	25123	425	24996
426	24791	427	24681	428	24576	429	24869	430	24793	431	24880	432	24853	433	24553
434	24715	435	24809	436	25072	437	24524	438	24893	439	25342	440	24754	441	24884
442	24737	443	24708	444	24632	445	24819	446	24990	447	24996	448	24535	449	25241
450	25084	451	24857	452	24667	453	24886	454	24760	455	24817	456	24937	457	24856
458	24774	459	24983	460	24831	461	24819	462	25225	463	24664	464	24574	465	24864
466	24829	467	25104	468	24829	469	24674	470	25044	471	24880	472	24821	473	24717
474	24742	475	24736	476	24572	477	24673	478	24521	479	24833	480	24733	481	24645
482	24838	483	24777	484	24773	485	24671	486	24822	487	24847	488	24946	489	25078
490	24725	491	24956	492	24839	493	24737	494	24583	495	25121	496	24634	497	24351
498	24771	499	24893	500	24857	501	24888	502	24904	503	24676	504	24679	505	24675
506	24770	507	24667	508	24686	509	24575	510	24747	511	24487	512	24383	513	24248
514	24619	515	24369	516	24321	517	24397	518	23982	519	24186	520	24160	521	23879
522	24016	523	23697	524	23742	525	23790	526	23796	527	23283	528	23520	529	23394
530	23208	531	23345	532	22978	533	23149	534	23076	535	23231	536	23070	537	22863
538	22788	539	23047	540	23150	541	23144	542	23118	543	23098	544	23420	545	23598
546	23450	547	23665	548	23741	549	23625	550	23723	551	24165	552	23901	553	24197
554	24368	555	24294	556	24533	557	24131	558	24572	559	24400	560	24512	561	24826
562	24581	563	24521	564	24658	565	24428	566	24646	567	24601	568	24410	569	24481
570	24771	571	24816	572	24740	573	25060	574	24530	575	25047	576	24919	577	24412
578	24716	579	24690	580	24813	581	24955	582	24736	583	24866	584	24497	585	24900
586	24732	587	24875	588	24838	589	24949	590	24583	591	24837	592	24754	593	24473
594	24611	595	25025	596	24794	597	24856	598	24884	599	24690	600	24509	601	24758
602	24939	603	24729	604	24752	605	24781	606	24900	607	25007	608	24756	609	24816
610	24445	611	24738	612	24784	613	24892	614	24768	615	24799	616	24920	617	24503
618	25068	619	24795	620	24672	621	24974	622	25008	623	24886	624	24724	625	24856
626	24620	627	25036	628	24779	629	24634	630	24970	631	24902	632	24827	633	24733
634	24950	635	24724	636	24715	637	25124	638	24768	639	25019	640	25189	641	24449
642	24507	643	24802	644	24713	645	24737	646	24728	647	24921	648	24359	649	24561
650	24752	651	24824	652	25119	653	24863	654	24779	655	24950	656	24615	657	24395
658	25192	659	24842	660	25196	661	24449	662	24680	663	24720	664	25206	665	24912
666	24807	667	24893	668	24794	669	24959	670	24837	671	24823	672	24817	673	24519
674	24695	675	24886	676	24881	677	24672	678	24902	679	24836	680	24912	681	24853
682	24837	683	24742	684	24744	685	24476	686	24801	687	24643	688	24782	689	25014
690	24530	691	24922	692	24633	693	24840	694	24892	695	24907	696	24602	697	24901
698	24976	699	24748	700	24867	701	24583	702	24830	703	24823	704	24384	705	24960
706	24965	707	24769	708	24992	709	24804	710	24798	711	24676	712	24418	713	24978
714	24760	715	24712	716	24905	717	24725	718	24851	719	24662	720	24733	721	25023
722	24752	723	24700	724	24674	725	24770	726	24659	727	24792	728	24901	729	24692
730	24641	731	24766	732	24855	733	24754	734	24945	735	24748	736	24939	737	24685
738	24573	739	25020	740	24720	741	24620	742	24685	743	24750	744	24555	745	24697
746	24722	747	24743	748	24496	749	24651	750	24499	751	24831	752	24841	753	24847
754	24671	755	24775	756	24683	757	24766	758	24731	759	24565	760	24682	761	24732
762	24362	763	24774	764	24746	765	24575	766	24352	767	24595	768	24820	769	24754
770	24947	771	24764	772	24847	773	24696	774	24636	775	24878	776	24491	777	24946
778	24849	779	24912	780	24397	781	24859	782	24655	783	24866	784	24711	785	24653
786	24632	787	24843	788	24648	789	24662	790	24606	791	24778	792	24704	793	24779
794	24651	795	24841	796	24754	797	24630	798	24803	799	24498	800	24650	801	24655
802	24558	803	24724	804	24549	805	24666	806	24566	807	24638	808	24587	809	24674
810	24728	811	24629	812	24792	813	24525	814	24743	815	24728	816	24510	817	24692
818	24627	819	24656	820	24673	821	24770	822	24714	823	24765	824	24290	825	24413
826	24700	827	24837	828	24665	829	24323	830	24664	831	24773	832	24672	833	24575
834	24550	835	24639	836	24569	837	24416	838	24651	839	24325	840	24482	841	24712
842	24623	843	24565	844	24608	845	24952	846	24668	847	24306	848	24665	849	24604
850	24534	851	24567	852	24488	853	24455	854	24831	855	24523	856	24476	857	24567
858	24651	859	24425	860	24676	861	24443	862	24723	863	24546	864	24507	865	24769
866	24535	867	24559	868	24846	869	24680	870	24917	871	24294	872	24612	873	24452
874	24496	875	24154	876	24149	877	24521	878	24716	879	24502	880	24689	881	24701
882	24702	883	24479	884	24684	885	24710	886	24604	887	24604	888	24419	889	24515
890	24717	891	24524	892	24443	893	24771	894	24340	895	24614	896	24535	897	24593
898	24888	899	24609	900	24717	901	24346	902	24520	903	24293	904	24575	905	24656
906	24506	907	24488	908	24593	909	24482	910	24235	911	24476	912	24617	913	24511
914	24714	915	24144	916	24353	917	24711	918	24323	919	24620	920	24561	921	24511
922	24282	923	24510	924	24395	925	24386	926	24427	927	24633	928	24338	929	24200

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930 24647 931 24295 932 24361 933 24477 934 24312 935 24611 936 24363 937 24392
938 24374 939 24326 940 24563 941 24472 942 24258 943 24388 944 24594 945 24402
946 24129 947 24324 948 24376 949 24387 950 24237 951 24515 952 24291 953 24304
954 24307 955 24295 956 24342 957 24242 958 24589 959 24463 960 24557 961 24297
962 24476 963 24233 964 24362 965 24183 966 24042 967 24251 968 24212 969 24253
970 24196 971 24203 972 24379 973 24508 974 24485 975 24175 976 24294 977 24442
978 24403 979 24483 980 24317 981 24505 982 24035 983 24129 984 24182 985 24397
986 23918 987 24092 988 24460 989 24419 990 23915 991 24523 992 24339 993 24092
994 24316 995 24277 996 24299 997 24183 998 24253 999 243451000 240971001 24199

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Output.- The computed values given below do not include the velocity calibration correction factor of 1.274.
Figure 7 is included as a sample computer plot.

```

CASE NO.      2      IERR=   1
COEFFICIENTS OF PARABOLA    Y= SA*X**2 + BX + C
SA=-1.87751204E+01(±5.103E-01)      BX=-5.68151598E-01(±1.434E+00)      C= 2.49184310E+04(±8.948E+00)
NC. OF ITERATIONS=     12
PARAMETERS FOR PEAK   1
IS=-4.19525441E-01      GAM=-3.15755782E-01
A=-1.99927587E+03(±4.890E+01)      P=-4.19525441E-01(±3.860E-03)      CGAM=-1.57899891E-01(±5.989E-03)      AREA=-9.75063770E+02
PHI1=-8.02428495E-02      PHI2= 3.29060414E-03      PHI1/PHI2=-2.43854460E+01

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APPENDIX C – Continued

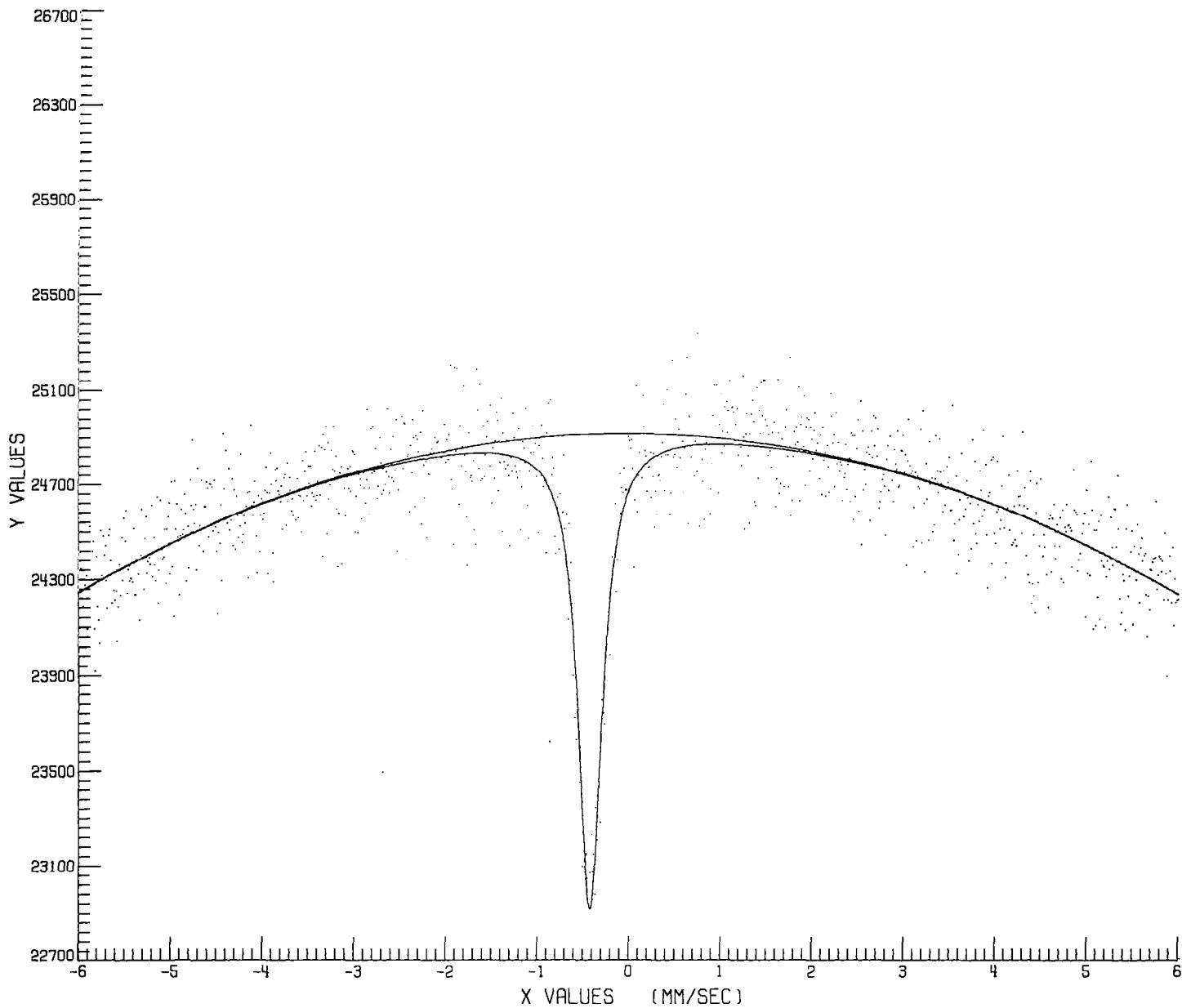


Figure 7.- Transmission Mössbauer spectrum through a 25- μm -thick type 316 steel absorber.

Sample Case 3

Input.-

```

$NAME1 IFLAG=1, IFPRR=1, IPRINT=0,
NP=6, CCAM0=6*.2, FPRPF=21*1.F-5,
P0=-5.5,-3.25,-1.1,.5+.2-.7,4.8,
AO=-1700,-1450,-900,-300,-1450,-2000,
$AN=67., R0=-2.4, VFLR=6, +
      -1015
 2 87291 .3 87741 .4 87402 .5 87727 .6 88032 .7 87528 .8 87798 .9 87380
10 87831 11 87551 12 87599 13 87168 14 87199 15 87037 16 87305 17 87078
18 87703 19 87561 20 87510 21 87692 22 87418 23 87156 24 86592 25 86905
26 86851 27 87223 28 86726 29 86613 30 86376 31 87009 32 86347 33 86484
34 86622 35 86785 36 87597 37 85760 38 85563 39 85815 40 85600 41 86430
42 86231 43 86104 44 85934 45 85439 46 85877 47 85565 48 85445 49 86312
50 85819 51 85809 52 86266 53 86089 54 86601 55 86297 56 86290 57 86228
58 85935 59 86167 60 86155 61 87034 62 86917 63 87072 64 86555 65 86720
66 86849 67 86325 68 87041 69 86875 70 86917 71 86824 72 86491 73 86743
74 87281 75 87360 76 86947 77 87166 78 87133 79 86829 80 86711 81 86881
82 86732 83 86962 84 86743 85 86728 86 87190 87 87046 88 86876 89 86959
90 86807 91 86811 92 87022 93 87117 94 86747 95 86523 96 86661 97 86543
98 96739 .9 86950 100 87272 101 87169 102 87074 103 87510 104 86468 105 86728
106 96662 107 97218 108 86894 109 87053 110 87091 111 86647 112 87051 113 86654
114 86937 115 86782 116 87155 117 87330 118 86612 119 87220 120 86905 121 86690
122 87042 123 86806 124 87225 125 86690 126 87277 127 86643 128 87187 129 87491
130 86937 131 87349 132 86300 133 86762 134 86597 135 86843 136 86581 137 87143
138 86884 139 86593 140 86477 141 87409 142 86897 143 85971 144 86327 145 86910
146 86980 147 86651 148 86700 149 86993 150 86801 151 86678 152 86354 153 86639
154 86388 155 86823 156 87038 157 8657+ 158 86251 159 86658 160 87073 161 86723
162 86184 163 87084 164 87035 165 86519 166 87239 167 86321 168 86388 169 86422
170 96663 171 85937 172 86373 173 83284 174 86843 175 86387 176 86696 177 86654
178 86638 179 86854 180 86256 181 86130 182 86555 183 86132 184 86386 185 86294
186 96526 187 96239 188 87091 189 86052 190 86449 191 86922 192 86303 193 86430
194 96226 195 96214 196 86405 197 86796 198 86833 199 86317 200 86839 201 86579
202 96001 203 86164 204 86693 205 86320 206 86320 207 86038 208 86262 209 85803
210 85543 211 85716 212 85892 213 86339 214 86173 215 86322 216 85949 217 86065
218 85932 219 85803 220 86018 221 85115 222 85112 223 85264 224 85487 225 85176
226 85393 227 84604 228 84575 229 84785 230 84762 231 84538 232 84984 233 84264
234 84927 235 84719 236 84719 237 85302 238 85112 239 83957 240 84936 241 85409
242 85196 243 85205 244 85710 245 85378 246 85509 247 85650 248 85256 249 84778
250 85258 251 85593 252 85573 253 85710 254 85023 255 85770 256 85997 257 85694
253 85622 259 85520 260 85363 261 85119 262 85546 263 85781 264 85636 265 85962
266 86007 267 85358 268 85306 269 86247 270 86249 271 85756 272 85922 273 85743
274 85717 275 85919 276 85219 277 85374 278 86038 279 86235 280 86231 281 85879
292 86483 293 85834 294 86047 295 85993 296 86142 297 86071 298 86441 299 86349
293 96264 294 86234 295 85612 296 85835 297 86009 298 85966 299 86005 297 85986
298 86291 299 86355 300 85865 301 86206 302 86173 303 86448 304 86072 305 86257
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314 85786 315 85564 316 85876 317 85750 318 85715 319 86465 320 86039 321 86354
322 86240 323 86060 324 86014 325 86003 326 85943 327 85949 328 86133 329 85510
330 86726 331 85624 332 85861 333 86333 334 85137 335 85695 336 85231 337 85677
338 85730 339 86117 340 86031 341 86615 342 85240 343 85922 344 85985 345 85949
346 85354 347 85116 348 85641 349 85230 350 85379 351 85240 352 85832 353 85534
354 85837 355 85551 356 85495 357 86166 358 85866 359 85393 360 85931 361 85228
362 85578 363 85216 364 86077 365 85553 366 85844 367 85453 368 85782 369 85526
370 85362 371 86125 372 85844 373 86176 374 85747 375 85620 376 85594 377 85717
378 85896 379 85674 380 85742 381 86228 382 85714 383 85255 384 85823 385 85934
386 85910 387 85723 388 85662 389 85572 390 85832 391 85633 392 85375 393 85577
394 86120 395 85802 396 85913 397 85597 398 85519 399 85542 400 85469 401 85540
402 85880 403 85809 404 85334 405 85296 406 85440 407 85277 408 85465 409 85129
410 85445 411 84715 412 84917 413 84998 414 85221 415 84902 416 84897 417 84676

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APPENDIX C – Continued

418 95275 419 94551 420 94955 421 3+937 422 94916 423 34823 424 84863 425 84796
 426 95275 427 95212 428 95719 429 35789 430 85300 431 95739 432 85241 433 85726
 434 95225 435 95225 434 95470 437 34952 438 85754 439 95420 440 85241 441 95215
 442 95735 443 95697 444 95613 445 35652 446 95721 447 95043 448 95517 449 95476
 450 85386 451 93514 452 95803 453 85921 454 86078 455 85155 456 35239 457 95553
 458 95451 459 95563 460 95776 461 95734 462 95928 463 95849 464 95449 465 95527
 466 35723 467 95415 468 85632 469 45323 470 85315 471 25958 472 85469 473 85212
 474 94382 475 95611 476 95404 477 45541 478 85723 479 95349 480 85515 481 84939
 482 35926 413 95706 494 95413 495 45151 496 35430 497 85492 498 85592 499 85650
 490 35905 491 95659 492 95742 493 35627 494 85513 495 95453 496 85532 497 85934
 498 85702 499 95525 500 95715 501 35404 502 85491 503 95102 504 35411 505 85272
 506 95808 517 95805 520 95634 519 35933 510 84972 511 95526 512 85437 513 95439
 514 95669 515 95779 516 95110 517 34937 518 85333 519 95497 520 85578 521 84934
 522 35354 523 95466 524 85313 525 45615 526 85476 527 85949 528 85671 529 85374
 530 35022 531 95253 532 85330 533 35089 534 85482 535 95162 536 85695 537 85832
 538 85582 539 15311 540 95375 541 35333 542 95236 543 84853 544 84313 545 84910
 546 95171 547 84573 548 95011 549 34497 550 84471 551 94704 552 44745 553 84392
 554 94558 555 84842 556 84466 557 34715 558 84267 559 85306 560 84834 561 84819
 562 35149 563 94766 564 85213 565 85468 566 85418 567 84700 568 35037 569 85386
 570 85476 571 85345 572 85076 573 35425 574 85179 575 85249 576 35457 577 85782
 578 85473 579 95251 580 85608 581 35113 582 85870 583 95269 584 85323 585 95693
 586 85698 587 85391 588 85443 589 35885 590 85824 591 85661 592 35335 593 85331
 594 85633 595 95735 596 85576 597 35426 598 85725 599 86462 600 85713 601 85078
 602 95554 603 85291 604 86193 605 86013 606 86165 607 85420 608 85911 609 95839
 610 85416 611 85647 612 86132 613 35844 614 85754 615 85814 616 85337 617 85437
 618 85436 619 95586 620 85812 621 35408 622 85520 623 85496 624 85791 625 85321
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 634 86022 635 95652 636 95237 637 86150 638 85820 639 85259 640 85603 641 85639
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 674 85723 675 55516 676 85862 677 35163 678 85493 679 85355 680 85611 681 85552
 682 85909 683 85800 684 85970 685 36510 686 86267 687 85437 688 86210 689 96053
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 730 84809 731 84378 732 84414 733 84310 734 84857 735 84241 736 94219 737 94769
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 762 85088 763 95571 764 85549 765 85841 766 86043 767 85612 768 85673 769 860+9
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 778 85992 779 85976 780 85914 781 85276 782 86079 783 85939 784 86133 785 85983
 786 86513 787 85904 788 85590 789 85903 790 86413 791 86175 792 86119 793 86300
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 802 86493 803 85212 804 86547 805 86033 806 86339 807 46226 808 86001 809 86476
 810 86935 811 86464 812 86557+ 813 36360 814 86052 815 87010 816 86656 817 86421
 818 86129 819 86616 820 86451 821 86317 822 86162 823 86473 824 86132 825 86429
 825 85227 827 87017 828 86949 829 86642 830 86586 831 86903 832 86434 833 86253
 834 86581 835 86405 836 86220 837 87143 838 86330 839 86771 840 86773 841 86349
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 898 85944 899 85000 900 86094 901 35392 902 86141 903 86550 904 86327 905 85259
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 970 87760 971 97136 972 87412 973 87946 974 87890 975 87256 976 87435 977 87862
 978 87541 979 87180 980 87350 981 88123 982 87598 983 97213 984 87345 985 87623
 986 87595 987 88004 988 87953 989 88115 990 87584 991 87421 992 87740 993 87501
 994 88221 995 88041 996 87742 997 88173 998 87612 999 878081000 881951001 87831
 1002 880501003 877621004 876931005 872441006 877481007 877710008 877131009 88156
 1010 878681011 875381012 878631013 879781014 881461015 878191016 87867

Output. - The computed values given below do not include the velocity calibration correction factor of 1.274.

Figure 8 is included as a sample computer plot.

```
CASE NO. 3      IFKRR= 1
COEFFICIENTS OF PARABOLA  Y= SA*X**2 + B*X + C
SA= 6.7C8C6850E+01(±1.491E+00)      B= 2.39187959E+00(±5.251E+00)      C= 8.56128891E+04(±2.223E+01)

NO. OF ITERATIONS= 11
PARAMETERS FOR PEAK 1
IS=-5.49C52583E+00      GAM= 4.1611C817E-01
A=-1.75334715E+03(±8.448E+01)      P=-5.490525983E+00(±9.348E-03)      CGAM= 2.08055408E-01(±1.914E-02)      AREA=-9.97995019E+02

PARAMETERS FOR PEAK 2
IS=-3.26347788E+00      GAM= 3.04767054E-01
A=-1.65571508E+03(±9.160E+01)      P=-3.26347788E+00(±8.427E-03)      CGAM= 1.52383547E-01(±1.377E-02)      AREA=-7.74450772E+02

PARAMETERS FOR PEAK 3
IS=-1.066E1911E+00      GAM= 2.00218439E-01
A=-8.55074490E+02(±1.126E+02)      P=-1.066E1911E+00(±1.262E-02)      CGAM= 1.00159220E-01(±1.940E-02)      AREA=-2.78553196E+02

PARAMETERS FOR PEAK 4
IS= 5.19C2t397E-01      GAM= 2.15334893E-01
A=-1.06891543E+03(±1.0d8E+02)      P= 5.19028397E-01(±1.095E-02)      CGAM= 1.07667446E-01(±1.711E-02)      AREA=-3.57397985E+02

PARAMETERS FOR PEAK 5
IS= 2.6E705C65E+00      GAM= 3.472E4113E-01
A=-1.6836C837E+03(±8.587E+01)      P= 2.68705C65E+00(±8.841E-03)      CGAM= 1.73642057E-01(±1.430E-02)      AREA=-8.97278080E+02

PARAMETERS FOR PEAK 6
IS= 4.80368961E+00      GAM= 3.59413650E-01
A=-2.00C75135E+03(±8.482E+01)      P= 4.80368961E+00(±7.592E-03)      CGAM= 1.79706825E-01(±1.339E-02)      AREA=-1.06996566E+03

THESE PARAMETERS HAVE BEEN OBTAINED FOR MULTIPLE PEAKS
IS= -3.1581686E-01      CS= 2.7603247E-02      GC1= 3.7528698E+00      GC2= 3.7825063E+00      GI= 2.1966588E+00
M1= 1.1242091E+00      M2= 1.2370192E+00      PHI= 4.2194604E-03
```

APPENDIX C – Concluded

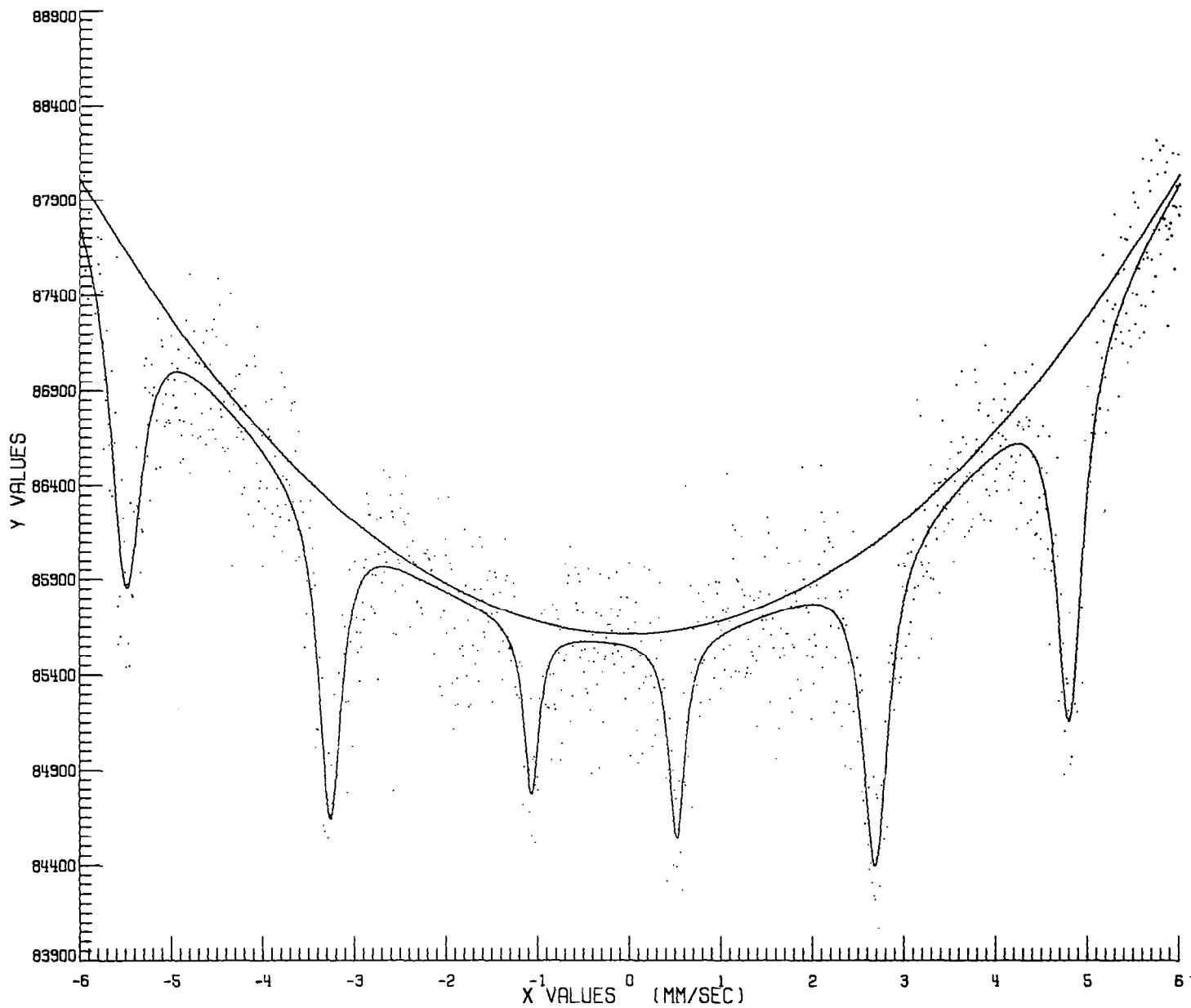


Figure 8.- Transmission Mössbauer spectrum through a 25- μ m-thick AISI C1095 steel absorber.

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